PCA Based Human Face Recognition with Improved Methods for Distorted Images due to Illumination and Color Background

Bruce Poon, M. Ashraful Amin, and Hong Yan

Abstract—Various illumination invariant techniques are being examined in order to identify the one which works well with principle component analysis for human face recognition. Experimental results show that by applying the technique called Gradientfaces at the pre-processing stage which computes the orientation of the image gradients in each pixel of the face images and uses the computed face representation as an illumination invariant version of the input image, it can greatly improve the recognition rates. From a low recognition rate of 0.25% up to 60.75% testing on the Asian face database which has images with various illumination and from a recognition rate of 38% up to 99.5% testing on the Faces94 face database which has color images with slightly darker faces and green background.

Index Terms—Face recognition, principle component analysis (PCA), gradientfaces, illumination insensitive measure.

I. INTRODUCTION

In our previous research works [1, 2, 3], we had identified that illumination is one of the main problems for human face recognition. A source of light can affect facial features. Some of them may appear to diminish in certain cases. In the past, a lot of works had been done to solve that problem.

II. RELATED WORKS

Jobson et al. [4] proposed the single scale retinex (SSR) algorithm. This photometric normalization techniques is based on the so-called retinex theory [5]. The multi scale retinex (MSR) algorithm which is an extension of the single scale retinex algorithm again proposed by Jobson et al. [6]. Park et al. [7] proposed the adaptive single scale retinex (ASR) algorithm which was one of the newest additions to the retinex techniques.

Homomorphic filtering (HOMO) is a well known normalization technique where the input image is first transformed into the logarithm and then into the frequency domain. Here, the high frequency components are emphasized and the low-frequency components are reduced. In the final step, the image is transformed back into the spatial domain by applying the inverse Fourier transform and taking the exponential of the result. A more detailed description of the technique can be found in [8]. Wang et al. [9] introduced the single scale self quotient image (SSQ) to the field of face recognition. This technique exhibits similarities to the single scale retinex technique. Unlike SSR technique, it uses an anisotropic filter for the smoothing operation. Like the SSQ technique, the multi scale self quotient image (MSQ) was also introduced to the field of face recognition by Wang et al. [9]. The technique exhibits similarities to the multi scale retinex technique. Unlike the MSR technique, it uses an anisotropic filter for the smoothing operation.

Chen et al. [10] proposed the discrete cosine transform (DCT) based normalization technique. This technique sets a number of DCT coefficients corresponding to low-frequencies to zero and hence tries to achieve illumination invariance. Du & Ward [11] proposed the wavelet based (WA) normalization technique. This technique applies the discrete wavelet transform to an image and then processes the obtained sub-bands. It emphasizes the matrices of detailed coefficient and applies histogram equalization to the approximate coefficients of the transform. After the manipulation of the individual sub-band, the normalized image is reconstructed using the inverse wavelet transform. Zhang et al. [12] proposed the wavelet denoising (WD) based normalization technique. This technique applies wavelet denoising to an image to obtain an estimate of the luminance and consequently to compute the reflectance.

Gross and Brajovic [13] proposed the isotropic diffusion (IS) based normalization technique which uses isotropic smoothing of the image to estimate the luminance function. It represents a simpler variant of the anisotropic diffusion based normalization technique. A more detailed description of the technique can be found in [8]. The anisotropic diffusion (AS) based normalization technique which uses anisotropic smoothing of the image to estimate the luminance function was again introduced to the field of face recognition by Gross and Brajovic [13]. The modified anisotropic diffusion (MAS) based normalization technique represents a modified version of the anisotropic diffusion based normalization technique was again proposed by Gross and Brajovic [13]. Two modifications were introduced into the technique when compared to the original approach:

Bruce Poon is with the School of Electrical & Information Engineering, University of Sydney, NSW 2006, Australia (e-mail: bruce.poon@ieee.org).
M. Ashraful Amin is with the Computer Vision & Cybernetics Research Group, SECS, Independent University Bangladesh, Bashundhara, Dhaka 1229, Bangladesh. (e-mail: aminmdashraful@iub.edu.bd).
Hong Yan is with the Department of Electronic Engineering, City University of Hong Kong, Hong Kong, China (e-mail:h.yan@cityu.edu.hk).

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the estimate of the local contrast was made more robust by introducing an additional $\tan$ function. This has the effect of saturating the extreme values that are introduced to the contrast estimate due pixel intensities near 0 in the original face images.

(ii) a robust post processing procedure [14] was applied in the final stage of the technique.

Freeman and Adelson [15] proposed the steerable filter (SF) based normalization technique which uses steerable filters for removing illumination induced appearance variations from the facial images. Struc and Pavesic [16] proposed the non-local means (NLM) based normalization technique which uses the non-local means denoising algorithm to compute the luminance function and consequently to estimate the reflectance. The adaptive non-local means (ANL) was again proposed by Struc and Pavesic [16] which uses the adaptive non-local means denoising algorithm to compute the luminance function and consequently to estimate the reflectance. Here, the adaptiveness of the smoothing is controlled by the images local contrast.

Zhang et al. [17] proposed the gradientfaces (GRF) based normalization technique which computes the orientation of the image gradients in each pixel of the face images and uses the computed face representation as an illumination invariant version of the input image. Wang et al. [18] proposed the single scale Weberfaces (WEB) normalization technique which computes the relative gradient in the form of a modified Weber contrast and uses the computed face representation as an illumination invariant version of the input image. The multi scale Weberfaces (MSW) is a straightforward extension of the single scale Weberfaces approach also proposed by Wang et al. [18]. The function computes the relative gradient in the form of a modified Weber contrast for different neighborhood sizes and uses a linear combination of the computed face representations as an illumination invariant version of the input image.

Xie et al [19] proposed the large and small-scale features (LSSF) normalization technique which normalizes the input image by first computing the reflectance and luminance functions of the image and then further processing both computed functions using a second round of normalization. SSR technique is being used in both steps, but does not implement the non-point light technique which requires training data that would limit the applicability of the technique to frontal images.

Tan and Triggs [14] proposed the Tan and Triggs (TT) normalization technique which normalizes the input image through the use of a processing chain that first applies gamma correction to the input image, then subjects the corrected image to difference of Gaussians (DoG) filtering and finally employs a robust post-processor to produce the final result. The DoG filtering-based normalization technique relies on the difference of Gaussians filter to produce the normalized image. Basically it applies a bandpass filter to the input image and produces a normalized version of it.

Sharif et al. [20] proposed an illumination normalization technique which works at the pre-processing stage where the face image is first divided into equal sub-regions. Each sub-region is then processed separately for illumination normalization. The segments are then joined back follow further processing like noise removal and contrast enhancement.

Yip and Sinha [21] had suggested that color cues did play a role in face recognition and their contribution became evident when shape cues were degraded. Under such conditions, the recognition performance with color images was significantly better than that with gray-scale images.

Singh et al. [22] had found that using principle component analysis for face recognition and Skin Color Model for face detection achieved an overall success rate of 95%.

The INface toolbox provided by Struc [23], [24] has a collection of various illumination normalization techniques. After evaluation and testing, we have identified that gradientfaces (GRF) based normalization technique works best with principle component analysis for human face recognition especially for those images affected by illumination.

This paper is an extension of our earlier work [25]. In addition to the effect of illumination, we also present the improved results on human face recognition utilizing gradientfaces (GRF) based normalization technique in the pre-processing stage for color images. Details of works and experiments are being described in the following sections.

### III. PROPOSED TECHNIQUE

#### A. System Structure

To handle the illumination normalization problem for facial recognition, Gradientfaces based normalization technique [17] is added in the pre-processing stage in order to compute the orientation of the image gradients in each pixel of the face images and uses the computed face representation as an illumination invariant version of the input image. A typical facial recognition system with four major generic components and an additional illumination normalization module is shown in Figure 1.

![Fig. 1 A generic facial recognition system with illumination normalization](image-url)

#### B. Facial Image Acquisition

In our previous research work [3], we had identified the problem with illumination on face images from the Asian Face Database [26] and with color on face images from the Faces94 Face Database [27]. To evaluate the differences in experimental results, we utilized the same face databases for comparison.

The following three groups of face images have been selected from the Asian Face Database:

a) Faces with various expressions and slight different illumination; b) Faces with various poses and slight
different illumination; and c) Faces with frontal images but various illumination conditions. For each group, there are ten different aligned images of each of 40 distinct persons. Each image has a size of 40×50 pixels and each pixel has 256 gray levels. Typical examples of various facial images are shown in Figures 2, 3 and 4.

For the Faces94 Face Database, there are ten various images of each of 40 distinct persons. All images were taken at the same illumination (darker with green background) but slight various face expressions and non-aligned. The size of each image is 100×110 pixels, with 256 gray levels per pixel. An example is provided in Figure 5.

C. Facial Images Preprocessing

In this preprocessing stage, we add the Gradientfaces based normalization technique [17] in order to extract the illumination insensitive measures which will be described as follow :

c.1 Reflectance Model : The reflectance Model used in many cases can be expressed as

\[ I(x, y) = R(x, y) L(x, y) \]  

(1)

where \( I(x, y) \) is the image pixel value, \( R(x, y) \) is the reflectance and \( L(x, y) \) is the illuminance at each point \((x, y)\). Here, the nature of \( L(x, y) \) is determined by the characteristics of the surface of object. Therefore, \( R(x, y) \) can be regarded as an illumination insensitive measure. Separating the reflectance \( R \) and the illuminance \( L \) from real images is an ill-posed problem. In order to solve the problem, a “common” assumption is that \( L \) varies very slowly while \( R \) can change abruptly.

c.2 Gradientfaces : In order to extract illumination insensitive measure from gradient, we have the following theorem by studying the relationships between the components of gradient domain.

**Theorem 1 :** Given an arbitrary image \( I(x, y) \) taken illumination condition, the ratio of y-gradient of \( I(x, y) \) to x-gradient of \( I(x, y) \) is an illumination insensitive measure.

**Proof :** Considering two neighboring points \((x, y)\) and \((x+\Delta x, y)\), according to the illumination model (1), we have

\[ I(x, y) = R(x, y) L(x, y) \]  

(2)

\[ I(x+\Delta x, y) = R(x+\Delta x, y) L(x+\Delta x, y) \]  

(3)

Subtracting (2) from (3), we obtain

\[ I(x+\Delta x, y) - I(x, y) = R(x+\Delta x, y) L(x+\Delta x, y) - R(x, y) L(x, y) \]  

(4)

Based on the above-mentioned “common” assumption, which means \( L \) is approximately smooth, we have

\[ I(x+\Delta x, y) - I(x, y) \approx R(x+\Delta x, y) L(x+\Delta x, y) - R(x, y) L(x, y) \]

(4)

Taking the limitation of the above equality (4), we can obtain

\[ \frac{\partial I(x, y)}{\partial x} \approx L(x, y) \frac{\partial R(x, y)}{\partial x} \]

(5)

Similarly, we have

\[ \frac{\partial I(x, y)}{\partial y} \approx L(x, y) \frac{\partial R(x, y)}{\partial y} \]

(6)
Dividing (6) by (5), we have
\[
\frac{\partial I(x, y)}{\partial y} \approx \frac{\partial R(x, y)}{\partial y} \frac{\partial I(x, y)}{\partial x} \frac{\partial R(x, y)}{\partial x}
\]  
(7)

According to illumination model (1), R can be considered as an illumination insensitive measure. Thus, the ratio of y-gradient of I(x, y)/\partial y to x-gradient of I(x, y)/\partial x is also an illumination insensitive measure.

In practical application, the ratio of y-gradient of image to x-gradient of image might be infinitude derived by zero value of x-gradient of image. Therefore, it cannot be directly used as the illumination insensitive measure. These considerations lead us to defining Gradientfaces as follows.

**Definition 1**: I be an image under variable lighting conditions, then Gradientfaces (G) of image I can be defined as
\[
G = \arctan \left( \frac{I_y}{I_x} \right), \quad G \in [0, 2\pi)
\]
(8)
Where I_x and I_y are the gradient of image I in the x, y direction, respectively.

c.3 Implementation: In order to extract Gradientfaces, we need firstly to calculate the gradient of face image in the x, y direction. Gradientfaces can then be computed by the definition (8). There are many methods for calculating the gradient of image. However, the numerical calculation of derivative (gradient) is typically ill-posed. To compute the gradient stably, we smoothen the image first with Gaussian kernel function. With a convolution-type smoothing, the numerical calculation of gradient is much more stable in calculation. The main advantage for using Gaussian kernel is twofold: (a) Gradientfaces is more robust to image noise and, (b) it can reduce the effect of shadows. The implementation of Gradientfaces can be summarized in Table I.

<table>
<thead>
<tr>
<th>Table I Implementation of Gradientfaces</th>
</tr>
</thead>
</table>
| **Input:** Image I  
**Output:** The Gradientfaces of I  |

1. Smoothen input image by convolving with Gaussian kernel function:
   \[ I' = I * G(x, y, \sigma) \]
   where * is the convolution operator and
   \[ G(x, y, \sigma) = \left( \frac{1}{2\pi \sigma^2} \right) \exp \left( - \frac{x^2 + y^2}{2 \sigma^2} \right) \]
   is Gaussian kernel function with standard deviation \( \sigma \).

2. Compute the gradient of image I by feeding the smoothed image though a convolution operation with the derivative of Gaussian kernel function in the x, y directions:
   \[ I_x = I^* * G_x(x, y, \sigma) \]
   and
   \[ I_y = I^* * G_y(x, y, \sigma) \]
   where \( G_x(x, y, \sigma) \) and \( G_y(x, y, \sigma) \) are the derivative of Gaussian kernel function in the x, y directions, respectively.

3. Compute the illumination insensitive measure by
   \[ G = \arctan \left( \frac{I_y}{I_x} \right) \in [0, 2\pi) \]  
   (a)

4. Obtain Gradientfaces \( \leftarrow G \).

**Table I.** Implementation of Gradientfaces

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As Gradientfaces only works on grayscale images, color images are converted to grayscale images first before applying Gradientfaces. Figure 7 shows the original images, the grayscale images and the corresponding Gradientfaces processed images for a subject of the Faces94 Face Database. Same illumination but slightly darker with green background and slight various face expressions (upper row), corresponding grayscale images (middle row) and the corresponding Gradientfaces processed images (lower row)

**Figure 6** Sample images for a subject of the Asian Face Database with frontal images but various illumination conditions (upper row) and the corresponding Gradientfaces processed images (lower row)

**Figure 7** Sample images for a subject of the Faces94 Face Database. Same illumination but slightly darker with green background and slight various face expressions (upper row), corresponding grayscale images (middle row) and the corresponding Gradientfaces processed images (lower row)

D. Facial Feature Extraction using principle component analysis (PCA)

Initial feature of a facial image is the gray intensity of each pixel. Each facial image is converted into a row vector by appending each row one after another. For the Asian database which has facial images geometry normalized and illumination insensitive measures extracted by the Gradientfaces technique has image size of 40 x 50. It will become a 2,000 dimensional feature vector which is very...
high for any classification technique to be applied in order to learn the underlying classification rules. Therefore, principle component analysis (PCA) is applied to extract more relevant features/signatures [28]. Principle component analysis (PCA) is a simple statistical method to reduce the dimensionality while minimizing mean squared reconstruction error [28].

Let us assume that $M$ facial images that are denoted as $I_1, I_2, ..., I_M$ have size $a \times b$ pixels. Using conventional row appending method, we convert each of the images into $N = a \times b$ dimensional column vector. At first the mean image as column vector, $\Xi$ of size $N$, from all the image vectors of is calculated as shown in Equation (9).

$$\Xi = \frac{1}{M} \sum_{i=1}^{M} I_i \tag{9}$$

Then each face difference from the average is calculated using the equation (10).

$$a_i = I_i - \Xi \tag{10}$$

We then construct the matrix $A = [a_1, a_2, ..., a_M]$ containing all the mean-normalized face vectors as columns. Using this normalized face vectors we can calculate the covariance matrix $\mathcal{S}$ along the feature dimension of size $N \times N$ of all the features using the following conventional formula as:

$$\mathcal{S} = \frac{1}{N} AA^T \tag{11}$$

Here notice that the matrix $AA^T$ of size $2000 \times 2000$ needed to be constructed to calculate the matrix $\mathcal{S}$. However, it is virtually impossible for the memory constrains to perform any matrix operation on the $AA^T$ matrix. Rather, the method described in [29] is employed to construct the matrix $\mathcal{N}$ using Equation (12). Instead of $AA^T$, the matrix $A^T A$ of size $360 \times 360$ (out of 400 images 10 for each subject, 40 images one for each subject is kept apart for testing) is constructed as $\mathcal{N}$ of size $M \times M$ using:

$$\mathcal{N} = \frac{1}{M} A^T A \tag{12}$$

Then we calculate the eigenvalue and eigenvectors of this covariance matrix using Equation (13).

$$[V, D] = \text{eigs}(\mathcal{N}) \tag{13}$$

Here, $D = [d_1, d_2, ..., d_M]$ of size $M$ contains the sorted eigenvalues, such that $d_1 > d_2 > ... > d_M$ and the corresponding eigenvectors of the matrix $\mathcal{N}$ is contained in the matrix $V = [v_1, v_2, ..., v_M]$ which is of size $M \times M$.

According to the method proposed in [24], we can acquire the corresponding eigenvectors of the matrix $\mathcal{S}$ using $V = [v_1, v_2, ..., v_M]$ as:

$$U = A \times V \tag{14}$$

Here notice that, even though each vector $v_i$ is of size $M$, the vectors $u_i$ of $U = [u_1, u_2, ..., u_M]$ are of size $N$.

We can use the matrix $U$ to project our $N$ data onto lower $M$ dimensions. The projected data from the original $N$ dimensional space to a subspace spanned by $r$ principal eigenvectors (for the top $r$ eigenvalues) contained in the matrix $\Omega_r$ expressed as:

$$Y_r = \Omega_r A \tag{15}$$

In our previous research work [3], we chose the top 50 principle components as features in the lower dimension as the sum of the top 50 eigenvalues of the covariance matrix is more than 90% of the sum of all the eigenvalues.

E. Facial Recognition or Classification

When all the facial images are finally represented with relevant features by projecting onto a lower dimension using PCA, we can use similarity measures between faces from the same individual and different individuals. Assume that the normalized vector formed face test images are kept in the matrix $T$ (note that there are 40 images for 40 subjects that were not used in the PCA stage), where each column corresponds to a test face image. For classification, we first normalize the test images vector by subtracting the mean calculated previously (Equation (9)) using:

$$B = T - \Xi \tag{16}$$

Then using Equation (15) we project the normalized test data set as shown in the following equation.

$$Z_r = \Omega_r B \tag{17}$$

For each column in the matrix $Z_r$, we calculate the Euclidean Norm of the difference with the projected vectors of matrix $Y_r$. Finally, the test image is identified as the person with the smallest value among all the Euclidean Norm values.

IV. EXPERIMENTAL RESULTS AND DISCUSSION

Figures 8, 9 & 10 show the recognition accuracy with & without Gradientfaces preprocessing under various conditions for Asian Face Database.

In Figure 8, for face database with various facial expressions and slightly different illumination, there is a slight improvement in recognition accuracy with Gradientfaces illumination normalization in the preprocessing stage, from 51.75% to 59.75%.
In Figure 8, for the Asian Face Database with various facial expressions and slightly different illumination, there is a big improvement in recognition accuracy with Gradientfaces illumination normalization in the preprocessing stage, from 6.25% to 60.75%. The results are summarized in Table II.

<table>
<thead>
<tr>
<th>Conditions</th>
<th>Recognition accuracy without preprocessing</th>
<th>Recognition accuracy with preprocessing</th>
<th>% of improvement</th>
</tr>
</thead>
<tbody>
<tr>
<td>Various Expression</td>
<td>51.75%</td>
<td>59.75%</td>
<td>15.45%</td>
</tr>
<tr>
<td>Various Poses</td>
<td>15.50%</td>
<td>36.50%</td>
<td>235.48%</td>
</tr>
<tr>
<td>Various Illumination</td>
<td>6.25%</td>
<td>60.75%</td>
<td>972.00%</td>
</tr>
</tbody>
</table>

In Figure 9, for face database with various poses and slightly different illumination, there is a big improvement in recognition accuracy with Gradientfaces illumination normalization in the preprocessing stage, from 15.50% to 36.50%.

In Figure 10, for face database with frontal images but various illumination, there is a much bigger improvement in recognition accuracy with Gradientfaces illumination normalization in the preprocessing stage, from 6.25% to 60.75%. The results are summarized in Table II.

<table>
<thead>
<tr>
<th>Conditions</th>
<th>Recognition accuracy without preprocessing</th>
<th>Recognition accuracy with preprocessing</th>
<th>% of improvement</th>
</tr>
</thead>
<tbody>
<tr>
<td>Color Images</td>
<td>38.00%</td>
<td>99.50%</td>
<td>261.84%</td>
</tr>
</tbody>
</table>

V. CONCLUSIONS

Illumination and color have been major problems on our PCA based human face recognition. With illumination normalization technique in the facial image preprocessing stage to extract the illumination invariant features, it improves the recognition rate. Among all the illumination normalization techniques we have evaluated, Gradientfaces has been identified as the one which works well with our
PCA based human face recognition system. It greatly improves the recognition rate especially those images under various illumination conditions, from a low recognition rate of 6.25% to 60.75%. It also improves recognition rate for color images with color background, from 38% to 99.50%.

Apart from facial images with various illumination and color, distorted images also include noisy & blurry images. With the characteristic of Gradientfaces normalization technique, further research works will be done on those noisy & blurry facial images if this Gradientfaces can also work well with our PCA based human face recognition system.

REFERENCES


[26] Asian face database from Intelligent Media Laboratory, www.imlab.postech.ac.kr

