# Periodic Boundary Cellular Automata Based Wear Leveling for Resistive Memory

Sutapa Sarkar, Manisha Ghosh, Biplab Kumar Sikdar, Mousumi Saha

Abstract—Locality of reference is preferable every time while writing to cache blocks. The write process may repeat only on a few adjacent cache blocks. As a result, it creates a stress on those blocks. If resistive memory is chosen to be the fundamental technology for the write purpose, the write sensitivity on those blocks increases more. It causes a loss to the durability of the memory. It can be damaged earlier in comparison to NAND/NOR Flash memories ( $10^5$  to  $10^6$  program/erase cycles). This non-uniformity in writes as well as malicious attacks in CMPs cache can cause sudden breakdown of those systems. The wear out of memory blocks at their primary stages can be avoided by wear leveling through distribution of writes to different blocks.

This work represents an efficient scheme of wear leveling applied specifically for resistive memories. The major part of this work is developed around one dimensional two state CA. It has the aim to achieve uniform writes throughout all memory blocks with spatial access pattern predictions. The adjacent write-overloaded blocks are considered as an area subjected to remapping. The periodic boundary cellular automata (PBCA) employed for the scheme performs density classification task (DCT) to choose the remapping zone of memory. Remapping is executed through changing the current address location of the identified memory blocks to the new location. Further, the proposed memory write management policy can be implemented together with the fault tolerant memory architecture to develop a memory subsystem with more durability and robustness.

*Index Terms*—Spatial access characteristics; Wear leveling; Density classification task; Periodic Boundary Cellular Automata.

#### I. INTRODUCTION

T HE performance of computing models of pipelining and superscalar processor [1] [2] is limiting due to reduction in throughput. Those processors require an increasing power budget which exceeds the standard of Moore's law. So, these are losing their suitability now a days. Chip multiprocessors (CMPs) are on the other hand the combination of several single processors fabricated in a single chip. Single core architecture is replaced by multicore processor (CMPs) [3] [4] [5]. But *on-chip* cache size has to be large in CMPs and it acquires a significant area of total chip floor. Therefore resistive memory (RRAM/ReRAM) is chosen in place of DRAM/Flash memories to take the advantages of higher

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packaging density as well as increasing scalability with lower energy consumption [6] [7]. However, the major disadvantage faced with *write issues* in ReRAM is that it is related to durability and reliability of the memory cells. Locality of reference generates write stress on some memory blocks which are rewritten a large number of times. It causes a severe reduction in *life time* of such memory and that is at least 20X faster than that of uniformly written but worn-out memory cells [8].

Since the last few decades the wear leveling scheme has been used to bring uniformity in the writes to all the blocks of a memory. It has been found to be applied in NAND Flash, as well as NVRAM technologies [9] [11] [33]. Resistive memory writing policy can be improved with this scheme but it requires some technology based modifications. Wear leveling can be defined by the process of shifting a write request from a memory block to another memory block [10]. Wear leveling schemes are subdivided into two different parts : 1) cause of multiple writes on the memory blocks having unbalanced distribution of workload of chip multiprocessors (CMPs) or for malicious attacks, 2) depending on the techniques of remapping like a look up table based/algebraic based method. Some categories of wear leveling schemes are compared in Table I, providing workload/attack-based and algebraic/table-based schemes.

Typical workload-based schemes are incapable of dealing with repetitive writes due to malicious attacks. Even system failure can occur within a small time span. A scheme called Practical Attack Detector (PAD) is proposed in [12] which can stop the cell failure due to malicious attacks by keeping a track on the write streams within a short time frame. The Rancar scheme deals with repeat address attack (RAA) through adaptive remapping in hybrid cache memory [13]. It translates the physical address to intermediate address for intraset/inter-set remapping by interchanging set index bits and tag bits. A table based (deterministic method) remapping scheme reported in [14] for resistive memory. Algebraic address remapping, defined in [6] [12] [15] can be adjusted in limited space overhead and to remove the look up table requirements because of the growing size of Look up table shows linearity with memory capacity.

Recently, cellular automata (CA) is being applied to some applications in cache system design such as detection of fault, data migration, protocol processor, fault tolerant and self-corrected memory etc. [16] [17] [18] [19] [20]. In this paper, a *CA* based approach is applied for workload based wear leveling in resistive memory. This research work targets to increase the system lifetime [15] by enhancing the durability of resistive memory cells by uniformly distributing writes in all the blocks. Access pattern identifies the write-stressed memory blocks as well as the less written memory blocks.

Write distribution among the memory blocks shows pro-

Schemes	Memory tech-	Granularity	Parameter reviewed	Remapping technique	Special feature
	nology	level	D did to d		
Start-gap [9]	РСМ	Cache line	Repetitive write activ- ity due to spatial lo- cality of reference	Address space randomization using Invertible Binary matrix and Fiestel network based al- gorithm	Start gap is basically intended for un- even workload distribution but Region based start gap is also effective for malicious attacks.
Car [13]	Hybrid- DRAM & PCM	Cache Set	Repeated set attack	Randomized cache address remapping method by swapping set and tag index bits	It adversely affects the spatial local- ity of reference for ordinary programs which are not subjected under attacks.
OWL [28]	NAND FLASH	Block	Temporal write activ- ity	Look up table based method	The scheme observes flip bits to ensure reduction of overwrites thereby elim- inating redundancy of repetitive write operations.
XWL [14]	Crossbar ReRAM	Block	Effective write activ- ity for different data pattern and row ad- dresses.	Look up table based method	The scheme is based on lifetime of a ReRAM cell as a function of IR voltage drop and large sneaky currents.
WAPTM [24]	PCM	Page	Write-activity	Look up table based method	Already implemented for Google An- droid 2.3 based on ARM architecture for reduction of write activity into page table.
Software based wear- leveling [27]	Hybrid- PCM+DRAM	Memory ad- dress	Write activity	Integer linear programming formulation & polynomial- time algorithm	Requirement of hardware is eliminated
PAD [12]	PCM	Cache line	Malicious attack	Not addressed	Adaptive wear leveling scheme is pro- posed in addition to prevention of ma- licious attack by calculating attack den- sity
Ouroborous [8]	NVRAM- PCM/FeRAM /STT-MRAM	Local & global region	Spatial write pattern is observed for access pattern prediction & malicious attack	Hybrid scheme with both table & algebraic based method.	It determines access pattern as well as demand prediction for local and global wear leveling.

TABLE I: COMPARATIVE STUDY ON DIFFERENT WEAR LEVELING SCHEMES

gram locality within few adjacent memory blocks mentioned as zone. The appropriateness of any wear leveling scheme lies in the selection of the size of the zone. Here, in this paper, the small-sized source as well as target remapping zone is identified by parallel operation. Spatial locality of reference is applied to predict precise and specific writestressed and less written zone by two stage hierarchical design using density classification task (*DCT*) that employs periodic boundary cellular automata (*PBCA*). An algebraic address translation procedure is used to obtain local/global remapping (address translation of central memory address) of the zone. This can be considered as a simple but costeffective scheme. This scheme can be implemented as an alternative method of workload-based traditional wear leveling schemes [15] irrespective of memory technology.

Section II gives basic concepts of *CA*. Motivation of this research work is introduced in Section III. Section IV describes the design framework of wear leveling in resistive memory. In Section V, *PBCA* based design methodology to find out the blocks to be remapped is explained. The address remapping technique is established in Section VI. Section VII evaluates the performance of the proposed scheme and ultimately the conclusion and future scope is stated in Section VIII.

## II. BASICS OF CELLULAR AUTOMATA

Cellular Automata (CA) can be appropriately used to model physical systems [29] [31] as of cache memory of chip multiprocessors (CMPs). *CA* has the following flavour for modelling and designing of any physical or biological system: i) homogeneous cellular structure, ii) scalability, iii) modularity, iv) local interaction among cells provides global condition of CA, iv) interaction may be confined in between the left neighbouring cell, cell itself and right neighbouring cell and v) parallel processing (parallelism).

The basic architecture of CA is analogous to autonomous Finite State Machine (FSM). So, the cells of a CA are allowed to evolve in discrete space and time. The next state computation of cells is occurred in accordance with applied transition function  $(f_i)$  - that is based on rule or logic. A CA cell always stores a value (or state) at discrete time instant 't'. The state of the  $i^{th}$  cell  $(S_i^t)$  at time t, is referred as the current or present state (PS). Two-state CA can keep only binary values (or states) '0' and '1'. The transition function  $f_i$  of a rule in 3-neighborhood, two-state and onedimensional CA can be given by Equation 1. The next states (NSs) of the  $i^{th}$  cell, it's left and right neighbours are specified by  $S_i^{t+1}$ ,  $S_{i-1}^{t+1}$  and  $S_{i+1}^{t+1}$  respectively.

$$S_i^{t+1} = f_i(S_{i-1}^t, S_i^t, S_{i+1}^t)$$
(1)

The cells of CA can be constructed by D flip-flop (Delay flip flop). A digital circuit of combinational logic can be used to realize the logic function  $f_i$  in accordance with the applied design rule [30]. Implementation of Rule 232 and 226 in CA is given in Figure 2. The combinational logic functions and D flip-flops are used to design the hardware of hybrid PBCA as shown in Figure 1.

The possible combinations of next states (NSs) of the  $i^{th}$  cell of a CA are exemplified in the rows of Table II which cumulatively represent a rule. The rule is expressed in the



Fig. 1: Block diagram of n-cell periodic boundary CA



Fig. 2: Next state functions of rules 232 and 226

format of it's decimal equivalent. For a 3-neighborhood CA, total number of possibility of CA rules are  $2^{2^3}$  (256). Table II shows few of those rules like '232', '226', '192' and '184' which are employed in the current design.

The collective combination of the applied rules  $(R_i s)$  of a CA represents the rule vector of that CA. A typical example of a rule vector is given in Equation 2.

$$R = \langle R_1, R_2, \dots, R_n \rangle = \langle 232, 184, 184, 184, 184, 184 \rangle$$
(2)

In null boundary CA, the status of the left to leftmost cell  $S_0$  is considered as logic value '0' (null) and it is also the case of right of a right most cell  $S_{n+1}$  that is '0' (null). For periodic boundary CA,  $S_0 = S_n$  and  $S_{n+1} = S_1$ , as given in Figure 1. A nonuniform or hybrid CA is configured with different rules for it's cells. But, uniform CA which is a special type of nonuniform CA, have  $R_1 = R_2 = \cdots = R_n$ . CA behaviour can be observed by state transition diagram (STD) which shows the sequence of states for evolution with time as shown in Figure 15. Single or multiple cycles are observed in STD. The CA can be categorized as reversible CA or irreversible CA according to the presence of those cycles.

Reachability tree is a form of binary tree mainly used to represent the reachable states of a CA in different levels of operation. Root node carries all possible RMTs (rule mean terms) of a rule. Those RMTs having '0' as their next states are kept under left edge (0-edge) of the tree. Those RMTs with their next state value as '1' are kept under right (1-edge) of the tree. The number of levels of the tree is determined by the number of cells of a CA.

Rechability tree can also be constructed to detect the



Level-2

Fig. 3. Reachability tree for <232 232 232>



Fig. 4. Reachability tree for attractor of hybrid CA <232 184 184 ...>

possible cycles or attractors formed in the state transition diagram for a rule vector of a CA. Figure 3 shows the reachability tree for the uniform CA<232 232 232>. On the other hand, the reachability tree for attractor of hybrid CA< 232 184 184 ... > is shown in Figure 4. Here periodic boundary condition is considered for both the cases. Rule 232 and rule 184 are used to realize our wear leveling method for resistive memory.

#### III. MOTIVATION

With increasing number of cores in CMPs, off-chip memory puts limitation in terms of bandwidth, latency and speed of operation.

To get rid of this bottleneck, on-chip memory is given

Present State	111	110	101	100	011	010	001	000	Rule
RMT	(7)	(6)	(5)	(4)	(3)	(2)	(1)	(0)	
Next State	1	1	1	0	1	0	0	0	232
Next State	1	1	1	0	0	0	1	0	226
Next State	1	1	0	0	0	0	0	0	192
Next State	1	0	1	1	1	0	0	0	184





Fig. 5. Partitioned hybrid cache architecture with STTRAM & SRAM

priority over off-chip memory. CMPs generally have on-chip two or three cache layers (L1 and L2 or L1, L2 and L3), from which L1 is private cache of each core and L2 or L3 is last level cache shared among the cores. But a large-sized onchip cache is required to mitigate the demand of the growing number of cores. The cache can be accommodated within the chip area if it can have higher package density and scalability like resistive memory. ReRAM is available in varieties namely Phase Change memory (PCM), Spin-transfer Torque memory (STTRAM), Magneto Resistive RAM (MRAM), Ferro-electric RAM (FeRAM), Memristors etc. Different types of resistive memory technology is compared in Table III. Hybrid *on-chip* cache has also been proposed in [6] [21] [22] where resistive memory and SRAM/DRAM are used together to exploit the advantages of both. A typical CMPs with four cores and shared Last Level Cache (LLC) is shown in Figure 5. Cores may be interconnected to hybrid LLC through bus, switch or a hybrid type of connectivity.

SMPCache simulator is developed to consider uniprocessor or multiprocessor traces which represent the memory access in terms of opcode read, data read and data write used for SMP/DSM multiprocessors. Single processor traces are considered for the current work that are taken from SPEC92 benchmarks (Hydro, Nasa7, Cexp, Mdljd, Ear, Comp, Wave, Swm and UComp). These are the few example traces collected from some real tests carried out on a MIPS R2000 system. All these represent a wide variety of "real" application programs which are come from the Parallel Architecture Research Laboratory, New Mexico State University.

A typical eight-core CMPs with two levels of setassociative cache architecture are configured for simulation to identify memory accesses (opcode read, data read and write) to the memory blocks. [23]. Figure 6 shows the statistics of total number of accesses, write accesses and



Fig. 6. Statistics of memory block's access in trace files collected from SMPcache

number of repetitively written memory blocks for WAVE, NASA7, SWM etc [23]. To assess the fact of spatial locality of reference, all processor's ( $P_0$ - $P_7$ ) write access patterns are observed and detailed in Table IV by complete system simulation of *SMPCache*. Observation reveals the fact that the write-distribution is concentrated within a very few number of cache blocks and other blocks are seldom written. Further, spatial locality of reference is noticed for contiguous memory blocks (later termed as cache zone) that can be considered for remapping candidates. Therefore, the current work is motivated to investigate a solution for resistive memory system through wear leveling. Algebraic remapping technique is considered to increase the cell lifetime that makes a high endurance memory system.

# IV. DESIGN FRAMEWORK

To adopt wear leveling in ReRAM/RRAM, two distinct types of operations need to be performed: i) Selection of source (write stressed) and target (seldom written) memory blocks to be remapped and ii) Determination of the target address from the source address. In this design, CMPs are assumed to have two layers of *on-chip* cache (L1 and L2), where L1 is private to each core and shared L2 is considered with set-associative mapping policy. Logical, contiguous and fixed-size portion of memory are considered as remapping zone. Remapping zone is found from write access pattern of memory block by employing *DCT*.

The Last level cache (LLC) blocks are considered into groups with M number of memory blocks per group. In pre-processing stage, these groups are categorized into two types: i) seldom or never used and ii) write dominated. Further, at decision stage, right and/or left half of the group (M/2 blocks) are selected to get the exact remapping candidates. Hierarchical with two stage *CA* based density classification task (*DCT*) is performed on the access pattern of the memory blocks to identify the category of memory blocks. Global/local remapping is performed by redirecting the write request. When less written zone is found within the

Memory technology	FeRAM	MRAM	STT-RAM	PCM
Nonvolatility	Yes	Yes	Yes	Yes
Cell size	Large	Large	Small	Small
Package Density(ratio)	Low	Low	High	High
Read access time(ns)	20 to 80	3 to 20	2 to 20	20 to 50
Write access time(ns)	50	3 to 20	2 to 20	20
Write energy consumption	Mid	Mid-High	Low	Low
Cell lifetime (in terms of number of	$10^{12}$	$> 10^{15}$	$> 10^{16}$	$10^{12}$
writes)				

#### TABLE III. COMPARISON ON DIFFERENT RESISTIVE MEMORY TYPES

Processor	Block address	Number of times written
$P_0$	1416, 1493	single
	1515-1517, 1518-1520,	1516, 1520-1521 multiple
	1521-1522	
	3596	multiple
$P_1$	2037-2039	2037-single
	2043-2045	2043-multiple
	3141	single
$P_2$	1521	single
	3843-3845	3845-single
$P_3$	2037-2039	2037-single
	2043-2045	single
	3141	single
$P_4$	1515-1517	multiple
	1518-1520	1520-multiple
	3141	single
$P_5$	1521	multiple
	2035	single
	3843-3844	multiple
$P_6$	1521	multiple
	2043	multiple
	3843-3845	3845-single
$P_7$	2043-2044	2043-multiple
	3843-3845	3845-single

#### TABLE IV. WRITE ACCESS PATTERN

same memory set, local or *intra-set* remapping is performed. But when it is found in different set, global or *inter-set* remapping is performed.



Fig. 7. Remapping in memory sub-system

Block diagram of a tentative design frame work with memory subsystem is described in Figure. 7. Processing unit generates virtual address which is further translated into physical address for memory access. But remapping technique creates a translation level in-between virtual address and physical address. Therefore, memory controller is equipped with subblock control logic, remapping candidate selection logic and remapping address generation unit. Remapping Candidate Selection Logic (*RCSL*) is a *CA* based unit used to detect the write-stressed memory blocks (source zone) as well as less written memory blocks (target zone). Those memory blocks which do not require any address translation can directly be applied to physical memory. But when remapping is required, memory controller sends the control to address generation block where the central address of source zone is translated to target address (central address of target zone). So, the virtual address is translated to physical address through intermediate address for accessing the physical memory as shown in Figure 7.

# A. Density classification task

The CA can be initialized with a binary pattern called Initial Configuration (IC) or seed. The seed is random in nature [25]. After that, CA is allowed to iterate up to a permissible number of steps. It may reach an attractor which does not allow further changes of states anymore. Onedimensional and two-state CA can be used to discriminate binary strings according to the densities of (1s or 0s). This operation is called density classification task (DCT).

The CA has the capacity to classify the initial configurations (ICs) having more ones or zeros in their bit pattern. They use to settle to an attractor having minimum hamming distance from the attractors. If seed contains more 0s (1s) than 1s (0s), the CA settles to a fixed point of all 1s (0s). DCT may be performed by realizing one or two stages. In two-stage DCT, two different CA rules are applied one after another, hierarchically. First stage with a given rule is iterated for  $t_1$  time steps. The resulting configuration is iterated for  $t_2$  time steps with another rule in the next stage [26].

#### B. Requirements of PBCA rules for DCT

For PBCA based solution of the DCT applied for the current design, CA has the following required features:

- Req1: Two attractors with single length cycle
- *Req2*: Formation of attractors having all 0s and all 1s *Req3*: Binary string (seed) having greater than 50% 1s
- (0s) should fall on all 1s (0s) attractors
- *Req4*: CA does not contain any other attractors (single length or multilength cycle)

## C. Selection of design rules

For two-stage operation, two different sets of rules are selected. Six cell hybrid *PBCA* with rule vector < 232 184 184 184 184 > or < 232 226 226 226 226 226 226 > can be selected for the first stage. Three cell uniform rule vector is found appropriate for decision stage Figure 7.

	1	0	0	0	0	1	1	0	0	0	1	1	0	1	0	1	0	1	1	0	0	0	0	1	0	1	0	0	
	4						Å	, r	-1																		2.0	Ĩ	-1
A	$SP_a$	rr[(	]			I	151	arr	ı																	AS	$P_{ar}$	r[N	– []

Fig. 8. Access pattern array

As per the given STD of 6-cell hybrid < 232 226 226 226 226 226 226 > or < 232 184 184 184 184 184 >, *Req1* and *Req2* are satisfied for the following design. As, there are two attractors (all 0s and all 1s) in PBCA rule employed in the current design. Further, all 0s and 1s attractors are single length cycle attractors those present in STD as shown in Figure 9 or Figure 14. But it has another attractor defined as  $\alpha$ -basin which is a multi-length cycle attractor. Though it does not contribute any error as it is interpreted in another way. Decision stage is based on rule < 232 232 232 > for the presence of all 0s and all 1s single length cycle attractors.

#### V. DESIGN METHODOLOGY

CMPs have many processors integrated in a single chip die. Those processors may access a contiguous shared cache memory (L2) at any instant. Due to uneven distribution of work-load, few memory blocks are written repetitively. These blocks are contiguous in nature as *spatial locality of reference* is observed in their access pattern. Let us assume, k number of processors (cores)  $Q_1$ ,  $Q_2$ ,  $Q_3$ , ......,  $Q_k$ are integrated within a chip. An access pattern array (of length N) keeps the write access information of each and every last level cacheline whose length is also 'N'. Spatial access pattern register ( $ASP_{arr}$ ) keeps the information of write access in terms of binary nonzero value. At any time instant, if the *i*<sup>th</sup> block MB[i] is written, the position of  $ASP_{arr}[i]$  is set as shown in Figure 8.

Each memory block can be represented by identical CA as it stores binary values, those are updated at discrete time instants. CA is iterated upto an attractor state or stable state. Here, CA settles down to an attractor basin having hamming distance closer to initial configuration (seed). Six cell hybrid

CA with rule vector  $< 232\ 184\ 184\ 184\ 184\ 184 >$  is iterated upto the depth of CA or until it reaches an attractor of 0-basin or 1-basin. LSB of the attractor are considered likewise:

- Case-1: Lsb of CA is 0 for seldom written zone
- Case-2: Lsb of CA is 1 for write dominated

State transition diagram of 6-cell hybrid PBCA with rule vector < 232 184 184 184 184 184 184 > is shown in Figure 14. 3-cell uniform PBCA < 232 232 232 > is employed in decision stage which is carried out for single time step. Check bits (LSB bits of CAs) are collected and saved to infer results.

To keep the remapping zone small, M=6 is assumed in this example as shown in Figure 10. Therefore, number of groups are formed having six cells in each. The first stage and final stage are operated hierarchically to perform *DCT* for categorization of memory blocks. CA is loaded with *seed* taken from  $ASP_{arr}$  and iterated. States with more than 50% of '0' ('1') in their bit pattern, fall in 0-basin (1-basin).

Space time evolution of a typical example is shown in Figure 11 (Figure 12). The *CA* falls on all 1s basin in first stage after four (five) clock states. In final stage, it is concluded that left half is *seldom written* zone and right half is *write stressed* zone as per Figure 13.

The left and right half (three memory blocks) are splitted out of six contiguous memory blocks and are processed in final stage (decision phase). 3-cell uniform PBCA with rule  $< 232 \ 232 \ 232 \ >$  is applied in each group. Space time evolution shows every iteration upto the settling points or attractors ('0' and '1') as shown in Figure 13.

Like first stage here also, the check bit is the least significant bit (LSB) bit of the attractor and saved in a register. For write-stressed block, the checkbit is '1' and '0' for less written memory blocks. Here in this example, as shown in Figure 13, left half has fallen in 0- basin and right half has fallen in 1-basin. They are considered as less written or write dominated blocks accordingly. In Figure.10, the generation of checkbits are illustrated. Both the CAs are initialized with the values of access pattern array to find the appropriate remapping zone.

In the first stage (pre-processing stage), alternate rule 226 can be used instead of rule 184. Therefore, 6-cell hybrid CA  $<232\ 226\ 226\ 226\ 226\ 226\ 226\ can work appropriately as an alternative to <math display="inline"><232\ 184\ 184\ 184\ 184\ 184\ >.$  Comparative state analysis report is furnished in Table VIII which shows some minor differences in performance as follows:

- i) Depth of CA is different.
- ii) Same state may not settle to same attractor.
- iii) State transition diagram shows different iteration time for same state transition.

In Figure 10, two groups are considered as the number of memory blocks are 12. The groups correspond to CA-1 and CA-2. The attractor-1 and attractor-2 produce checkbits, which are found as '1' and '0'. Therefore, group-2 is considered as seldom written zone and group-1 is write stressed zone. To keep the remapping zone smaller, only three memory blocks are identified from the selected cache zone by making it divide by two.

These two groups (group-2L and group-2R) are iterated again to perform DCT with the 3-cell PBCA with uniform



Fig. 9. STD for 6-cell < 232 226 226 226 226 226 > hybrid PBCA



Fig. 10. Generation of checkbits

rule set of  $< 232\ 232\ 232 >$ . *CA-3* and *CA-4* settle to any of the two attractors '000' or '111' within a single clock cycle as shown in Figure 15. According to the given example, both *CA-3* and *CA-4* settle down to '111' attractor. The checkbit (LSB of the attractor) is '1' for left hand side as well as the right hand side. The decision is taken as per decision rule as illustrated in Table V. Therefore, both RHS and LHS are *write dominated* and the candidates of remapping as per decision rule.

# VI. ADDRESS REMAPPING TECHNIQUE

Remapping candidates are write-stressed zone (three contiguous memory blocks) that must be mapped to another less

Access pattern

	State	1	0	0	1	1	1
$i_0$	CA	232	184	184	184	184	184
	State	1	1	0	1	1	1
$i_1$	CA	232	184	184	184	184	184
	State	1	0	1	1	1	1
$i_2$	CA	232	184	184	184	184	184
	State	1	1	1	1	1	1
$i_3$	CA	232	184	184	184	184	184
	State	1	1	1	1	1	1
$i_4$	CA	232	184	184	184	184	184

Fig. 11. Space time evolution of pre-processing stage with hybrid rule <232 184 184 184 184 184 184 >

written zone (three contiguous memory blocks). Remapping Candidate Selection Logic (RCSL) block identifies the write-stressed zone as well as less written zone through CA. Intraset remapping is performed in between blocks of a set (local wear leveling) and Interset remapping is performed among different sets (global wear leveling) [8]. The source zone (write-stressed zone) of remapping are found alongwith the target zone (less written zone) in parallel operation. The conversion of block address from write-stressed zone to seldom written zone is performed in remapping-address generation unit. New block address generation (intermediate address) from older ones is achieved through algebraic technique for local (Intraset) as well as global Interset zone remapping. Address generation block produces the remapped

TABLE V. DECIS	SION RUL	ĿΕ
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Checkbit-0	Checkbit-1	Decision	Remarks
0	0	Neither LHS or RHS is write dominated	Remapping is not required
0	1	RHS is write dominated	3 cells of RHS are remapping candidates
1	0	LHS is write dominated	3 cells of LHS are remapping candidates
1	1	Both LHS and RHS are write dominated	Remapping is required for all 6 cells

Access pattern



Fig. 12. Space time evolution of the first stage with hybrid rule < 232 226 226 226 226 226 226 >

		Ι	$_{\rm HS}$					RHS	
$\operatorname{St}$	ate	1	0	0	S	tate	1	1	1
$i_1$	CA	232	232	232	$i_1$	$\mathbf{C}\mathbf{A}$	232	232	232
$\operatorname{St}$	ate	0 1	7 0 5	2 0	, s	tate	1	71 5	11
$i_2$	CA	232	232	232	$i_2$	CA	232	232	232
St	ate	7 0	2 0 5	7 0	, s	tate	1 5	71 5	71
$i_3$	$\mathbf{CA}$	232	232	232	$i_3$	$\mathbf{CA}$	232	232	232
				Ť					÷.
			Chec	$kbit_0$				Chec	$kbit_1$

Fig. 13. Space time evolution of final stage

address in consultation with the memory controller.

Let S be a non-empty group with a defined operation '\*' in it. T be a subgroup of S then  $\{a^*T \mid a \in S\}$  is called a coset. In this case, it is called left coset whereas T\*a is called right coset. For normal subgroup,  $a^*T=T^*a$ . Cosets always partition the set into disjoint sets. For normal subgroup, cosets are identical or disjoint sets. The number of cosets is defined by the Equation 3 [32].

$$[S:T] = \frac{S_k}{T_k} \tag{3}$$

Group of all memory words (S) is  $\langle Z_{256}, + \rangle$  and  $\langle Z_{16}, + \rangle$  represents a subgroup (T). Therefore number of the cosets is 16 as per Equation 3. Therefore, the number of blocks per set is 16 (N) with 16 number of sets (M). Here operation \* is represented by the Equation 4.

$$a * b = (a+b)mod(n-tuples)\dots\{a, b \in S\}$$
(4)

The set of distinct cosets or partitions (P) represents the quotient group and given by Equation 5.

$$Q = \{\{0 + H\}, \{1 + H\}, \dots, \{15 + H\}\}$$
(5)

From the physical address, we can find out the bank and cache block address. Block address can be as per Equation 6.

$$MB_i = M * n + j \tag{6}$$

Here i denotes the block index. Set index (j) and block offset (n) variables are the remapping parameters. These can be varied from 0 to M-1 and 0 to N-1 respectively to adjust remapping offsets. To change within set or local wear leveling, block offset (n) and for global wear leveling set index (j) has to be varied in Equation 6. Let us take an example here with length of memory is 1024. S =  $< Z_{1024}$ ,+ > represents group of all memory words and T =  $\langle Z_{16}, + \rangle$ represents subgroup of memory block within a set. Distinct cosets/partitions are collection of blocks with index numbers are  $P_0 = \langle 0, 16, 32, 48, 64 ... \rangle$ ,  $P_1 = \langle 1, 17, 33, 49, 65 ... \rangle$ ,  $..P_{15} = <15, 31, 47, 63..>$ . Block of index number 49 can be written as  $MB_{49}=16*3 + 1$ . For global (interset) mapping the set index is changed from 1 to 6. So, the new block address will be 54 belonging to set 6. For local mapping j is to be varied in Equation 6.

#### VII. PERFORMANCE ANALYSIS

The density classification task (DCT) is a standard tool incorporated in the design to assess the spatial locality of reference or to identify the reused set of contiguous memory blocks. Write pressure is targeted to be reduced on those spatially located blocks using redirection of writes to another contiguous less written blocks. Source or target remapping zones are distinguished by the attractors of the employed CAs in consecutive two-stage operations as described in Section V. The Access pattern array is saved with a nonzero value to the corresponding position of the block for indicating write operation on it. In Table VI, all the possible number of states are classified as per the presence of number of 1s within the states. Those states, having less than 50% of 1s in their access pattern, fall on 0-basin and having more than 50% of 1s, fall on 1-basin for CA < 232 226 226 226 226 226 > as shown in Table VI and for CA <232 184 184 184 184 184 > as shown in Table Table VII. Almost uniformly distributed 0s and 1s states fall in  $\alpha$ -basin (Table VI and VII). Few states are falling on opposite basin introducing errors in the design.

Hybridized CA with rule 232 & 184 and rule 232 & 226 can perform the same function in the following design and can be employed as alternate rules in the first stage. But they will show a relative advantage and/or disadvantage in performance in terms of misprediction rate and speed of execution. PBCA with rule 232 and rule 226, have a single state '48' (110000) associated with 1-basin causes mispredication. State '30' (011110) which falls in 0-basin, is another mispredicted state that introduces error in the design. Though few states with equal number of 0s (1s) in their bit



Fig. 14. STD for 6-cell < 232 184 184 184 184 184 > hybrid PBCA

TABLE VI. DESIGN ANALYSIS REPORT WITH CA  $<232\ 226\ 226\ 226\ 226\ 226\ 226\ 226$ 

	4		2	4	-
Number of	1	2	3	4	5
ones					
ones					
States	1, 2, 4, 8, 16,	3, 5, 6, 9, 10, 12, 17, 18,	7, 11, 13, 14, 19, 21,	15, 23, 27, 29, 30, 39, 43,	31, 47, 51, 55,
	32	20, 24, 33, 34, 36, 40, 48	22, 25, 26, 28, 35, 37,	45, 46, 49, 50, 53, 54, 57,	59, 61, 62
			38, 41, 42, 44, 52, 56	58, 60	
basin-0	1, 2, 4, 8, 16,	3, 5, 6, 9, 10, 12, 17, 18,	13, 14, 22, 26, 28	30	-
	32	20, 24, 33, 34, 36, 40			
basin-1	-	48	41, 52, 56	15, 23, 29, 39, 43, 45, 46,	31, 47, 51, 55,
				49, 50, 53, 54, 57, 58, 60	59, 61, 62
basin- $\alpha$	-	-	7, 11, 19, 25, 27 35,	-	-
			37, 38, 42, 44		
Misprediction	-	48 has fallen in basin-63	-	30 has fallen in basin-0	



Fig. 15. State transition diagram of 3-cell uniform PBCA<232 232 232>

pattern fall on 1-basin (3 states) or 0-basin (5 states) does not cause any misprediction to insert any errors. Rule 232 and 184 have two mis-predicted states. State '15' fall in 0basin (having greater than 50% of 1s) and '33' fall in 1-basin (having lesser than 50% of 1s) will contribute a little bit error in the design as they fall in opposite basin. Here also few states (5 states) with equal distribution fall on 0-basin or 1basin (3 states) but doesn't contribute to any error contents as above.

It is observed that both the rules used for first stage have an  $\alpha$  basin present on the state transition diagams (STDs) of CA < 232 226 226 226 226 226 > and CA < 232184 184 184 184 184 > as shown in Figure 9 and Figure 14. As per requirement 4 (Req4), apart from all 0s and all 1s attractor no other attractors are permissible in proposed selection logic. Though no single length attractor is found, but one multilength attractor  $(21 \rightarrow 42 \rightarrow 21)$  is found in STDs. Hence the presence of this multilength loop (21  $\rightarrow$  $42 \rightarrow 21$ ) in them is violating the requirement (*Req4*) of the cellular automata (CA) based remapping candidate selection logic. But this basin is associated with all the uniformly distributed states for both the rules. Therefore, the presence of ' $\alpha$ ' basin does not contribute any error in the design. Recollecting that this zone is defined as neither write stressed nor seldom written. Comparative analysis of the PBCA with

Number of	1	2	3	4	5
ones	-	-	5		ũ là chiến c
ones					
States	1, 2, 4, 8, 16,	3, 5, 6, 9, 10, 12, 17, 18,	7, 11, 13, 14, 19, 21,	15, 23, 27, 29, 30, 39, 43,	31, 47, 51, 55,
	32	20, 24, 33, 34, 36, 40, 48	22, 25, 26, 28, 35, 37,	45, 46, 49, 50, 53, 54, 57,	59, 61, 62
			38, 41, 42, 44, 52, 56	58, 60	
basin-0	1, 2, 4, 8, 16,	3, 5, 6, 9, 10, 12, 17, 18,	7, 11, 13, 14, 22	15	-
	32	20, 24, 34, 36, 40, 48			
basin-1	-	33	35, 37, 41	23, 27, 29, 30, 39, 43, 45,	31, 47, 51, 55,
				46, 49, 50, 53, 54, 57, 58,	59, 61, 62
				60	
basin- $\alpha$	-	-	19, 25, 26 28, 38, 42,	-	-
			44, 52, 56		
Misprediction	-	33 has fallen in basin-63	-	15 has fallen in basin-0	-

TABLE VII. DESIGN ANALYSIS REPORT WITH CA< 232 184 184 184 184 184 >

TABLE VIII. COMPARATIVE STATE ANALYSIS REPORT

Types of Basin	basi	in-0	basi	in-1	basi	nα
Rules	232 & 184	232 & 226	232 & 184	232 & 226	232 & 184	232 & 226
States	0, 1, 2, 3, 4, 5,	0, 1, 2, 3, 4, 5, 6,	23, 25, 27, 29,	7, 11, 15, 23, 27,	19, 25, 26,	19, 25, 35,
	6, 7, 8, 9, 10, 11,	8, 9, 10, 12, 13,	30, 31, 33, 35,37,	29, 31, 38, 39,	28, 38, 42,	37, 41, 42,
	12, 13, 14, 15,	14, 16, 17, 18,	39, 41, 43, 45,	43, 45, 46, 47,	44, 52, 56	44, 50, 52
	16, 17, 18, 19,	20, 22, 24, 26,	46, 47, 49, 50,	51, 53, 54, 55,		
	20, 22, 24, 32,	28, 30, 32, 33,	51, 53, 54, 55,	56, 57, 58, 59,		
	34, 36, 40, 48	34,36, 40, 48	57, 58, 59, 60,	60, 61, 62, 63		
			61, 62, 63			
Cycles	One single length	One single length	One single length	One single length	$21 \rightarrow 42 \rightarrow$	$21 \rightarrow 42 \rightarrow$
	loop $0 \rightarrow 0$	loop $0 \rightarrow 0$	loop 63→63	loop 63→63	21	21
Misprediction	15(001111) as it	30(011110) as it	33(100001) as it	48 (110000) as it	No unpre-	No unpre-
	falls on '0' basin	falls on '0' basin	falls on '1' basin	falls on '1' basin	dictable	dictable
	having greater	having greater	having less num-	having less num-	states	states
	number of 1s	number of 1s	ber of 1s	ber of 1s		
Depth of CA	9	11	9	11	9	11

Efficiency of wear leveling scheme is a function of size of the remapping zone [8] which is calculated in terms of number of contiguous memory blocks of remapping zone. Here, the size is three taking central block, left and right neighbouring block. The final stage is a 3-cell uniform CA which decides the remapping candidates. To keep minimum size of the zone, only three memory blocks are considered from the write dominated zone which is identified in final stage selected from the first stage. Final stage is executed in a single clock cycle as shown in Figure 15 of STD of 3-cell Uniform PBCA < 232 232 232>. But using two-stage hierarchical operation may increase design complexity of memory controller in terms of computation and space overhead.

Remapping method can be well explained with the help of Table IX. RL and RG are defined as local and global remapping methods respectively to fulfill the requirement of wear leveling in ReRAM. Three different sized memory 256 B, 512 B and 1024 B are considered here with 16, 32 and 16 number of sets. Remapping parameters are blockoffset  $(TB_0)$  and set-index  $(TS_i)$  which are defined over local (RL) and global (RG) methods. Source set index  $(SS_i)$  and source block offset  $(SB_0)$  are varied accordingly to find the target block address for different source blocks. Algebraic remapping method is therefore accomplished in between intraset and interset remapping to reduce write-stress on memory blocks to improve the durability of memory cells.

#### VIII. CONCLUSION AND FUTURE WORK

In this paper, we have proposed a design frame work for a typical wear leveling scheme which is intended to apply on resistive memory using periodic boundary one dimentional two states cellular automata (CA). Write distribution on memory blocks are tried to be kept uniform by remapping of intended write request within shared LLC of chip multiprocessors (CMPs). This scheme can improve cell lifetime by local/global wear leveling techniques though it incurs a hardware overhead of the design. This work addresses wear leveling due to repetitive writes in resistive memory caused by the spatial locality of reference. But write access pattern not only shows spatial locality of access, it also shows the spatial correlation among the accessed blocks. It is due to the reason of data storage pattern (data structure). Therefore, the wear leveling can also be considered for spatially correlated memory blocks by observing the data storage patterns.

Here, in our proposed wear leveling scheme for resistive memory, uneven or non-uniformity of writes due to workload distribution of chip multiprocessors are considered as the reason of repetitive writes in memory. It is not addressing write-stress caused due to malicious attacks. Therefore, this periodic boundary cellular automata based technique can be

Туре		Memory			Remapping parameter			Source			Target			Target address		
RL	RG	$M_{256}$	$M_{512}$	$M_{1024}$	$n_{256}$	$n_{512}$	$n_{1024}$	$SS_i$	$SS_i$	$SS_i$	$TS_i$	$TS_i$	$TS_i$	$T_{256}$	$T_{512}$	$T_{1024}$
		&	&	&	or	or	or	&	&	&	&	&	&			
		$S_{16}$	$S_{32}$	$S_{16}$	$j_{256}$	$j_{512}$	$j_{1024}$	$SB_o$	$SB_o$	$SB_o$	$TB_o$	$TB_o$	$TB_o$			
	-	17	39	97	$1 \rightarrow 5$	$7 \rightarrow 6$	$6 \rightarrow 7$	1,1	7,1	1,6	5,1	6,1	5,6	21	199	113
-		17	39	97	$1 \rightarrow 5$	$1 \rightarrow 6$	$6 \rightarrow 7$	1,1	7,1	1,6	1,5	7,6	1,7	81	38	101
	-	65	69	101	$4 \rightarrow 6$	$2 \rightarrow 6$	$6 \rightarrow 8$	1,4	5,2	5,6	1,6	5,6	5,8	97	197	133
-		65	69	101	$1 \rightarrow 6$	$5 \rightarrow 6$	$5 \rightarrow 10$	6,4	5,2	5,6	1,6	5,6	10,6	70	70	106
	-	215	508	1021	$13 \rightarrow 5$	$15 \rightarrow 6$	$16 \rightarrow 9$	7,13	28,15	13,16	7,5	5,6	13,9	87	220	580
-		215	508	1021	$7 \rightarrow 2$	$28 \rightarrow$	$13 \rightarrow 7$	7,13	28,15	13,16	2,13	19,15	7,16	210	499	1015
						19										
$\checkmark$	-	107	436	735	$6 \rightarrow 1$	$13 \rightarrow 3$	$45 \rightarrow$	11,6	20,13	15,45	11,1	20,3	15,15	27	116	255
							15									
-		153	364	735	$9 \rightarrow 2$	$12 \rightarrow 4$	$15 \rightarrow 9$	9,9	12,11	15,45	2,9	4,11	9,45	41	356	729

TABLE IX. TABULAR REPRESENTATION OF REMAPPING METHOD

extended for prevention of malicious attacks by capturing temporal as well spatial access patterns.

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