2D-DOAE Using Temporal-Spatial Subspace Technique with Doppler Correction

Youssef Fayad, Member, IAENG, Caiyun Wang, and Qunsheng Cao

Abstract—In this paper a modified ESPRIT algorithm, which bases on time subspace (T-ESPRIT) and spatial subspace of estimate 2D-DOA (azimuth and elevation) of a radiated source, that can increase the estimation accuracy with low computational load is introduced. Using the algorithm, the planar array is divided into a multiple uniform sub-planar arrays with the common reference point, and the T-ESPRIT method is applied for each sub-array. Secondly, Doppler frequency shift $f_d$ resulted from the target movement is estimated using displacement invariance technique (DIT). Then, in order to increase the estimation accuracy, the estimated Doppler frequency is used to correct the DOAE values according to target movement. Moreover, the proposed algorithm is combined the refined T-ESPRIT method with time differential of arrival (TDOA) technique to calculate an optimum DOA. It is found that the estimated results are better than the traditional ESPRIT methods leading to the estimator performance enhancement.

Index Terms— T-ESPRIT, Doppler frequency, TDOA, DOAE, Subspace.

I. INTRODUCTION

Estimating of direction-of-arrival (DOAE) is the creator of the tracking gate dimensions (the azimuth and the elevation) in the tracking while scan radars (TWS), a high DOAE errors means a high angle glint error which affects the accuracy of the tracking radar system. The DOAE of the multiple narrowband signals is an important process in array signal processing including sonar, radar, astronomy and mobile communications. The ESPRIT and its extracts have been widely studied in one-dimensional (1D) DOAE for uniform linear array (ULA), non-uniform linear array (NULA) [1]-[11], and also extended to two-dimensional (2D) DOAE [12]-[19]. All of these ESPRIT methods have been developed to upgrade the accuracy of DOAE with low calculation costs.

This paper presents a new modified algorithm based on time subspace (T-ESPRIT) [1], [2] and spatial subspace to reduce the computational costs of the 2D-DOAE (azimuth and elevation) of a radiated source which has been detected by a uniform planar array antenna with high accuracy. First, the spatial subspace is realized by arranging the main planar array as a multiple uniform sub-planar arrays related to the common reference point to get a unified phase shifts measurement point for all sub-arrays. The T-ESPRIT algorithm is applied on each sub-array separately, and in the same time with the others to realize time and space parallel processing, so that it reduces the non-linearity effect of model and decreases the computational time. Then, the target movement is detected via estimate its Doppler frequency by comparing the displacement invariances of transmitter and receiver arrays, which enables measurement of the sensor array displacement invariance fluctuation resulted from wavelength change induced by the target movement. It is worth mentioning that the subspace approach is also employed into DIT method to reduce the computations time. Moreover, the effect of Doppler frequency on the T-ESPRIT method is explained in order to refine the DOAE. Finally, the TDOA technique is applied and combined the multiple sub-arrays to calculate the optimum DOAE value at the reference antenna, which obtains to enhance the estimation accuracy and reduce computational load [20], [21].

The paper is organized as follows. In Section II, the Doppler correction for 2D T-ESPRIT technique and its combination with TDOA are introduced. In Section III, the simulation results are presented, and Section IV is conclusions.

II. PROPOSED ALGORITHM

A. The Measurement Model

In this model, the radiation propagates in straight lines due to isotropic and non-dispersive transmission medium assumption. Also, it is assumed that the sources as a far-field away the array. Consequently, the radiation impinging on the array is a summation of the plane waves. The signals are assumed to be narrow-band processes, and they can be considered to be sample functions of a stationary stochastic process or deterministic functions of time. Considering there are $K$ narrow-band signals, and the center frequency $f$ is assumed to have same $\omega_0 = 2\pi f$, the for the $k$th signal can be written as

$$s_k(t) = E_k e^{j(\omega_0 t + \Psi_k)}, k = 1, 2, ..., K$$  

(1)

where $s_k(t)$ is the signal of the $k$th emitting source at time instant $t$, $\Psi_k$ the carrier phase angles are assumed to be random variables, the each uniformly distributed on $[0,2\pi]$ and all statistically independent of each other.

Fig. 1 introduces a planar array oriented in $xoy$ plane and arranged as sub-planar arrays and indexed with $N, G$ along $y$ and $x$ directions respectively. Fig. 2 is shown a $(n, g)$ sub-planar array where $n=1, ..., N$, $g=1, ..., G$, has elements indexed $L$, $l$ along $y$ and $x$ directions respectively.

For any pairs $(i, l)$, its coordinates with respect to the reference point (R.P) along $y$ and $x$ directions respectively are $(y_{i,l}, x_{i,l})$, where $i=1, ..., I$, $l=1, ..., L$.
The space phase factors along $x$ and $y$ directions are expressed as

\[ (2) \]

\[ (3) \]

where $(\nabla_{n,g}^{k}, \varphi_{k}^{n,g})$ denote the $k$th source estimated elevation angle and azimuth angle respectively with respect to $(n, g)$ sub-array, and $\Delta x$ and $\Delta y$ are reference displacements between neighbor elements along $x$ and $y$ directions within any $(n, g)$ sub-array also $\Delta x$ and $\Delta y$ are reference displacements between neighbor sub-arrays along $x$ and $y$ directions respectively, and $\lambda$ is the wavelength of the signal. The receiving model can be expressed as:

\[ (6) \]

where the matrices, $[S(t)], [A]$ and $[W(t)]$ are the receiving signal, transform factor for each sub-array, and AWGN (Additive White Gaussian Noise), respectively. They are given in subspace as follows

\[ (7) \]

\[ (8) \]

where $\bigotimes$ denotes the Kronker product. So, for any $(n, g)$ sub-array

\[ (9) \]

where $p_{1}(\theta_{k}^{n,g}, \varphi_{k}^{n,g})$, and $q_{1}(\theta_{k}^{n,g}, \varphi_{k}^{n,g})$, are symbolized as $p_{k}^{n}, q_{k}^{n}$. And:

\[ (10) \]

\[ (11) \]

\[ (12) \]

The auxiliary polarization angle is defined as $\gamma = [0, \pi/2]$, and the polarization phase difference is given as $\eta \in [-\pi, \pi]$. We omit $(n, g)$ for simplicity. The whole data is divided into $M$ snapshots at each time $t_s$ second with sampling frequency $f_s$ according to Nyquist law. Then it picks up enough data $r$ enclosed by each snapshot $m$ with time period as short as possible. So, from (6) each receiving signal measurement value through $m$th subspace is given as

\[ (13) \]

The index $m$ runs as $m=1, 2, \ldots, M$ snapshots. Therefore, the whole space-time steering data matrix can be expressed as

\[ (14) \]

\[ (15) \]

Then

\[ (16) \]

For T-ESPRIT scheme the ESPRIT algorithm is used in an appropriate picked data represented in (14) for each $(m)$ subspace given in (16). It is noted that (15) presents a parallel calculation for each subspace for the same sampling accuracy, however, the calculations load reduction and consequently saving time are achieved.

The ESPRIT algorithm is based on a covariance formulation that is

\[ (17) \]

\[ (18) \]

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where $\hat{R}_{zz}$ is the correlation matrix of the sub-array output signal matrix, $\hat{R}_{xx}$ is the autocorrelation matrix of the signal. The subscript (*) denotes the complex conjugate transpose. The correlation matrix of $\hat{R}_{zz}$ can be done for eigenvalue decomposition as follow

$$\hat{R}_{zz} \equiv \hat{E}_S\hat{\Lambda}_S\hat{E}_S^* + \sigma^2 \hat{E}_N\hat{E}_N^*$$  \hspace{1cm} (19)

where the eigenvalues are ordered $\lambda_1 > \lambda_2 > \cdots > \lambda_K > \lambda_{K+1} = \cdots = \lambda_{2(L \times L)} = \sigma^2$.

The eigenvectors $\hat{E}_S = [\hat{e}_1, \hat{e}_2, \ldots, \hat{e}_K]$ for larger $K$ eigenvalues spans the signal subspace, the rest $2I(L-1)$ smaller eigenvalues $\hat{E}_N = [\hat{e}_{K+1}, \cdots, \hat{e}_{2(L \times L)}]$ spans the noise subspace which is orthogonal to the signal subspace. Therefore, there exists a unique nonsingular matrix $Q$, such that

$$\hat{E}_S = [A]Q = [u_1^T \otimes p_i(\theta_h,\varphi_k) \otimes q_i(\theta_h,\varphi_k)]Q$$  \hspace{1cm} (20)

In (13) let $A_{p1}$ and $A_{p2}$ be the first and the last $2L \times (L-1)$ rows of $A$ respectively, they differ by the factor $\Delta p_k = e^{j2\pi \Delta \lambda_x \sin \theta_x \cos \varphi_k}$ along the $x$ direction. So $A_{p2} = A_{p1}\hat{q}_p$, where $\hat{q}_p$ is the diagonal matrix with diagonal elements $\Delta q_p$. Consequently, $\hat{E}_{p1}$ and $\hat{E}_{p2}$ will be the first and the last $2L \times (L-1)$ sub-matrices formed from $\hat{E}_S$. Then the diagonal elements $p_k$ of $\hat{q}_p$ are the eigenvalues of the unique matrix $\Psi_p = Q^{-1}\hat{E}_{p}Q$, that satisfies

$$\hat{E}_{p2} = \hat{E}_{p1}\Psi_p$$  \hspace{1cm} (21)

Similarly, the two $2I \times (L-1)$ sub-matrices $A_{q1}$ and $A_{q2}$ consist of the rows of $A$ numbered $2I \times (L-1) + l$ and $2I \times (L-1) + l + 2$ respectively, differ by the space factors $\Delta q_k = e^{j2\pi \Delta \lambda_y \sin \theta_y \cos \varphi_k}$ along the $y$ direction, $l=1,\ldots,2(L-1)$. Then $A_{q2} = A_{q1}\hat{q}_q$ where $\hat{q}_q$ is the diagonal matrix with diagonal elements $\Delta q_q$. Consequently, $\hat{E}_q$ forms the $2I \times (L-1)$ two sub-matrices $\hat{E}_{q1}$ and $\hat{E}_{q2}$. Then the diagonal elements $\Delta q_q$ of $\hat{q}_q$ are the eigenvalues of the unique matrix $\Psi_q = Q^{-1}\hat{E}_{q}Q$, that satisfies

$$\hat{E}_{q2} = \hat{E}_{q1}\Psi_q$$  \hspace{1cm} (22)

Therefore, the arrival angles $\theta_h,\varphi_k$ for each sub-array can be calculated as

$$\theta_h = \sin^{-1}\left\{\left(\frac{\lambda}{2\pi}\right)^2 + \left(\frac{\lambda c}{2\pi \Delta \lambda_x \sin \theta_x \cos \varphi_k}\right)^2\right\}^{1/2}$$  \hspace{1cm} (23)

$$\varphi_k = \tan^{-1}\left[\frac{\Delta \lambda_y \arg(q_k)}{\Delta \lambda_x \arg(p_k)}\right]$$  \hspace{1cm} (24)

B. Doppler Correction

The moving target echo signal is shifted by the Doppler frequency. The more accurate T-ESPRIT algorithm should consider the effect of the Doppler frequency shift due to the target movement. So,

$$\arg(\Delta p_k) = \frac{2\pi}{\lambda_x} \Delta \lambda_x \sin \theta_x \cos \varphi_k$$  \hspace{1cm} (25)

$$\arg(\Delta q_k) = \frac{2\pi}{\lambda_y} \Delta \lambda_y \sin \theta_y \sin \varphi_k$$  \hspace{1cm} (26)

where $\lambda_x$ and $\lambda_y$ are the wavelength components of the received wave into antenna plane and differ from the transmitted wavelength because of the Doppler frequency $f_d$ caused by the target moving velocity $\vec{v}_t$ [22], [23], [24]. As shown in Fig. 3, it is obvious that the wavelength $\lambda_x$ and $\lambda_y$ have expressions caused by the velocity components $v_x$ and $v_y$,

$$\lambda_x = \frac{\lambda(c+v_x)}{c}$$  \hspace{1cm} (27)

$$\lambda_y = \frac{\lambda(c+v_y)}{c}$$  \hspace{1cm} (28)

Substituting into (25), (26), then

$$\arg(\Delta p_k) = \frac{2\pi c}{\lambda(c+v_x)} \Delta \lambda_x \sin \theta_x \cos \varphi_k$$  \hspace{1cm} (29)

$$\arg(\Delta q_k) = \frac{2\pi c}{\lambda(c+v_y)} \Delta \lambda_y \sin \theta_y \sin \varphi_k$$  \hspace{1cm} (30)

where $v_x = |\vec{v}_s| \cos \alpha \sin \theta_x \cos \varphi_k$  \hspace{1cm} (31)

$v_y = |\vec{v}_s| \cos \alpha \sin \theta_y \sin \varphi_k$  \hspace{1cm} (32)

And

$$|\vec{v}_s| = \frac{c f_d}{2 f \cos \alpha}$$  \hspace{1cm} (33)

We define $\alpha$ as the angle between the direction of propagation and the target velocity vector $\vec{v}_s$, the value of $\alpha$ changes $f_d$ sign indicating the target direction toward or away from the antenna position. From (29)-(32) the arrival angles $(\theta_h,\varphi_k)$ can be fine estimated from $(\arg(p_k), \arg(q_k))$ as follows

$$\theta_h = \sin^{-1}\left\{\left(\frac{c \arg(\Delta p_k)}{(2\pi c \Delta \lambda_x / \lambda) - \arg(\Delta p_k)\|\vec{v}_s\| \cos \alpha}\right)^2 + \left(\frac{c \arg(\Delta q_k)}{(2\pi c \Delta \lambda_y / \lambda) - \arg(\Delta q_k)\|\vec{v}_s\| \cos \alpha}\right)^2\right\}^{1/2}$$  \hspace{1cm} (34)

$$\varphi_k = \tan^{-1}\left[\frac{\Delta \lambda_y \arg(q_k)}{\Delta \lambda_x \arg(p_k)\|\vec{v}_s\| \cos \alpha}\right]$$  \hspace{1cm} (35)

Fig. 3. Target linear velocity components into antenna plane
C. Doppler frequency estimation

In section B the effect of Doppler frequency on the moving target DOAE is modeled and incorporated into ESPRIT algorithm in order to increase the estimation accuracy. This Doppler frequency should be estimated with maintaining the low computational costs which is the important aim of this work. So, to realize this aim the T-ESPRIT technique which had been explained into (13)-(16), will be applied within Displacement Invariance Technique (DIT) to form T-DIT method. In T-DIT the wavelength change is measured via comparing the displacement invariance ratio \( \left( \frac{\Delta \lambda}{\lambda} \right) \) of the received signal with the displacement invariance ratio \( \left( \frac{\Delta \lambda}{\lambda} \right) \) of a signal generated from a transmitted signal sample and its phase. For the transmitted signal, where no Doppler effect, the departure space phase factors for each subspace are calculated as,

\[
\arg g_d (\Delta p_k) = \frac{2\pi \lambda}{\lambda} \sin \theta_k \cos \varphi_k \\
\arg g_d (\Delta q_k) = \frac{2\pi \lambda}{\lambda} \sin \theta_k \sin \varphi_k
\]

where departure and arrival angles are almost equal for the co-located planar array. From (29)-(35), the Doppler shift for each target \( f^k \) can be estimated as follows,

Substitute (33) into (31), (32) then into (29), (30),

\[
ar g_d (\Delta p_k) = \frac{2\pi \lambda}{\lambda} \cdot \sin \theta_k \cos \varphi_k \cdot \frac{2f}{2f + f^k \sin \theta_k \cos \varphi_k}
\]

Substitute (36)-(37) into (38), (39) respectively,

\[
\frac{\arg g_d (\Delta p_k)}{\arg g_d (\Delta q_k)} = \frac{2f + f^k \sin \theta_k \cos \varphi_k}{2f}
\]

Thus,

\[
f^k = \left( \frac{2f}{\sin \theta_k} \right) \cdot \left[ \left( \frac{\arg g_d (\Delta p_k)}{\arg g_d (\Delta q_k)} \right)^2 - 1 \right]^{1/2}
\]

The variable \( \theta_k \) is the coarse estimated value of the elevation angle stated from (23). From Figure.3 it is clear that the target direction estimation depends on \( v_y \) moving direction and \( \theta_k \), their values are listed in Table I.

<table>
<thead>
<tr>
<th>TABLE I</th>
<th>Target Directional Judgment</th>
</tr>
</thead>
<tbody>
<tr>
<td>\sin(\theta_k)</td>
<td>v_y</td>
</tr>
<tr>
<td>+ ve</td>
<td>+ ve</td>
</tr>
<tr>
<td>+ ve</td>
<td>- ve</td>
</tr>
<tr>
<td>- ve</td>
<td>- ve</td>
</tr>
<tr>
<td>- ve</td>
<td>+ ve</td>
</tr>
</tbody>
</table>

It is clear from Figure.4 that our main purpose is to determine \( v_y \) sign (the target direction). Substituted (37) into (30), then it has follow,

\[
v_y = c \cdot \left( \frac{\arg g_d (\Delta p_k)}{\arg g_d (\Delta q_k)} - 1 \right)
\]

So,

\[
\begin{align*}
\begin{cases}
\arg g_d (\Delta q_k) < \arg g_d (\Delta q_k) \quad \text{if } v_y = +ve \\
\arg g_d (\Delta q_k) > \arg g_d (\Delta q_k) \quad \text{if } v_y = -ve \\
\arg g_d (\Delta q_k) = \arg g_d (\Delta q_k) \quad \text{if } v_y = 0
\end{cases}
\end{align*}
\]

and \( \lambda_x = \lambda_y = \lambda \) for stationary target.

D. Optimal DOAE Calculation

For sub-Planar pair shown in Fig. 5, the TDOA \( (\delta^{ng}) \) for the \( k \)th received signal is calculated as follow [25]

\[
\delta^{ng} = \frac{H}{c} \sin \theta^{ng}
\]

where \( c \) is the wave velocity \((3\times10^8 \text{ m/sec})\) and \( H \) is the distance between any \((n, g)\) sub-array groups as shown in Fig. 5. For the sub-planar groups shown in Fig. 6, the TDOA between group \((1, 1)\) and group \((N, G)\) for the \( k \)th source is denoted by \( \delta^{1G} \), and the TDOA between group \((N, 1)\) and group \((1, G)\) for the \( k \)th source is denoted by \( \delta^{N1} \).

So, from (45)

\[
\delta^{1G} = \frac{H}{c} \sin \theta^{1G}
\]

\[
\delta^{N1} = \frac{H}{c} \sin \theta^{N1}
\]

And

\[
H = \sqrt{(H_x)^2 + (H_y)^2}
\]

where \( H_x, H_y \) are the distance between the first and last sub-array arranged along x and y directions respectively.
And
\[ H_x = x_c^{g=G} - x_c^{g=1} \]  \hspace{1cm} (49)
\[ H_y = y_c^{n=N} - y_c^{n=1} \]  \hspace{1cm} (50)

From (3), and (5)
\[ x_c^g = \left( \frac{(l-1) \cdot \Delta x}{2} \right) + \left( (g-1) \cdot l \cdot \Delta x \right) \]  \hspace{1cm} (51)
\[ y_c^n = \left( \frac{(l-1) \cdot \Delta y}{2} \right) + \left( (n-1) \cdot l \cdot \Delta y \right) \]  \hspace{1cm} (52)

And
\[ \hat{\theta}^{1G}_k = \frac{\hat{\phi}^{1G}_k + \hat{\phi}^{N,G}_k}{2} \]  \hspace{1cm} (53)
\[ \hat{\theta}^{N1}_k = \frac{\hat{\phi}^{N1}_k + \hat{\phi}^{1,G}_k}{2} \]  \hspace{1cm} (54)

Where the value of \( \theta_k \) for any \( (n, g) \) sub-array group was estimated as in (34). Substitute (48-54) into (46), (47) the \( k^{th} \) received signal TDOA \( \tau_k^{(g)} \) are obtained. So, as shown in Fig.6 the optimal DOAE values \( (\hat{\theta}_k, \hat{\phi}_k) \) are measured at the center of the sub-array groups which is located in the cross point of the straight lines pass through group \( (1, 1) \) and group \( (N, G) \) and through group \( (N, 1) \) and group \( (1, G) \). Thus, \( (\hat{\theta}_k, \hat{\phi}_k) \) values can be represented in terms of \( (\hat{\theta}^{1G}_k, \hat{\theta}^{N1}_k) \) as follow [25], [26]

\[ \sin \hat{\theta}^{1G}_k = \sin \hat{\theta}_k \sin \hat{\phi}_k = \frac{\delta^{1G}_k}{H} \]  \hspace{1cm} (55)
\[ \sin \hat{\theta}^{N1}_k = \sin \hat{\theta}_k \cos \hat{\phi}_k = \frac{\delta^{N1}_k}{H} \]  \hspace{1cm} (56)

From (55), (56) the optimal DOAE values are
\[ \hat{\phi}_k = \tan^{-1} \left( \frac{\delta^{1G}_k}{\delta^{N1}_k} \right) \]  \hspace{1cm} (57)
\[ \hat{\theta}_k = \sin^{-1} \left( \frac{\delta^{1G}_k}{H} \right) \]  \hspace{1cm} (58)

III. \hspace{0.5cm} SIMULATION RESULTS

Considering the 2D-DOAE process with the AWGN, the parameters are given \( f_s = 25 \) MHz. Assuming total 25 temporal snapshots, pickup enclosed data \( r = 20 \) times, and 200 independent Monte Carlo simulations. In order to validate the proposed method, it has been used in the planar case with number of elements, such as \( (I, L) = (3, 3), (N, G) = (2, 2) \) with displacement values \( \text{\( \Delta x = \Delta y = \lambda/2 \)} \), with initial values of \( \theta = 45^\circ \) and \( \phi = 60^\circ \). It is found that the computational load has been decreased as a result of reducing the measurement matrix dimension to \( [2L \times r] \) instead of \( [2(IG)(LN) \times Mr] \). Table II represents the computation time and complexity of the proposed method in term of number of flip-flops. It is obvious that the computational load has been reduced as a result of employing time subspace and spatial subspace to enable a simultaneous processing for \( M \) subspaces with each has \( r \) snapshots for sub-array with \( (I, L) \) elements instead of processing for one space has a large number of snapshots \( d, (d = Mr) \) snapshots for array with \( (IG, LN) \) elements.

\[ \text{TABLE II} \]
\[ \text{COMPUTATION TIME AND COMPLEXITY COMPARISON} \]

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Computational time (msec)</th>
<th>Conventional ESPRIT</th>
<th>Proposed algorithm</th>
</tr>
</thead>
<tbody>
<tr>
<td>TimeSnap</td>
<td>17.7</td>
<td>1.14</td>
<td></td>
</tr>
<tr>
<td>Complexity</td>
<td>( O((4d(IGLN))^2 + 8(IGLN)^3) )</td>
<td>( O((M+4r(IL))^2 + 8(IL)^3) )</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 7 is plotted the RMSEs of the proposed algorithm (T-ESPRIT with spatial subspace) by dividing the planar array into two sub-planar arrays with \( (I, L) = (3, 3), (N, G) = (2, 2) \). Results shown in Fig. 7 indicate that the proposed algorithm errors are getting closer to the CRB as a result of applying subspace concept with Doppler correction.

Additionally, in order to introduce the improvement in the computation time compared to estimate Doppler frequency via using the FFT method, Table. III represents a comparison between the proposed method computation time and the different FFT methods mentioned in [27].

\[ \text{TABLE III} \]
\[ \text{COMPARISON OF THE REQUIRED COMPUTATION TIME} \]

<table>
<thead>
<tr>
<th>Algorithms</th>
<th>Computation time (Sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Direct calculation</td>
<td>80.3702</td>
</tr>
<tr>
<td>FFT method</td>
<td>1.5112</td>
</tr>
<tr>
<td>ZFFT method</td>
<td>0.1604</td>
</tr>
<tr>
<td>PWZFFT method</td>
<td>0.0835</td>
</tr>
<tr>
<td>Proposed T-DIT method</td>
<td>0.00926</td>
</tr>
</tbody>
</table>

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Results in Table III show that the computation time is reduced to 11.09% compared to the best computation time which has been realized via using PWZFFT method [27]. This improvement has been realized because of using the temporal subspaces concept which enables parallel processing. The accuracy improvement of the 2D-DOAE using proposed algorithm has been verified by comparing the resulted RMSEs with the RMSEs of 2D-Beamspace ESPRIT and the ESPRIT-Like algorithms used in [15], [17] respectively.

A comparison results displayed in Fig. 8 show that the proposed algorithm has a better performance, especially at a low SNR. This upgrade has been realized due to the increase of DOAE accuracy when combining the T-ESPRIT with spatial subspace algorithm applying the subspace approach which decreases the errors caused by the model non-linearity effect and increases the resolution of phase difference measurement. Additionally, this improvement is due to Doppler correction which reduces the DOAE uncertainty associated with effect of the target movement.

From Table II, it has been found that the proposed algorithm requires $O(M+4r(IL)^2+8(IL)^2)$) flops [28], while the conventional ESPRIT algorithm needs $O(4d(IL)^2+8(GLN)^2)$ flops. The proposed ESPRIT algorithm requires about 6% of the computational time compared with that of the classical ESPRIT algorithm.

Clearly we can figure out that the process of combining between the refined T-ESPRIT algorithm and the spatial subspace algorithm achieved success into increasing the DOAE accuracy with low computational load. Simply, the developed ESPRIT method improves the estimator performance.

IV. CONCLUSIONS

In this paper, a new ESPRIT method is developed based on the concept of subspace. Firstly, T-ESPRIT method algorithm is used to estimate DOA for each sub-array realizing time subspace concept. Secondly, T-ESPRIT DOA estimated value is corrected according to Doppler frequency resulted from target movement which is estimated using T-DIT method. Finally, the modified T-ESPRIT method is combined with TDOA algorithm to compute the optimal DOAE value which was estimated with different sub-arrays to realize spatial subspace concept. It has been found that the estimation accuracy has been increased with low computational load; also the computational time has been reduced about 88% for Doppler estimation and 94% for DOAE, which consequently enhance the estimator performance.

REFERENCES

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