

# A Nonlinear C-UPFC Control Design for Power Transmission Line Applications

H.Ghane , S.K.Y.Nikravesh

**Abstract**— The C-UPFC is an elegant FACTS device and consists of three voltage source inverters (VSI) with common DC link. One of the converters is connected in parallel at the midpoint of line and the other two converters are connected in series. This paper deals with design and evaluation of a novel nonlinear control scheme based on input output feedback linearization technique for improving power transmission line dynamics. The simulation results indicate that with proposed nonlinear control, the C-UPFC is capable of independently controlling the active and reactive power flows at the both ends of line and the magnitude of AC voltage at line mid point. Simultaneously keep the DC link voltage at constant value.

**Index Terms**— FACTS, Nonlinear Control, C-UPFC, Feedback Linearization

## I. INTRODUCTION

The increasing demand for electric power requires to increase the transmission capabilities. Under de-regulation, however, electric utilities are reluctant to build new transmission line for economic and environmental consideration. The system is operated in ways, which lead to maximum use of existing transmission facilities, and this is not achievable unless new devices are installed on the transmission line to ensure proper performance of power system [1-3]. In recent years, the advances in power electronics have led to the development of the Flexible AC transmission system (FACTS). FACTS is designed to enhance power system capability and its dynamic by using reliable and high speed electronic devices. In these devices, with the help of high power GTO devices, the cumbersome rotating synchronous condenser can be replaced by the solid-state synchronous voltage source (SVS) in power transmission applications. The SVS is similar to an ideal synchronous machine in which a balanced three-phase sinusoidal voltage, with controllable magnitude and phase angle, is generated at the desired fundamental frequency. When connected in shunt or in series with a transmission line, the SVS can internally generate inductive and capacitive reactive power. It can also generate or absorb real power if a real power source is connected at the dc-link.[4]-[5].

The UPFC is the most elegant device of FACTS controllers. Two back-to-back connected SVS systems with one SVS connected in shunt and the other in series with the transmission line produces what is known as a unified power flow controller (UPFC). The power circuit of a UPFC, (see Fig.1), is composed of an excitation transformer (ET), a boosting transformer (BT), Two three phase GTO based voltage source converters (VSC), and a DC link capacitor. It is clear that  $m_E, m_B, \delta_E, \delta_B$  (the amplitude modulation ratios and phase angles of corresponding sources) act as the input control signals for UPFC [6]-[10].

In this topology, by using mentioned four control variables, it is possible to control the line active power flow, sending or receiving end reactive power and shunt converter AC bus voltage. Because of the limited number of control variables, the ordinary UPFC is not capable of controlling more than four variables in power transmission system, simultaneously. To overcome this problem, a new topology of UPFC has been developed in [11] and [12]. This new FACTS device is named center node UPFC (C-UPFC) installed at the midpoint of transmission line as shown in Fig. 2.

Since C-UPFC is a new developed configuration of UPFC, the researches and control schemes designed for it are limited. It was first introduced in [11], with tow separate DC links, (one for shunt VSC and one for tow series VSCs), after that, [12] improve its configuration with using one DC link for all three VSCs. But just linear PI controllers are investigated and its scope is limited to steady state analysis. The last published paper about C-UPFC performance is [13] which investigate C-UPFC's transient model in transmission line and like previous papers linear control is applied in it. In this paper after state space modeling of C-UPFC in transmission line, nonlinear controller based on input-output feedback linearization, will be designed to ensure that under all operating conditions the performance of our controller is guaranteed. Indeed the superior capabilities of this device will be discussed. It will be shown that this device can control the active and reactive powers of sending and receiving ends and simultaneously can regulate the midpoint voltage magnitude and DC link voltage.

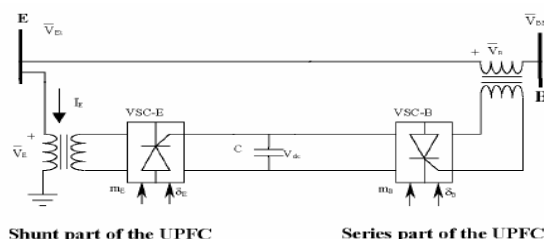


Fig. 1: General configuration of UPFC

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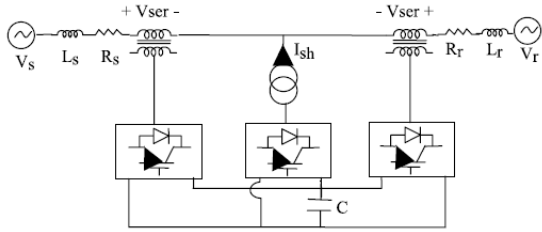


Fig. 2. General configuration of C-UPFC

At the first the dynamic equations of transmission system including the C-UPFC will be derived and state space modeling will be presented. Section two consists of some manipulations on state space equations. Then outputs of interest described in terms of state variables. At the next section the input-output feedback linearization technique will be briefly described and then applied on the proposed system. This section is followed by the proof of exponential convergence of outputs to their reference values. And finally in the last section, results of simulations will be compared with existing published researches and advantages of presented nonlinear MIMO controller over so far used controllers for C-UPFC will be clarified.

## II. SYSTEM DYNAMIC

Fig.3 shows the transient model of C-UPFC in transmission line [13]. In which, the  $L_{sh}$ ,  $L_{sr\_s}$ ,  $L_{sr\_r}$  and  $R_{sh}$ ,  $R_{sr\_s}$ ,  $R_{sr\_r}$  represent leakage inductances of transformers and losses of inverters and transformers. By writing Kirchhoff's Voltage Law for three converters and transformation of resulting equations into d-q frame, three pair of differential equations are obtained which can be used as part of state space modeling as below;

$$\begin{aligned}
 L_{sr\_s} \begin{bmatrix} \frac{d}{dt} I_{sr\_sd} \\ \frac{d}{dt} I_{sr\_sq} \end{bmatrix} &= \begin{bmatrix} -N_{sr\_s} E_{sd} - R_{sr\_s} I_{sr\_sd} - V_{sr\_sd} + \omega L_{sr\_s} I_{sr\_sd} \\ -N_{sr\_s} E_{sq} - R_{sr\_s} I_{sr\_sq} - V_{sr\_sq} - \omega L_{sr\_s} I_{sr\_sq} \end{bmatrix} \\
 L_{sr\_r} \begin{bmatrix} \frac{d}{dt} I_{sr\_rd} \\ \frac{d}{dt} I_{sr\_rq} \end{bmatrix} &= \begin{bmatrix} -N_{sr\_r} E_{rd} - R_{sr\_r} I_{sr\_rd} - V_{sr\_rd} + \omega L_{sr\_r} I_{sr\_rd} \\ -N_{sr\_r} E_{rq} - R_{sr\_r} I_{sr\_rq} - V_{sr\_rq} - \omega L_{sr\_r} I_{sr\_rd} \end{bmatrix} \\
 L_{sh} \begin{bmatrix} \frac{d}{dt} I_{shd} \\ \frac{d}{dt} I_{shq} \end{bmatrix} &= \begin{bmatrix} -N_{sh} V_{md} + R_{sh} I_{shd} + V_{shd} + \omega L_{sh} I_{shq} \\ -N_{sh} E_{rq} - R_{sh} I_{shq} + V_{shq} - \omega L_{sh} I_{shd} \end{bmatrix} \quad (1)
 \end{aligned}$$

In which  $N_{sr\_s}$ ,  $N_{sr\_r}$ ,  $N_{sh}$  represent the transformer ratio of three VSCs. The output voltages of three VSCs are appeared in the above relations. Based on [14] with some modification, It is possible to describe the output voltage of every VSC in terms of its control input as below;

$$\begin{cases} V_{id} = \frac{1}{2} m_i V_{dc} \cos \delta_i \\ V_{iq} = \frac{1}{2} m_i V_{dc} \sin \delta_i \end{cases}, \quad i = sr\_s, sh, sr\_r \quad (2)$$

Now the dynamic of DC link voltage must be calculated. According to [14], its dynamic is obtained with some modification to include the third series converter. Anyway

after transforming into d-q frame, the DC link voltage dynamic is obtained as below [14];

$$\begin{aligned}
 \frac{d}{dt} V_{DC} &= -\left(\frac{3}{2} \frac{1}{2C} m_{sh}\right) \begin{bmatrix} \cos \delta_{sh} & \sin \delta_{sh} \end{bmatrix} \begin{bmatrix} I_{shd} \\ I_{shq} \end{bmatrix} \\
 &+ \left(\frac{3}{2} \frac{1}{2C} m_{sr\_s}\right) \begin{bmatrix} \cos \delta_{sr\_s} & \sin \delta_{sr\_s} \end{bmatrix} \begin{bmatrix} I_{sr\_sd} \\ I_{sr\_sq} \end{bmatrix} \\
 &+ \left(\frac{3}{2} \frac{1}{2C} m_{sr\_r}\right) \begin{bmatrix} \cos \delta_{sr\_r} & \sin \delta_{sr\_r} \end{bmatrix} \begin{bmatrix} I_{sr\_rd} \\ I_{sr\_rq} \end{bmatrix} \quad (3)
 \end{aligned}$$

As stated earlier, in the C-UPFC control scheme, ac-bus voltage  $V_m$  control is one of our final objectives.

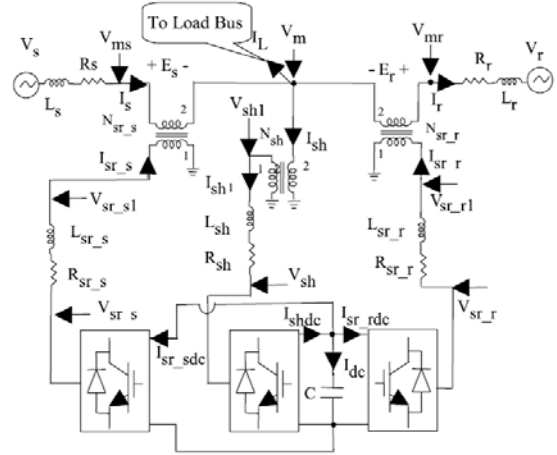


Fig.3. Transient model of C-UPFC

It is noticeable that in the presented control strategy it is assumed that  $V_m$  is aligned with the d-axes of mentioned d-q frame. In addition the variation of load current is supposed to be negligible and voltage sources have constant values. With this assumptions, the dynamic equation for  $V_m$  is obtained as follows with reference to Fig.3.

$$\begin{aligned}
 V_m &= V_{sd} - R_s (I_{shd} + I_{rd} + I_{ld}) - L_s \omega (I_{shq} + I_{rq} + I_{lq}) \quad (4) \\
 \dot{V}_m &= -R_s \left( N_{sh} \frac{d}{dt} I_{shd} + N_{sr\_r} \frac{d}{dt} I_{sr\_rd} \right) \\
 &\quad - L_s \omega \left( N_{sh} \frac{d}{dt} I_{shq} + N_{sr\_r} \frac{d}{dt} I_{sr\_rq} \right) \quad (5)
 \end{aligned}$$

## III. STATE SPACE MODELING

After rearrangement of equations (1), (3), and (5) and taking the ac currents of VCSs, DC link voltage, and ac bus voltage as state variables, the complete state space model is expressed as follows;

$$\dot{x} = F(x) + \bar{B}(x, \hat{u}) \quad (6)$$

In which;

$$\begin{aligned}
 x &= \begin{bmatrix} I_{shd} & I_{shq} & I_{sr\_sd} & I_{sr\_sq} & I_{sr\_rd} & I_{sr\_rq} & V_{dc} & V_m \end{bmatrix}^T \\
 \hat{u} &= \begin{bmatrix} m_{sh} & \delta_{sh} & m_{sr\_s} & \delta_{sr\_s} & m_{sr\_r} & \delta_{sr\_r} \end{bmatrix}^T
 \end{aligned}$$

And;

$$\text{By taking } K_i = \frac{N_i}{L_i} \text{ and } T_i = \frac{R_i}{L_i} \text{ which } i = sr\_s, sh, sr\_r$$

$$F(x) = \begin{bmatrix} -T_{sh}x_1 - \omega x_2 + K_{sh}x_8 \\ \omega x_1 - T_{sh}x_2 \\ \frac{1}{(1 + K_{sr\_s}N_{sr\_s}L_s)} [(K_{sr\_s}N_{sr\_s}R_s - T_{sr\_s})x_3 + (K_{sr\_s}N_{sr\_s}L_s\omega - \omega)x_4 + K_{sr\_s}x_8 - K_{sr\_s}V_{sd}] \\ \frac{1}{(1 + K_{sr\_s}N_{sr\_s}L_s)} [(\omega - K_{sr\_s}N_{sr\_s}L_s\omega)x_3 + (K_{sr\_s}N_{sr\_s}R_s - T_{sr\_s})x_4 - K_{sr\_s}V_{sq}] \\ \frac{1}{(1 + K_{sr\_r}N_{sr\_r}L_r)} [(K_{sr\_r}N_{sr\_r}R_r - T_{sr\_r})x_5 + (K_{sr\_r}N_{sr\_r}L_r\omega - \omega)x_6 + K_{sr\_r}x_8 - K_{sr\_r}V_{rd}] \\ \frac{1}{(1 + K_{sr\_r}N_{sr\_r}L_r)} [(\omega - K_{sr\_r}N_{sr\_r}L_r\omega)x_5 + (K_{sr\_r}N_{sr\_r}R_r - T_{sr\_r})x_6 - K_{sr\_r}V_{rq}] \\ 0 \\ -R_sN_{sr\_s}f_3(x) - L_s\omega N_{sr\_s}f_4(x) \end{bmatrix} = \begin{bmatrix} f_1(x) \\ f_2(x) \\ f_3(x) \\ f_4(x) \\ f_5(x) \\ f_6(x) \\ f_7(x) \\ f_8(x) \end{bmatrix}$$

It is obvious that the state space model is non-affine. Because it is much more comfortable to deal with an affine model, with some modification on inputs the system can be presented in an affine model as follows;

$$\begin{aligned} u_1 &= m_{sh}K_{sh}Cos\delta_{sh} & u_5 &= m_{sr\_r}K_{sr\_r}Cos\delta_{sr\_r} \\ u_2 &= m_{sh}K_{sh}Sin\delta_{sh} & u_6 &= m_{sr\_r}K_{sr\_r}Sin\delta_{sr\_r} \\ u_3 &= m_{sr\_s}K_{sr\_s}Cos\delta_{sr\_s} \\ u_4 &= m_{sr\_s}K_{sr\_s}Sin\delta_{sr\_s} \end{aligned} \quad (7)$$

Thus by using above transformation, the resulting affine model is as below;

$$\dot{x} = F(x) + B(x)u \quad (8)$$

In which  $B(x)$  is a  $8 \times 6$  matrix whose nonzero elements are listed below;

$$\begin{aligned} B(x)_{11} &= B(x)_{22} = \frac{-x_7}{L_{sh}} \\ B(x)_{33} &= B(x)_{44} = \frac{-x_7}{L_{sr\_s}(1 + K_{sr\_s}N_{sr\_s}L_s)} \\ B(x)_{55} &= B(x)_{66} = \frac{-x_7}{L_{sr\_r}(1 + K_{sr\_r}N_{sr\_r}L_r)} \\ B(x)_{71} &= \frac{3}{2C}x_1, B(x)_{72} = \frac{3}{2C}x_2, B(x)_{73} = \frac{3}{2C}x_3 \\ B(x)_{74} &= \frac{3}{2C}x_4, B(x)_{75} = \frac{3}{2C}x_5, B(x)_{76} = \frac{3}{2C}x_6 \\ B(x)_{83} &= \frac{R_sN_{sr\_s}}{L_{sr\_s}(1 + K_{sr\_s}N_{sr\_s}L_s)}x_7 \\ B(x)_{84} &= \frac{\omega L_sN_{sr\_s}}{L_{sr\_s}(1 + K_{sr\_s}N_{sr\_s}L_s)}x_7 \end{aligned} \quad (9)$$

In this step by using the important advantage of C-UPFC which is the ability of controlling more than four outputs,

the six objectives of proposed control scheme are specified. They include sending and receiving active and reactive power, midpoint ac voltage and DC link voltage. Thus output vector is established as follows;

$$y = [P_s \quad Q_s \quad P_r \quad Q_r \quad V_m \quad V_{dc}]^T \quad (10)$$

In the following by writing outputs in terms of state variables, the state space modeling is completed.

$$y = h(x) = \begin{bmatrix} \frac{3}{2}N_{sr\_s}(V_{sd}x_3 + V_{sq}x_4) \\ \frac{3}{2}N_{sr\_s}(V_{sd}x_4 - V_{sq}x_3) \\ \frac{3}{2}N_{sr\_r}(V_{rd}x_5 + V_{rq}x_6) \\ \frac{3}{2}N_{sr\_r}(V_{rd}x_6 - V_{rq}x_5) \\ x_8 \\ x_7 \end{bmatrix} \quad (11)$$

And hereby the complete state space model is ready to apply the proposed nonlinear control on it in the next section.

#### IV. NONLINEAR CONTROL DESIGN

##### A. A brief review of feedback linearization Scheme

A brief review of nonlinear control using feedback linearization is presented here. Without loss of generality, the following MIMO (multi input and multi output) system is considered.

$$\begin{aligned} \dot{x} &= f(x) + b(x)u \\ y &= h(x) \end{aligned} \quad (12)$$

Where  $x$  is a  $n$  dimensional state vector,  $u (\in \mathbb{R}^l)$  represents the Control inputs,  $y$  stands for  $l$  dimensional output vector,  $f$  and  $b$  are smooth vector fields, and  $h$  is a smooth scalar function. The input-output linearization of the above MIMO system is achieved by differentiating  $y$  of the

system until the inputs appear explicitly. Thus, by differentiating Eq. (11),

$$\dot{y}_i = L_f h_i + \sum_{j=1}^m (L_{b_j} h_i) u_j \quad , \quad i = 1, \dots, l \quad (13)$$

Where  $L_f h$  and  $L_{b_j} h$  represent the Lie derivatives of  $h(x)$  with respect to  $f(x)$  and  $b(x)$ ; respectively. The key point is that, if  $L_{b_j} L_f^{(r_i-1)} h_i(x) = 0$  for all  $j$ ; then the inputs do not appear in (10) and further differentiation is to be repeated as

$$y_i^{(r_i)} = L_f^{(r_i)} h_i + \sum_{j=1}^l (L_{b_j} L_f^{(r_i-1)} h_i) u_j \quad , \quad i = 1, \dots, l \quad (14)$$

Such that  $L_{b_j} L_f^{(r_i-1)} h_i \neq 0$  for at least one  $j$  and in this step  $r_i$  is defined as relative degree of  $i$ th output. This procedure is repeated for each output  $y_i$ . Thus, there will be a set of  $l$  equations given by

$$\begin{bmatrix} y_1^{(r_1)} \\ \vdots \\ y_l^{(r_l)} \end{bmatrix} = L(x) + M(x) \begin{bmatrix} u_1 \\ \vdots \\ u_l \end{bmatrix} \quad (15)$$

Where  $M(x)$  and  $L(x)$  are expressed by

$$M(x) = \begin{bmatrix} L_{b_1} L_f^{r_1-1} h_1 & \dots & L_{b_l} L_f^{r_1-1} h_1 \\ \vdots & \dots & \vdots \\ L_{b_1} L_f^{r_l-1} h_l & \dots & L_{b_l} L_f^{r_l-1} h_l \end{bmatrix} \quad (16)$$

$$L(x) = \begin{bmatrix} L_f^{r_1} h_1(x) \\ \vdots \\ L_f^{r_l} h_l(x) \end{bmatrix} \quad (17)$$

$M(x)$  is called as the decoupling matrix for the MIMO system. If  $M(x)$  is nonsingular, then the control  $u$  can be obtained as:

$$u = \begin{bmatrix} u_1 \\ \vdots \\ u_l \end{bmatrix} = -M^{-1}(x)L(x) + M^{-1}(x) \begin{bmatrix} v_1 \\ \vdots \\ v_l \end{bmatrix} \quad (18)$$

Where  $[v_1 \dots v_l]^T$  is the new set of inputs defined by the designer. The resultant dynamics of the system with new control is easily obtained by substitution of Eq. (18) into Eq. (15) and is given by

$$\begin{bmatrix} y_1^{(r_1)} \\ \vdots \\ y_l^{(r_l)} \end{bmatrix} = \begin{bmatrix} v_1 \\ \vdots \\ v_l \end{bmatrix} \quad (19)$$

It is readily noticed that the input-output relation in Eq.(19) is decoupled and linear. Thus linear control scheme can be used to control the linearized system.

### B. C-UPFC Nonlinear Control Design

For applying input output feedback linearization scheme on the resultant system in the section III, it is needed to differentiate from outputs as described above.

$$\dot{y} = L(x) + M(x)u \quad (20)$$

In which  $L(x)$  and  $M(x)$  are  $6 \times 1$  and  $6 \times 6$  matrixes which their elements are described as below; The six elements of  $L(x)$  are:

$$\begin{aligned} L_1(x) &= \frac{3}{2} N_{sr-s} [V_{sd} f_3(x) + V_{sq} f_4(x)] \\ L_2(x) &= \frac{3}{2} N_{sr-s} [V_{sd} f_4(x) - V_{sq} f_3(x)] \\ L_3(x) &= \frac{3}{2} N_{sr-r} [V_{rd} f_5(x) + V_{rq} f_6(x)] \\ L_4(x) &= \frac{3}{2} N_{sr-r} [V_{rd} f_6(x) - V_{rq} f_5(x)] \\ L_5(x) &= f_8(x) \\ L_6(x) &= f_7(x) = 0 \end{aligned} \quad (21)$$

And the nonzero elements of  $M(x)$  are:

$$\begin{aligned} M_{13}(x) &= -\frac{3}{2} N_{sr-s} \frac{V_{sd} x_7}{L_{sr-s} (1 + K_{sr-s} N_{sr-s} L_s)} \\ M_{14}(x) &= -\frac{3}{2} N_{sr-s} \frac{V_{sq} x_7}{L_{sr-s} (1 + K_{sr-s} N_{sr-s} L_s)} \\ M_{23}(x) &= \frac{3}{2} N_{sr-s} \frac{V_{sq} x_7}{L_{sr-s} (1 + K_{sr-s} N_{sr-s} L_s)} \\ M_{23}(x) &= -\frac{3}{2} N_{sr-s} \frac{V_{sd} x_7}{L_{sr-s} (1 + K_{sr-s} N_{sr-s} L_s)} \\ M_{35}(x) &= -\frac{3}{2} N_{sr-r} \frac{V_{rd} x_7}{L_{sr-r} (1 + K_{sr-r} N_{sr-r} L_r)} \\ M_{36}(x) &= -\frac{3}{2} N_{sr-r} \frac{V_{rq} x_7}{L_{sr-r} (1 + K_{sr-r} N_{sr-r} L_r)} \\ M_{45}(x) &= \frac{3}{2} N_{sr-r} \frac{V_{rq} x_7}{L_{sr-r} (1 + K_{sr-r} N_{sr-r} L_r)} \\ M_{46}(x) &= -\frac{3}{2} N_{sr-r} \frac{V_{rd} x_7}{L_{sr-r} (1 + K_{sr-r} N_{sr-r} L_r)} \\ M_{53}(x) &= B_{83}(x) \quad , \quad M_{53}(x) = B_{84}(x) \\ M_6(x) &= \frac{3}{2C} [x_1 \quad x_2 \quad x_3 \quad x_4 \quad x_5 \quad x_6] \end{aligned} \quad (22)$$

In which  $M_6(x)$  represents the sixth row of  $M(x)$ .

It is readily specified from Eq.(20) that the relative degree of all outputs is one. Now it is just remained to obtain nonlinear control through input output feedback linearization as below;

$$u = M^{-1}(x)(v - L(x)) \quad (23)$$

By applying Eq.(23) in Eq.(20) the resultant linear relation between input and output vector is generated as follows;

$$\dot{y} = v \quad (24)$$

In which  $v$ , is the new input vector and is determined such that exponentially convergence of error signals to zero is guaranteed. To achieve this goal,  $v$  is defined as

$$v = (y_{ref} - y) = e + \dot{y}_{ref} \quad (25)$$

$$\dot{e} = \dot{y}_{ref} - \dot{y} \quad (26)$$

Substituting Eq.(25) and Eq.(25) in Eq.(24) lead to

$$e + \dot{e} = 0 \quad (27)$$

It is clear that the error signal,  $e$ , is exponentially convergent to zero. Even it is possible to increase the convergence rate of error by some modification applied on  $v$  as bellow;

$$v = (y_{ref} - y) = Ke + \dot{y}_{ref} \quad (28)$$

That leads to

$$e + K\dot{e} = 0 \quad (29)$$

In which  $K$  is a proportional matrix gain and is determined by assigning desired poles on the left-half s-plane. Thus, asymptotic tracking control to the reference with the desired convergence rate can be achieved.

At the next section the simulation results are compared with just linear controller and the superior advantages of nonlinear control like as fast and exponentially convergence of outputs even in affront of fast changing reference values, are clarified.

### V. SIMULATION RESULTS

The proposed nonlinear control scheme for C-UPFC is evaluated by computer simulation in MATLAB/SIMULINK. The values of parameters used in simulations are listed below, in the tables. In Table.1 the machine parameters including nominal voltage and power, impedance and phase are illustrated.

Table1. Machines Parameters Value

Parameter Machine	V (KV)	MVA	R+jLw *(pu)	Phase (deg)
Machine 1 (Sending Side)	240	800	.0066+ j0.04	0
Machine 2 (Receiving Side)	240	800	.0066+ j0.04	-10

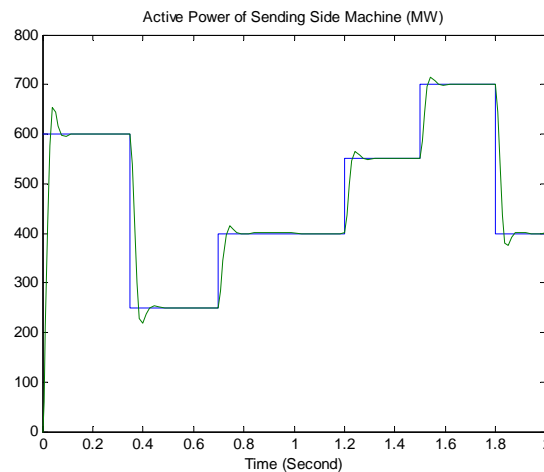
It is noticeable that in table.1, the line impedance is included in machine impedance in per unit.

In table.2, each VSC's parameters consisting of leakage inductance, resistor and turn ratio of corresponding transformer are illustrated. Also the capacitance,  $C$ , is set to 1250  $\mu F$  in simulations.

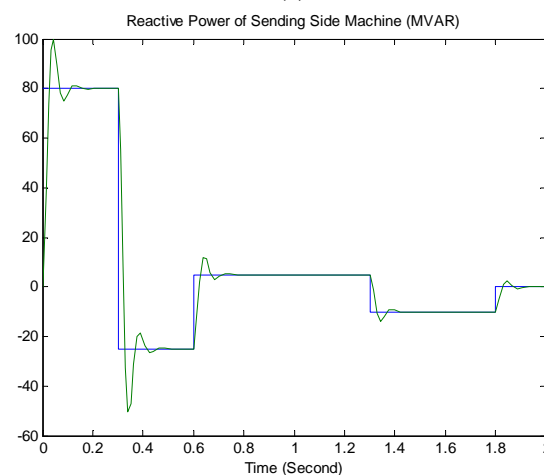
Table 2. Three VSC's Parameters Value

Parameters Machine	N (Trans. Ratio)	R (pu)	Lw (pu)
Series_s Converter	1000	0.015	0.15
Shunt Converter	0.001	0.04	0.12
Series_r Converter	1000	0.015	0.15

By simulating in SIMULINK the below results were achieved;



(a)



(b)

Fig. 4. Reference and actual values of sending machine active and reactive power

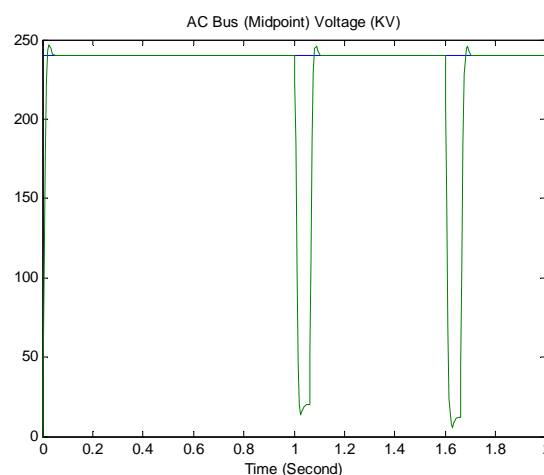


Fig. 5. Line midpoint ac voltage regulation

\* Sum of line and machine impedances

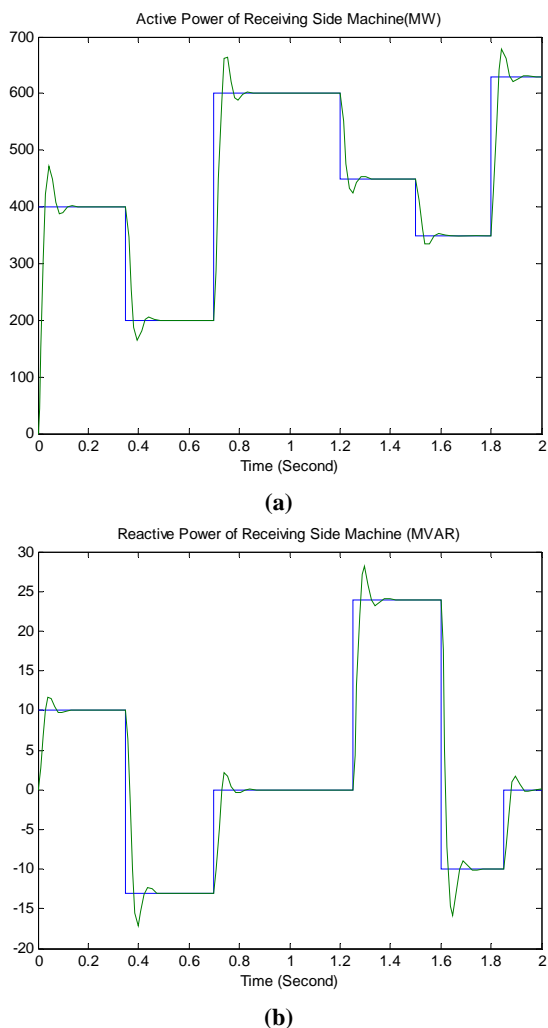


Fig. 6. . Reference and actual values of receiving machine active and reactive power

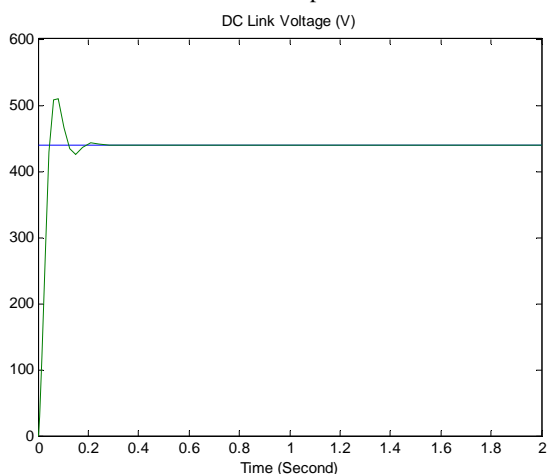


Fig. 7. AC link reference and actual voltage

Fig.4-7 illustrate superior performance of feedback linearization scheme in asymptotically tracking of reference signals. As is obvious in mentioned figures, each of outputs only needs a very short time (less than 0.2 second) to cope with the sudden change of their reference signal and settle on the reference values. In Fig 5. it is illustrated that even in worst case in which three phase ground fault is occurred, the proposed nonlinear control, have the powerful ability to compensate it almost as soon as the faulty condition vanishes. In other word, in the post fault condition the proposed nonlinear control scheme exhibits a superior

compensating function. At the last it is worth to say such a fast, and exponential convergent performance that in addition has a good transient response could never be achieved with any linear control. Meanwhile the independent operating point performance of the proposed nonlinear control is clearly illustrated in Fig. 5 in which a large disturbance terribly changes the operating condition of system.

## VI. CONCLUSION

In this paper the state space modeling and nonlinear control design of C-UPFC as an elegant FACTS device are presented. It was shown that with proposed nonlinear control scheme, independent of operating point, C-UPFC can easily regulate and compensate line active and reactive power flows and DC link and magnitude of load bus ac voltage especially in transient modes in which linear control have many problems. Meanwhile the superior capability of C-UPFC for control more than four variables in power line system as an advantage in compare with UPFC was clarified. It was shown in the simulations results that the proposed nonlinear MIMO controller with the help of state space modeling, considerably improve the dynamic of response and exhibit almost full tracking, even for step changing in the active and reactive power, in compare with past published researches on power transmission system including C-UPFC.

## REFERENCES

- [1] L. Gyugi, "A unified power flow control concept for flexible ac transmission systems", IEE Proc. Part C. 139 (4) 1992, 323-331
- [2] N. Mithulananthan, "Application of FACTS Controllers in Thailand Power Systems", RTG Budget-Joint Research Project, 2003. New York: Springer-Verlag, 1985, ch. 4.
- [3] Julia.j.black, "Flexible AC Transmission System Compensation on a Utility Transmission System", A Thesis for Degree of Master of science, University of Nevada, Las Vegas, December 1994
- [4] Hingorani N.G. and L. Gyugui, "Understanding FACTS", IEEE Press, New York, 2000.
- [5] M. Vilathgamuwa, X. Zhu, S.S. Choi, "A robust control method to Improve the performance of a unified power flow controller" Electric Power Systems Research 55 (2000) 103-111
- [6] Juan M.Ramirez , Ricardo J.Davalos , Abraham Valenzuela , Ixtlahuatl Coronado , "FACTS-Based Stabilizers Coordination" Trans.1995, pwr.10(2): 1085-109.
- [7] Gyugyi L. and C.D. Schauder, "The Unified Power Flow Controller: a New Approach to Power Transmission Control", IEEE Trans.1995, pwr.10(2): 1085-109.
- [8] A.j.Keri, A.A.Edris, "Unified Power Flow Controller: Modeling and Analysis", IEEE Trans, 1999
- [9] H.F.Wang, " A Unified Model for the Analysis of FACTS Devices in Damping Power System Oscillations Part I: Single-machine Infinite-bus Power Systems", IEEE Trans on Power Delivery, 1997
- [10] S.A. Taher, " Design of Robust UPFC Controller Using H<sub>∞</sub> Control Theory in Electric Power System "American Journal of Applied Sciences 5 (8): 980-989, 2008
- [11] Boon Teck Ooi, Bin Lu, "C-UPFC: A New FACTS Controller with 4 Degrees of Freedom", 0-7803-5692-6, 2000 IEEE
- [12] B. Ooi, B. Lu, "C-UPFC: A new FACTS Controller for Midpoint Sittng", Conf.Record of the Int. Power Electron.. Conf., April, 2000, Tokyo, Japan, pp. 1947- 1952
- [13] A. Ajami , S.H. Hosseini , S. Khanmohammadi , G.B. Gharehpetian "Modeling and Control of C-UPFC for Power System Transient Studies, Simulation Modeling Practice and Theory 14 (2006) (564-576)
- [14] Nabavi-Niakani. A., and Irvani. M.R, "Steady-State and Dynamic Models of Unified Power Flow Controller (UPFC) for Power System Studies", IEEE Trans., 1996, PWRW, pp.1937-1943
- [15] J.J.E.Slotine, "Applied Nonlinear Control", 1991 by Prentice Hall Inc, ISBN : 0-13-040890-5