Workforce Optimization: the General Task-based Shift Generation Problem

Kimmo Nurmi, Nico Kyngäs and Jari Kyngäs

Abstract— Workforce scheduling studies have mainly focused on staff rostering, i.e. assigning employees to shifts and determining working days and rest days. In the recent years, the generation of shifts has gained increasing interest in academic community. Shift generation is the process of determining the shift structure, along with the tasks to be carried out in particular shifts and the competences required for different shifts. Application areas of staff rostering and shift generation include hospitals, retail stores, call centers, cleaning, home care, guarding, manufacturing and delivery of goods. This paper presents the General Task-based Shift Generation Problem (GTSGP). To the best of our knowledge, the problem has not been studied in the literature. The GTSGP is to create anonymous shifts and assign tasks to these shifts so that employees can be assigned to the shifts. The targeted tasks must be completed within a given time window. Tasks may have precedence constraints and transition times between tasks are considered. The goal is to maximize the number of shifts employees are able to execute. We present the first computational results of solving GTSGP instances. We briefly describe the PEAST algorithm, which is used to solve the test instances.

Index Terms— PEAST algorithm, shift generation, workforce optimization, workforce scheduling.

I. WORKFORCE SCHEDULING AND WORKFORCE OPTIMIZATION

Workforce scheduling, also called staff scheduling and labor scheduling, is a difficult and time consuming problem that every company or institution that has employees working on shifts or on irregular working days must solve. Workforce scheduling studies have mainly focused on staff rostering, i.e. assigning employees to shifts and determining working days and rest days. In the recent years, the generation of shifts has gained increasing interest in academic community. Shift generation is the process of determining the shift structure, along with the tasks to be carried out in particular shifts and the competences required for different shifts. Application areas of staff rostering and shift generation include hospitals, retail stores, call centers, cleaning, home care, guarding, manufacturing and delivery of goods.

Shift generation is essential in cases where the workload is not static. On the contrary, in airlines, railways and bus companies and mostly in hospitals the demand for employees is quite straightforward because the timetables are known beforehand and the shifts are already fixed. The most important optimization target is to match the shifts to the workload as accurately as possible. The generation of shifts is based on either the number of employees working at the certain timeslots or the number of tasks that the shifts have to cover.

The generated shifts form an input for the staff rostering, where employees are assigned to the shifts. The length of the planning horizon is usually between two and six weeks. The most important constraints are employees’ competences and preferences as well as the working and resting times, since these are laid down by the collective labor agreements and government regulations. Note that staff rostering also includes the scheduling of days-off and vacations.

The demand-oriented workforce scheduling process starts from four entry points (see Figure 1). First, workload prediction is the phase of determining the workload. This is done based on both known and predicted events. For example, the arrivals of customers can be predicted using models based on queueing theory, simulation and statistics, while known events may be gathered from current sales contracts. The events are transformed into either tasks or staff demand, depending mostly on the duration and spatial diversity of the events. Note that sick leaves and other no-shows should be considered when calculating the staff demand.

Second, the HR master system provides necessary employee data, such as labor contract, work unit and working hours. Third and fourth, the labor regulations and the common practices as well as the competences and preferences of the employees are maintained by the workforce management system itself. These four entry points gather the required information first for the shift generation phase and then for the staff rostering phase.

The process continues with shift generation, which is

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Future staffing requirements must be carefully considered in resource and holiday planning phase. Holidays, training sessions and other short-term absences as well as long-term sick-leaves and forthcoming retirements have major impact to actual staff rostering. A resource analysis should be run on the data to see if there will be any chance of succeeding at matching the workforce with the shifts while adhering to the given constraints. The analysis checks the balance between the shifts and the available employees.

In the practical point of view, the workforce scheduling process relies on both optimization resources and human resources. It links the organization together, optimizing processes and streamlining decision-making. The usefulness and utilization of the optimized shifts and rosters depend more on the good-quality outcome of the preceding phases than the actual optimization result. However, when the input data for the shift generation and for the staff rostering are well validated, significant benefit in financial efficiency and employee satisfaction can be achieved.

Nevertheless, the optimized staff rosters need to be changed. Daily rescheduling deals with ad hoc changes that are necessary due to sick leaves and other no-shows. The workforce management system should recommend suitable substitutes considering the qualifications, employment contract, legal limitations and salaries. The goal is to find the most economical candidates. Finally, the completed working times will be booked and made available for payroll accounting system.

In theory, the best results can be achieved when shift generation and staff rostering are processed and solved at the same time. However, different variations of both problems and even their sub-problems are known to be NP-hard and NP-complete [1]-[5]. Nonetheless, some interesting implementations exist. Jackson et al. [6] presented a very simple randomized greedy algorithm that uses very little computational resources. Lapegue et al. [7] introduced the Shift Design and Personnel Task Scheduling Problem with Equity objective (SDPTSP-E) and built employee timetables by fixing days-off, designing shifts and assigning fixed tasks within these shifts. They minimized the number of tasks left unassigned.

Dowling et al. [8] first created a master roster, a collection of working shifts and off shifts, and then allocated the tasks in their Task Optimiser module. Prot et al. [9] proposed a two-phase approach consisting in first computing a set of interesting shifts, then, each shift is used to build a schedule by assigning tasks to workers, and then iterating between these two phases to improve solutions. They relaxed the constraint that each task has to be assigned. Smet et al. [10] presented the Integrated Task Scheduling and Personnel Rostering Problem, in which the task demands and the shifts are fixed in time. Due to the complexity issues in large-scale practical applications, shift generation and staff rostering are mainly solved separately. Our approach is to first generate the shifts and then roster the staff as described in Section III.


The article is organized as follows. In the next section we introduce different shift generation scenarios and the problems triggered from these scenarios. Section III describes the general task-based shift generation problem. Section IV briefly describes the PEAST algorithm, which is used to solve wide variety of scheduling problems. In Section V we present our first computational results.

II. INTRODUCTION TO SHIFT GENERATION PROBLEMS

Shift generation is the process of transforming the determined workload into shifts. The result includes the optimized shift structure, the tasks to be carried out in particular shifts, the competences required for different shifts and the break times required. For labor intensive organizations, it is crucial to find a good match between the predicted and scheduled workload. The generation of shifts is based on either the number of employees working at the certain timeslots or the number of tasks that the shifts have to cover. We call these problems employee-based and task-based shift generation problems.

Numerous models and algorithms for shift generation problems have been developed. The first major contribution was published by Musliu et al. [12]. They introduced an employee-based problem, in which the workforce requirements for a certain period of time were given, along with constraints about the possible start times and the length of shifts, and an upper limit for the average number of duties per week per employee. They generated solutions that contained shifts (and the number of employees per shift) that minimize the number of shifts, overstaffing, understaffing, and differences in the average number of duties per week.

Di Gaspero et al. [16] proposed an employee-based problem in which the most important issue was to minimize the number of shifts. They dealt with cyclic schedules, i.e. the last planning day of the planning horizon (e.g. one week) coincides with the first planning day of the next cycle, and the requirements are repeated in each cycle. The problem statement also includes a collection of acceptable shift types each of them characterized by the earliest and the latest start times, and a minimum and maximum length of its
shifts.

Bhulai et al. [17] presented a generalized model for multi-skill shift design in call centers. Their method generated a rough match between the predicted workload and labor capacity, taking the stochastic nature of the call arrival process into account. Kyngäls et al. [18] introduced the unlimited shift generation problem in which the most important goal is to minimize understaffing and overstaffing. They define the strict version of the problem such as each timeslot should be exactly covered by the correct number of employees. In [15]-[17], the shifts are limited to a number of types, for which the length and the start time of the shifts have to be within certain ranges. In [18], the lengths and the start times of the shifts are not strictly limited.

In the person-based multitask shift generation problem with breaks presented in [19], employees can have their personal shift length constraints and competences. Even if the goal is to construct a set of shifts and not to assign them to employees, they ensure that the employees’ have the ability to execute the shifts. They do this by choosing a suitable subset of the employees as a preprocessing phase for the shift generation process and creating each shift according to a single employee’s personal (shift length and competence) constraints. The exact procedure can be done separately, but in a real-world case with a realistic planning horizon (usually at least a week) it is often best to schedule days-off first and then use the result as a basis for the staff rostering.

Compared to the employee-based shift generation problem, far fewer models and algorithms have been developed for the task-based shift generation problem in which a number of different tasks must to be carried out. The problem is to create shifts and assign tasks to these shifts so that employees can be assigned to the shifts.

The first major contribution of task-based problem was published by Dowling et al. [8]. They created a master roster, a collection of working shifts and off shifts, and then allocated the tasks in their Task Optimiser module, which is invoked one day before the day-of-operation. They allocated a set of tasks (with required attributes and with known start and end times) to personnel with the requisite skills who are available for work on that day (with known shift start and end times).

Krishnamoorthy and Ernst introduced a group of problems called Personnel Task Scheduling Problems (PTSP) in [20]. Given the staff that are rostered on a particular day, the PTSP is to allocate each individual task, with specified start and end times, to available staff who have skills to perform the task. Later, Krishnamoorthy et al. [21] introduced a special case referred as Shift Minimisation Personnel Task Scheduling Problem (SMPTSP) in which the only cost incurred is due to the number of personnel (shifts) that are used. This variant was motivated by situations where a large pool of casual staff is available and management would like to minimize pool usage. A similar model was earlier presented in [22] where they minimized the number of workers required to perform a machine load plan. The SMPTSP is also similar to the basic interval scheduling problem presented in [23] where the goal is to decide which jobs to process on which machines. Unlike in the interval scheduling problem, in the SMPTSP all tasks need to be assigned and not all employees can process each task.

Lin and Ying [24] developed a three-phase heuristic for the SMPTSP. They obtain an initial solution using a simple but very effective construction heuristic, which is then improved using an iterated greedy heuristic, which in turn is used as an initial upper bound while solving the MIP model of the problem. Lapegue et al. introduced an equity objective to the SMPTSP [25]. The idea is to find a solution where employees have approximately the same amount of work, thus generating more fair schedules. However, they relax the constraint that all tasks need to be assigned. The SMPTSP problem with Equity objective minimizes the number of unassigned tasks and the inequity among workers.

The next section describes more general shift generation problem in which the tasks are not fixed in time. Furthermore, the tasks are not explicitly assigned to employees.

III. THE GENERAL TASK-BASED SHIFT GENERATION PROBLEM

In this section, we present the General Task-based Shift Generation Problem (GTSGP). To the best of our knowledge, the problem was first introduced in [26]. However, numerous models, algorithms and implementations for specific shift generation problems have been developed as presented in Section II. The motivation for the GTSGP derives from the demand-oriented workforce scheduling process presented in Section I. Due to the complexity issues in large-scale practical applications, shift generation and staff rostering are mainly solved separately. In most cases, the first problem consists of choosing a small subset of shifts from a pre-defined set of shift types that is common to all days of the planning horizon and then for each day of the planning horizon, deciding which employees execute which tasks in which shifts. For example, Dowling et al. [8] and Prot et al. [9] first create a set of shifts and then assign the tasks to the shifts. Our approach is the opposite. We first generate the shifts and then roster the staff. This approach is due to customer needs in retail stores, cleaning, home care and guarding.

Given the tasks that should be rostered on a particular day, the GTSGP is to create anonymous shifts and assign tasks to these shifts so that employees can be assigned to the shifts. The targeted tasks must be completed within a given time window. For example, shelving in retail stores is often carried out in the forenoon. It is obvious that we will need far more employees if we fix the starting times of the tasks compared to the dynamic starting times. Some tasks are so-called back-office tasks. In a contact center, for example, answering emails might require a given number of working hours per day dedicated to the activity even though the distribution of those hours within the day does not matter. The back-office work could be preempted as stated in [9]. However, in real-world applications, we should have a freedom in determining the starting times of back-office tasks.

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The GTSGP differs from the SMPTSP in several ways:

1) tasks are not explicitly assigned to employees
2) tasks are not fixed in time
3) tasks may have shift-local precedence constraints
4) transition times between tasks are considered
5) the number of feasible (shift, employee) pairs are maximized.

Transition times between tasks are considered in the crew scheduling problem [27], where a set of crews, a set of locations and a set of tasks is given. For each task, a location is given and for each pair of locations a distance is given. The problem is to assign tasks to crews using a minimum number of crews.

We consider the shift structure separately for each day, so there is no connection between the shifts of different days. Recall, that we roster the staff after the shifts have been generated for each day. This is why we must create as versatile shifts as possible to insure that the rostering of the staff can be completed. We have to ensure that the resulting set of shifts can be carried out by the employees, i.e. each shift can be assigned to an employee s.t. all shifts are assigned to someone and no employee is assigned to multiple shifts.

For each day, the goal is to maximize the number of feasible (shift, employee) pairs. A pair (s, e) is considered feasible if employee e can carry out shift s. Note, that in the practical applications of the GTSGP we have faced so far, the full-time permanent and temporary employees cover 100% of the total workload in the shift generation and rostering phases. This is opposite to the idea behind the SMPTSP, where a large pool of casual staff is available and management would like to minimize pool usage.

The GTSGP covers a one-day planning period of t timeslots. The set of shifts $S$ is to be generated. The number of shifts is usually the same as the number of available employees. In case of understaffing, additional pseudo employees can be used. A set of tasks $T$ is to be assigned to the shifts. Each task $t$ has a duration $d_t$ (in timeslots), a time window $[lb_t, ub_t]$, a task type $D_t$ and a location $l_t$. A task $t$ must not start before $lb_t$ and must not end after $ub_t$. A task type $D_t$ is related to the collection of skills required by the tasks, which is a subset of the skill set $C$. It is easier to manage the required skills for the tasks by first classifying them to task types. Respectively, each employee e from the set of employees $E$ has a collection $K_e$ of skills. In addition, each employee $e$ has a time constraint $[elb_e, eub_e]$ for the total working time and a contiguous availability set $A_e$ of timeslots. An employee $e$ must not work less than $elb_e$ or more than $eub_e$ timeslots in the targeted day. An employee $e$ cannot execute tasks that are assigned to the timeslots not in $A_e$. Furthermore, each employee $e$ has a unique mode of transport $r_e$. The global transition matrix $M$ consists of transitions $m_{ij}$ where $m_{ij}$ indicates the number of timeslots needed using transport mode $i$ to transit from location $j$ to location $k$. For example, one employee can use a car or a bus while the other can use a bicycle. The time from the employee’s home depot to the first task, the transition times between the tasks and the time from the last task back to the employee’s home depot are not counted as working time. Only the transitions between tasks count against employee availability.

In summary, an employee $e$ can be assigned to the shift $s$ only if the following criteria hold:

(C1) He/she possesses all the skills indicated by the task types of the tasks assigned to the shift (skill).
(C2) The total working time of the tasks in the shift is within $[elb_e, eub_e]$ (working time).
(C3) All the timeslots of the tasks in the shift are included in $A_e$ (availability).
(C4) He/she has enough transition time to move between the tasks in the shifts (transition time).

The GTSGP has four basic assumptions:

(B1) Each task will be assigned to a shift.
(B2) Preemption of tasks is not allowed.
(B3) Each task is processed only once without interruption.
(B4) Each employee can execute only one task at a time.

A solution to the GTSGP is feasible, if the following five hard constraints have no violations:

(H1) The tasks in the shift do not overlap in time (overlap).
(H2) Some tasks may have shift-local precedence constraints, that is, a task may not be executed after some other tasks in the same shift (precedence).
(H3) Each shift can be executed (C1-C4 hold) by one or more employees (shift).
(H4) Each shift can be assigned to an employee s.t. all shifts are assigned to someone and no employee is assigned to multiple shifts (combination).

Lunch and other breaks can also be created using the idea given in [19]. To evaluate the hard constraint H4, we have to solve the corresponding assignment problem. Note, that the criterion H4 actually implies H3. Figure 2 shows a solution to an assignment problem with six shifts and six employees. The corresponding assignment problem would have no solution, if employee F could not execute shift 3, even though criterion H3 would still hold.

The GTSGP can now be stated as follows:

1) Maximize the sum of number of feasible (shift, employee) pairs over all pairs.
2) Satisfy the hard constraints H1-H4.

The number of shifts employees are able to execute in the example given in Figure 2 is 13. Note, that in the GTSGP, the shift structure is implicitly generated from the skills, working times, availabilities and transition times of the employees (criteria C1-C4). Lin and Ying [28] state that it would be interesting and useful to take into account employee preferences, such as assignments to a preferred task. In our model the staff preferences are considered in the staff rostering phase (see Figure 1).

The GTSGP can also include the same soft constraints for the employee-based shift generation problem (see [19]), for example the following:

(S1) Shifts of less than \( k_1 \) and over \( k_2 \) timeslots in length must be minimized.
(S2) The average shift length should be as close to \( k_3 \) timeslots as possible.
(S3) Shifts that start between timeslots \( k_4 \) and \( k_5 \) must be minimized.
(S4) Shifts that end between timeslots \( k_6 \) and \( k_7 \) must be minimized.
(S5) Each shift should contain at most \( k_8 \) switches from one task to another.

IV. SOLUTION METHOD

The search space of the GTSGP is enormously larger than that of the SMPTSP. For example, consider an instance with ten shifts and with one hundred tasks each having a duration of ten timeslots and a time window of nineteen timeslots. In the SMPTSP, we have ten possible assignments for each task totaling \( 10^{100} \) solution candidates. In the GTSGP, however, we have \( 10 \times 20 \) possible assignments for each task totaling \( 200^{100} \) solution candidates, i.e. \( 20^{100} \) times more candidates.

The computational requirements even for the large-scale SMPTSPs are so high that exact methods may not produce a feasible solution within a limited computing time. The metaheuristic and matheuristic algorithms developed for the SMPTSP (see the references in Section II) use the idea of maximal cliques to reduce the search space. A clique is a set of overlapping tasks for a worker at a given time. The same idea is not applicable in the GTSGP since the tasks are not fixed in time.

We solve the GTSGP using the PEAST algorithm described in [29]. The algorithm is a population-based metaheuristic. The acronym PEAST stems from the methods used: Population, Ejection, Annealing, Shuffling and Tabu. It has been used in staff rostering [30], employee-based shift generation [19], professional sports league scheduling [31] and school timetabling problems [32]. Furthermore, the algorithm has been used to solve somewhat more academic problems, such as balanced incomplete block design [33], single round robin tournaments with balanced home-away assignments and pre-assignments [33] and constraint minimum break problems [34].

The PEAST algorithm seeks to overcome the three biggest challenges for metaheuristics: a good quality of the generated solutions, the acceptable running time of the algorithm and that it can be used to solve wide variety of problems. These are often contradicting requirements that a metaheuristic attempts to balance. Simple and small neighborhoods decrease the running time, but the quality improvement of an individual iteration of the algorithm is expected to be low, thus requiring larger total number of iterations. On the other hand, in large complex neighborhoods, as in the PEAST, single iterations require significantly more time, but the quality improvement is expected to be much higher requiring less iterations.

A metaheuristic is specified by four core issues: initial solution, search space, neighborhood and cost function. The heart of the PEAST is the local search called GHCM, which is used to explore promising areas in the search space. Another important feature of the algorithm is the use of shuffling operators, which assist in escaping from local optima. Furthermore, simulated annealing and tabu search are used to avoid staying stuck in promising search areas too long. The algorithm uses ADAGEN, the adaptive genetic penalty method, which assigns dynamic weights to the hard constraints based on the constant weights assigned to the soft constraints. For the detailed discussion of the algorithm, we refer to [29] and [35]. The pseudo-code of the algorithm is given in Figure 3.

![Figure 3](image_url)
than that of the previous non-improving move, or if the maximum number of moves is reached. Then, a new sequence of moves is started.

Due to the complexity issues and the very large search space of the GTSGP, we have to consider five calculation key points when solving real-world instances. First, whenever possible, we should reduce the number of tasks by grouping or sequencing smaller tasks into bigger single tasks. Second, we should similarly group skills to larger skill groups. This is not as vital as with the number of tasks. Third, without losing too much important information, the slot size should be as long as possible, i.e. the number of timeslots should be as small as possible.

Fourth, when generating a sequence of moves, we have to calculate the cost function many times during one GHCM operation. Furthermore, we have to calculate the cost function while rollbacking the moves, often down to the starting point. The computational resources are too high to calculate the solution value. Therefore, we should recalculate only those parts of the solution, which are changed due to the single moves of the move sequence. This is very tough to implement, but it is vital for real-world use of the PEAST algorithm.

Finally, to check out the hard constraint H5, we have to solve the assignment problem as described in Section III. The problem was originally solved in $O(n^4)$ time, but it can be solved in $O(n^3)$ time using appropriate data structures [36]. Unfortunately, this is still far too slow since we have to solve the assignment problem in each single move in the move sequence. One possibility would be to use a greedy heuristic, but it does not guarantee that we can generate such shifts that the staff rostering can be completed. Fortunately, implementing the move sequence in such a way that we can apply the ideas presented in [37], we are able to calculate only the changes incurred to the initial assignment problem. In our implementation the calculation of changes requires $O(n^3)$ time.

V. FIRST COMPUTATIONAL RESULTS

In this section we present our first computational results. We first try to solve some of the SMPTSP benchmark instances and then we present one GTSGP benchmark instance. Real-world benchmark instances for SMPTSP do not exist at the moment, but three artificial benchmark instances have been published.

Krishnamoorthy et al. [21] presented a data set of 137 instances for the SMPTSP. The data set is referred to as KEB instances. Smet et al. [38] generated ten more difficult instances than KEB instances, referred to as SWMB instances. Furthermore, Fages and Lapegue [39] generated a new data set of 100 instances, because the KEB and SWMB instances are trivial with regard to finding good quality lower bounds. This data set is referred to as FL instances. A good summary of the instances and an excellent greedy algorithm for the SMPTSP can be found in [40].

It is obvious, that the PEAST algorithm designed for the GTSGP cannot compete with the specifically tailored SMPTSP algorithms described in [9], [21], [24], [25], [38] and [40]. However, as a first test, we decided to select seven instances from the KEB data set. The instances were selected to cover different task sizes and employee sizes and their ratio. In addition, four of the instances are such that the heuristic presented in [21] were not able to solve them to optimality. Table 1 shows the test instances and our first test runs. We were able to solve six of the seven instances.

<table>
<thead>
<tr>
<th>KEB instance id</th>
<th>#Tasks</th>
<th>#Emps</th>
<th>Optimum</th>
<th>Heuristic</th>
<th>PEAST</th>
</tr>
</thead>
<tbody>
<tr>
<td>KEB 1</td>
<td>40</td>
<td>23</td>
<td>20</td>
<td>20</td>
<td>20</td>
</tr>
<tr>
<td>KEB 9</td>
<td>104</td>
<td>49</td>
<td>40</td>
<td>41</td>
<td>40</td>
</tr>
<tr>
<td>KEB 26</td>
<td>203</td>
<td>116</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>KEB 27</td>
<td>204</td>
<td>49</td>
<td>40</td>
<td>40</td>
<td>40</td>
</tr>
<tr>
<td>KEB 39</td>
<td>351</td>
<td>45</td>
<td>40</td>
<td>41</td>
<td>40</td>
</tr>
<tr>
<td>KEB 63</td>
<td>577</td>
<td>97</td>
<td>80</td>
<td>82</td>
<td>80</td>
</tr>
<tr>
<td>KEB 75</td>
<td>665</td>
<td>72</td>
<td>60</td>
<td>71</td>
<td>65</td>
</tr>
</tbody>
</table>

$KEB = KEB$ instance id, $#Tasks = number$ of tasks, $#Emps = number$ of employees, $Optimum = optimum$ value, $Heuristic = the$ value obtained using the heuristic in [21], $PEAST =$ the value obtained using the PEAST algorithm.

Next, we present one GTSGP benchmark instance, which introduces all the features and hard constraints of the problem described in Section III. We have implemented a GTSGP test generator, which we used to generate the test instance. Test instances are generated in a way that at least one solution with no hard constraint violations exists. The instance was created using the following settings:

- Number of task type precedence constraints: 13
- Minimum (max) number of skills in task types: 5 (10)
- Average number of employees fit for a shift: 3
- Average gap of employees’ minimum and maximum working time: 20%
- Average difference of shift durations: 20%
- Percentage of backup-office tasks: 0%
- Percentage of fixed tasks: 50%
- Average task window deviation: 50%
- Probability of a location change between the tasks in the same shift: 50%
- Number of transition timeslots required between the tasks in the same shift: 0, 1 or 2.

Table 2 shows the characteristics of the test instance. The data for the instance is available online [41] (instance #8). We were able to find a solution with no hard constraint violations and with 39 feasible pairs (see Figures 4a and 4b).

<table>
<thead>
<tr>
<th>Timeslots</th>
<th>20</th>
<th>Min (Max) number skills of employees (see C1)</th>
<th>20 (29)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tasks</td>
<td>100</td>
<td>Min (Max) working time limits of employees (see C2)</td>
<td>11-13 (18-20)</td>
</tr>
<tr>
<td>Shifts</td>
<td>20</td>
<td>Min (Max) employee available timeslots (see C3)</td>
<td>13 (20)</td>
</tr>
<tr>
<td>Employees</td>
<td>20</td>
<td>Min (Max) number of employee transition times of length 2 (see C4)</td>
<td>18 (44)</td>
</tr>
<tr>
<td>Task types</td>
<td>10</td>
<td>Min (Max) number of skills related to task types</td>
<td>5 (10)</td>
</tr>
<tr>
<td>Precedences</td>
<td>13</td>
<td>Min (Max) time window length of tasks</td>
<td>1 (17)</td>
</tr>
<tr>
<td>Skills</td>
<td>30</td>
<td>Min (Max) duration of tasks</td>
<td>1 (16)</td>
</tr>
<tr>
<td>Locations</td>
<td>11</td>
<td>-----------------------------------------------</td>
<td>--------</td>
</tr>
</tbody>
</table>

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Fig. 4a. A solution with no hard constraint violations and with 39 feasible pairs. Numbers in parentheses denote the starting timeslot of task.

Fig. 4b. The 39 feasible pairs of the solution and one possible solution (denoted by *) to the corresponding assignment problem.

VI. CONCLUSION

We presented the General Task-based Shift Generation Problem (GTSGP). To the best of our knowledge, the problem has not been studied in the literature. We briefly described the PEAST algorithm, which was used to solve the presented test instances. We first solved seven SMPTSP instances, which are very special cases of GTSGP. Then we solved one GTSGP instance, which introduced all the features and hard constraints of the GTSGP. The computational results were encouraging.

The PEAST algorithm for staff rostering has been integrated into Visma Numeron WFM, a market-leading workforce management software in Finland. This research has contributed to better systems for our industry partners. We are currently working on integrating the shift generation and the GTSGP to the WFM software.

Our current direction is to provide the mathematical formulation of the GTSGP, apply the PEAST algorithm to all the KEB, SWMP and FL instances, and to use the GTSGP test generator to create a large set of benchmark instances for the GTSGP.

REFERENCES


