Determining the Repairing Interval for the Means of Transportation with Regard the Unexpected Failures and Repairing Costs

Do Duc TUAN and Vo Trong CANG, *Members, IAENG*

Abstract: The paper presents the theoretical basis of the relationship between the parameter of the flow of irregular failures with working time $\omega(l)$, and the relationship between the number of converted unit repairs during one unit of working time $S(L)$. These relations will serve for the determination of the optimal repairing interval for the means of transportation with regard the unexpected failures and the costs for repair of their components.

Index Terms: Optimization, Repairing Interval, Unexpected Failures, Repairing Costs, Means of Transportation

I. THE FAILURE FLOW PARAMETER DURING THE WORKING TIME

The failure flow parameter changes during the time of work, as shown in Fig 1.1 [1]. This process can be divided into three stages:

Stage I - running clearance:

After the start of use or after the repair of equipments, their failure flow parameter increases sharply, and then will gradually decrease to a level determined. This characteristic of the relationship $\omega(l)$ is due to the quality of manufactured parts and details, the existence of hiden defects, the violations of technology when manufacturing or repairing.

Stage II-normal use:

This stage is characterized by the unchanged failure flow parameter. In this stage appear the extraordinary damages, which mainly occur due to random causes and are distributed relatively evenly during the working time. Failure flow parameter in this stage is determined by the characteristics and structural perfection of equipments, as well as the conditions and exploitation mode of equipments.

Stage III - increasing wear or aging:

The basic feature of this stage is the increasing failure flow parameter due to several factors, such as:

- The abrasion and aging of the parts and details lead to an increase in the probability that the pulse load exceeds the limit of their strength;

- The increase in the gap within the assemblied elements leads to the increase in the vibration, shock and momentum;

 -The occurrence of the excessive within the moveable joints leads to the decrease in their mechanical strength;

- The decrease in electrical resistance of electro-insulating materials.
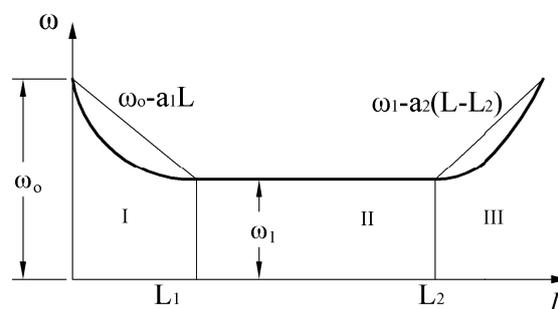
Figure 1.1. The change of the failure flow parameter during the working time

To prevent the failure of parts and weared details we set the preventive-planned repairing system, in which we undertook to restore or replace the details and components with the technical specs close to the critical values [6].

On the other hand, the establishment of the planned repair, which is before the stage of wear and aging with the increase in damages, is meaningless.

For example, the implementation of the planned repair at the time of L_1 (Fig. 1.2) is not only beneficial, but harmful. At this time the number of unscheduled repairs increases due to the occurrence of the damages of running clearance.

Vo Trong CANG, PhD, is a senior lecturer in the Faculty of Transportation Engineering, HoChiMinh city University of Technology (HCMUT), Vietnam National Univ. of HochiMinh city (VNU-HCM). He is associate researcher at the Digital Control and Systems Engineering (DCSE-lab) Key-Lab under the VNU-HCM (Tel: +84+ 903676591;
e-mail: votrongcang@gmail.com or vtcang@hcmut.edu.vn)

Do Duc TUAN, is a Professor at the Department of Locomotives and Wagons, Faculty of Mechanical Engineering, University of Transport and Communication (UTC), Hanoi, Vietnam.
(e-mail: ddtuan@utc.edu.vn)
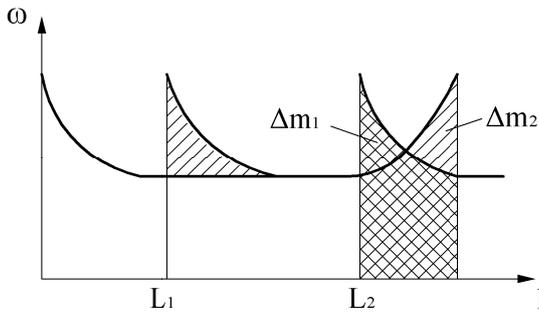
Figure 1.2. The change of the failure flow parameter in difference distances running to repair

Here, the scheduled repair is logical if it is made at the time of any L_2, where the number of damages Δm_2 is greater than the number of damages of running clearance Δm_1 (characterized by the growth of the failure flow parameter).

It is necessary to determine a reasonable time to conduct the planned repair, in which the total cost for conduct of repair (planned and unplanned) is minimal [2].

If at the planned repair we carry out the fully restore of the parts, i.e. the function $\omega(l)$ will be restored completely after repairs as had earlier, then during the long enough working time of the means, the relationship $\omega(l)$ will have the form as shown in Fig 1.3. Here, L, 2L, 3L ... correspond to the times of the planned repairs.
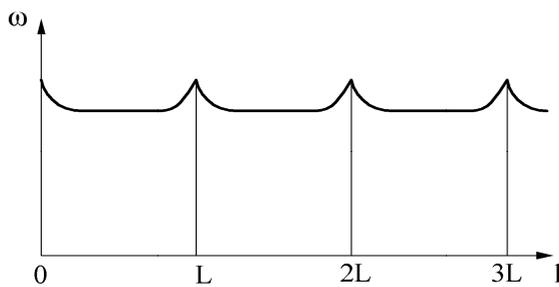
Figure 1.3. The change of the failure flow parameter within the intervals between repairs.

Because the relationships $\omega(l)$ in the intervals [0,L], [L,2L], [2L,3L] ... are completely the same, so just consider an interval [0, L] is sufficient.

The number of unscheduled repairs in the interval [0, L] is equivalent to the amount of damages:

$$H_{(l)} = \int_0^L \omega(l).\,dl \quad , \qquad (1.1)$$

Thus the average number of damages within the long enough working time l will be:

$$N_{DX} = H_{(l)} = \frac{l}{L} \int_0^L \omega(l).\,dl \quad , \qquad (1.2)$$

The number of times to repair N_{KH} planned in the interval $[0, l]$ is:

$$N_{KH} = \frac{l}{L} \quad , \qquad (1.3)$$

Let C_{KH} is the average cost for one planned repair, and C_{DX} is the average cost for one unscheduled repair considering the loss of the stopping of the means, then the

total cost for the conduct of both planned and unplanned (unscheduled) repairs in the interval [0, l] is:

$$C = C_{DX}\frac{l}{L} \int_0^L \omega(l).\,dl + C_{KH}\frac{l}{L} \quad , \qquad (1.4)$$

Upon dividing this expression for l, we obtain the average total cost for the repair:

$$q(L) = \frac{1}{L}\left[C_{DX.} \int_0^L \omega(l).\,dl + C_{KH} \right] , \qquad (1.5)$$

The quantity $q(L)$ is the optimum target of the interval between repairs of the elements of the means, and it is received from their failure information. To calculate the optimum target $q(L)$ by Eq. 1.5 we need to know the relationship of the failure flow parameter ω with working time l. In general form, this relationship can be approximated in high accuracy with the polynomial of n-th degree:

$$\omega(l) = \begin{cases} \omega_0 - a_1(l)^n & , \; l \le l_1 \\ \omega_1 & , \; l_1 < l \le l_2 \\ \omega_1 + a_2(l - l_2)^n & , \; l_2 < l \end{cases}$$

To simplify, this relationship can be approximated with the piecewise-linear method. This approximation can satisfy in the real situation [1, 2].

We assume that $(0, l_1)$ and (l_2, L) are small enough, the wear will intensively increase in the stages I and III, the function will be:

$$\omega(l) = \begin{cases} \omega_0 - a_1(l) & , \; 0 \le l \le l_1 \\ \omega_1 & , \; l_1 < l \le l_2 \\ \omega_1 + a_2(l - l_2) & , \; l_2 < l \end{cases}$$

In this case, the compolsary repair should be planned at the appropriate period uppon the severe wear - when the damage is increased rapidly, i.e. $L > l_2$. Then, the integral in Eq. 1.4 are splitted into three:

$$\int_0^L \omega(l).\,dl = \int_0^{l_1}(\omega_0 - a_1 l).\,dl + \int_{l_1}^{l_2} \omega_1.\,dl +$$

$$+ \int_{l_2}^L [\omega_1 + a_2(l - l_2)].\,dl$$

Upon transforming with $a_1 = \dfrac{\omega_0 - \omega_1}{l_1}$ we have

$$\int_0^L \omega(l).\,dl = \frac{a_1.l_1^2}{2} + \omega_1 L + \frac{a_2.(L-l_2)^2}{2} \quad , \qquad (1.6)$$

Upon replacing (1.6) into (1.5), we obtain

$$q(L) = C_{DX.}\omega_1 + \frac{a_2 C_{DX}(L-l_2)^2}{2L} +$$

$$+ \frac{\left(\frac{C_{DX}.a_1.l_1^2}{2} + C_{KH}\right)}{L} \quad , \qquad (1.7)$$

Indeed, the function $q(L)$ is a 2nd degree polynomial with one minimum point (see Fig. 1.4).

The second term $\dfrac{C_{DX}(L-l_2)^2}{2L}$ is positive increased with the distance between repairs L, while the third term

$\dfrac{\left(\dfrac{C_{DX}\cdot a_1\cdot l_1^2}{2}+C_{KH}\right)}{L}$ is negative; the term $C_{DX}\cdot\omega_1$ is constant within the full range of variable of the interval between repairs and it does not affect the horizontal position L_0 of the minimum point, but affects the release of $q(L_0)$.

$$\dfrac{a_2 C_{DX}(L-l_2)^2}{2L}$$

$$\left(\dfrac{a_1 C_{DX} l_1^2}{2}+C_{KH}\right)/L$$

$$C_{DX}\omega_1$$
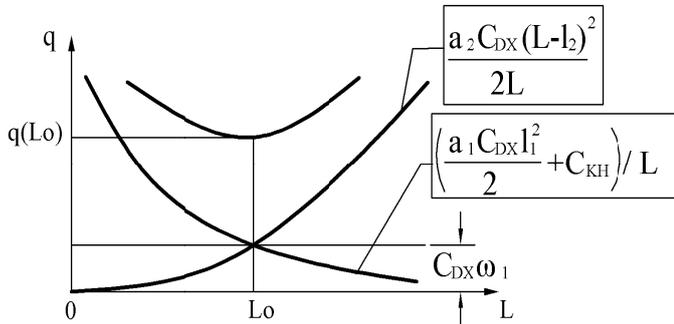
Figure 1.4. The Relationship between the total units cost with the interval between repairs

To determine the optimal interval between repairs we take the derivative of $q(L)$ and give it equal to 0:

$$q'(L)=\dfrac{a_2 C_{DX}(L^2-l_2^2)}{2L^2}-\dfrac{\dfrac{C_{DX}a_1 l_1^2}{2}+C_{KH}}{L^2}=0$$

Of which:

$$L_0=\sqrt{\dfrac{a_1 l_1^2}{a_2}+l_2^2+\dfrac{2C_{KH}}{a_2 C_{DX}}}\quad,\qquad(1.8)$$

From the expression (1.8) in particular, we found that planned repair should be conducted in the stage of increasing damages, as $L_0 > l_2$.

Also, when there is no damage specific to the wear and running clearance, i.e. when $a_1\to0$, $a_2\to0$, $\omega(l)\to\omega_1=$ const, the optimal interval between repairs $L_0\to\infty$, i.e. no need to carry out planned repairs, because it does not prevent the unexpected failures.

The unexpected failures affect the absolute value of the total unit cost for both the planned and unplanned (unscheduled) repairs.

This is seen from expression (1.5), because of which the $C_{DX}\omega_1$, where ω_1 is the value of failure flow parameter during the stage of normal use, in which the unexpected failures of the considered components are overwhelming.

However, the abscissa of the minimum point of the total unit cost does not depend on the value of ω_1, as shown in expression (1.8), but is determined mainly by the speed of the changes of the failure flow parameter within the stage of running clearance (a_1) and within the stage of the increasing wear or aging (a_2).

The time for running clearance l_1 depends greatly on the type of previous repair. So, there will not any information about that period, while the structure of the repair cycle is being determined.

In addition, the period of running clearance l_1 represents only a fraction of normal use period $[l_1, l_2]$, so we can ignore the first term in the expression (1.8).

Thus, the optimal interval between repairs is determined primarily by the time of the normal use period $[l_1, l_2]$ and depends on the relationship (ratio) of the cost of the planned repair C_{KH} and the cost of the unplanned repair (unscheduled) C_{DX}, as well as the speed of the increase in the failure flow parameter in the stage of increased wear or aging a_2, i.e. the intensity of these processes.

This intensity allows forecast the life of the components which are under wear and aging. Such the relationship of the failure flow parameter with the working time has been shown in several studies (e.g. [1, 2, 6]).

Featuring change of such failure flow parameter, its function can be expressed as straight lines:

$$\omega(l)=\begin{cases} a_1\,l+b_1 &, \quad 0\le l\le l_1; \\ a_2\,(l-l_1)+b_2 &, \quad l_1<l\le l_2; \\ a_3\,(l-l_1)+b_3 &, \quad l_2< l \end{cases}\qquad(1.9)$$

The expression of the function $\omega(l)$ consists of eight coefficients (a_1, a_2, a_3, l_1, l_2, b_1, b_2, b_3) and should determined by the ready empirical relationships $\omega^*(l)$, i.e. the graph of experimental failure flow parameter. However, there are several redundant factors, so due to the conditions of continuity of the function $\omega(l)$, we have the boundary equations as follows:

$$\omega_1(l_1)=\omega_2(l_1)\quad\text{and}\quad\omega_2(l_2)=\omega_3(l_2)$$

From this, we have:

$$b_2=a_1 l_1+b_1\ ;$$

$$b_3=a_2\,(l_2-l_1)+a_1\,l_1+b_1\ .$$

Finally, the function of the failure flow parameter has the form as:

$$\omega_1(l)=a_1\,l+b_1\ ,\qquad\qquad\qquad 0\le l\le l_1$$

$$\omega_2(l)=a_2(l-l_1)+a_1\,l_1+b_1\ ,\qquad l_1<l\le l_2$$

$$\omega_3(l)=a_3(l-l_2)+a_2(l_2-l_1)+a_1 l_1+b_1\ ,\qquad l_2< l,\quad(1.10)$$

Here, the expression of $\omega(l)$ consists only of six constants: a_1, a_2, a_3, b_1, l_1, l_2, but to define the problem we have to approximate the empirical chart of the experimental failure flow parameter $\omega^*(l)$ with the theoretical $\omega(l)$.

The approximation, (i.e. replacing the empirical function $\omega^*(l)$ with the theoretical $\omega(l)$,) in this case will give more accurate results, if the amount of damages, calculated in accordance $\omega^*(l)$ and $\omega(l)$ will have a minimum deviation, i.e. considering the requirements of the least squares method.

The objective function for the approximation of the failure flow parameter would be

$$y=\sum_{i=1}^{n}\left(s_i-s_i^*\right)^2\ ,\qquad(1.11)$$

of which:

S_i and S_i^*- the corresponding numbers of theoretic and empirical damages counted in the i-th interval of working time;

n - number of working time interval (i.e. the steps of the diagram).

The number of empirical damages S_i^* will determined by the rectangular area of the i-th interval of the $\omega^*(l)$ chart:

$$S_i^* = \omega_i \, \Delta_i^* l , \qquad (1.12)$$

Using piecewise-linear approximation the theoretic amount of damages S_i is determined by the trapezoidal area of l_{i-1}; $\omega(l_i - l); \, l_i$, i.e.

$$S_i = \omega(X_i) \, \Delta l \ , \qquad (1.13)$$

of which:

$\omega(X_i)$ - theoretical value of the function $\omega(l)$ at the midpoint (median) of the i-th interval;

Δl - the average line of the trapezoid.

Replacing (1.12) and (1.13) into (1.11), we get:

$$y = \sum_{i=1}^{n} [\omega(X_i)\Delta l - \omega_i^* \Delta l]^2 =$$

$$\Delta l^2 \sum_{i=1}^{n} [\omega(X_i) - \omega_i^*]^2, \qquad (1.14)$$

Because that Δl^2 is constant, the optimal condition of Eq. 1.14 is equivalent to the minimum objective function:

$$Z = \sum_{i=1}^{n} [\omega(X_i) - \omega_i^*]^2 \ \to min, \qquad (1.15)$$

Whereas, the graph approximation of the failure flow parameter is changed into the piecewise-linear approximation of the empirical function $\omega^*(l)$, which is given by n points coordinated of $(x_i; \omega_i^*)$, where x_i is the middle point of the i-th interval of the $\omega^*(l)$ chart;

ω_i^* - is the value of the failure flow parameter in the i-th interval

Replacing with (1.11), we can write the (1.15) as following:

$$Z = \sum_{X_i \leq l_1} A^2 + \sum_{l_1 < X_i \leq l_2} B^2 + \sum_{l_2 < X_i} C^2$$

where: A, B, C - the deviation of the failure flow parameter' function, compared with the corresponding empirical values, on the changing intervals of working time respectively:

A = $a_1 x_i + b_1 - \omega_1^*$;

B = $a_2 (x_i - l_1) + a_1 l_1 + b_1 - \omega_i^*$;

C = $a_3 (x_i - l_2) + a_2(l_2 - l_1) + a_1 l_1 + b_1 - \omega_i^*$

The objective function (1.15) depends on the parameters $a_1, a_2, a_3, l_1, l_2, b_1$, but note that l_1 and l_2 coincide with the boundaries of the range of the $\omega^*(l)$ graph, then their defining region is limited by the $l_1, l_2, ..., l_n$.

So to degrade the system of variables, we should fix the values of l_1 and l_2 and determine the local minimal of the objective function z. We should repeat the solution with different combinations of l_1 and l_2, etc. … then chose from all of the answers the solution that ensures the minimum value of the objective function. Thus, while fixed l_1 and l_2, the four variable function z=(a_1, a_2, a_3, b_1) is minimal.

II. DETERMINE THE OPTIMAL WORKING TIME

To treat the integral function of the failure flow parameter within Eq. 1.5, we insert one, two or three integral components depending on the type of the function $\omega(l)$ within [0, L]:

$$\sum_{0}^{L} \omega(l) \, dl = \int_0^{l_1} (a_1 l + b_1) \, dl +$$

$$+ \int_{l_1}^{l_2} [a_2(l - l_1) + b_2] dl +$$

$$+ \int_{l_2}^{L} [a_3(l - l_2) + b_3] dl$$

Uppon calculating the integral we obtain (2.1):

$$\int_0^L \omega(l) dl = 0.5 \, a_1 l_1^2 + b_1 l_1 +$$

$$+0.5 \, a_2 (l_2 - l_1)^2 + b_2(l_2 - l_1) +$$
$$+0.5 \, a_3 (L - l_2)^2 + b_3(L - l_2) \ , \qquad (2.1)$$

Replacing expressions of the coefficients b_2 and b_3 into (1.6), then

$$\int_0^L \omega(l) dl = 0.5 \, a_1 l_1^2 + b_1 l_1 +$$

$$+0.5 \, a_2 (l_2 - l_1)^2 + b_2(l_2 - l_1) +$$
$$+(a_1 l_1 - b_1)(l_2 - l_1) + 0.5 \, a_3 (L - l_2)^2 +$$
$$+[a_2(l_2 - l_1) + (a_1 \, l_1 + b_1)](L - l_2) \ , \qquad (2.2)$$

We replace (2.2) into (1.5), then take the derivative by L and give it equal to 0, we get the expression, which determine the optimal interval between repairs:

$$L_0 = \sqrt{\frac{[a_1 l_1^2 + a_2(l_2^2 - l_1^2)]}{- a_3} + l_2^2 + \frac{2.C_{KH}}{a_3 C_{DX}}} \ , \qquad (2.3)$$

Analysis of the expression (2.3) shows that the optimal interval between repairs depends significantly on the relationship of the costs for carrying out repairs planned C_{KH} and unplanned C_{DX}.

The planned repair cost includes the cost for materials or spare parts C_1, the cost for wages C_2 and the cost for stop of the means C_3, i.e.: $C_{KH} = C_1 + C_2 + C_3$.

The cost for unplanned repair, in addition to the stated quantities C_1, C_2 and C_3, also includes the cost C_4, which is caused by damage of the vehicle during operation, i.e.:

$$C_{DX} = C_1 + C_2 + C_3 + C_4.$$

Thus, $C_{DX} \geq C_{KH}$, and $C_{DX} = C_{KH}$ only happens to the elements, whose damages do not cause to the vehicle's loss during operation.

So far, still no formal studies on the determination of damage caused by the stop of the means halfway due to their failures. So if there were, they would not fully reflect the damages caused due to failures [5, 6, 7].

So, although the companies of transportation have information about the time to stop the means due to failures, it did not allow assessment of the C_4 within the unplanned repairing cost. Consequently, it can not compute the absolute value of the average total cost of the repairs.

However, using the relative values of C_{DX} and $C_{KH,}$ we can determine the optimal interval between repairs L_0, corresponding to the minimum value of the average total unit costs $q(L_0)$.

The ratio K of repair costs for planning and unplanned is:

$$K = \frac{c_{DX}}{c_{KH}}, \qquad (2.4)$$

Because $C_{DX} \geq C_{KH}$ then $K \geq 1$.

Performing C_{DX} by K and C_{KH}, then replace it into Eq. 1.5, we get:

$$q(L) = \frac{c_{KH}\left[K \int_0^L \omega(l)\,dl + 1\right]}{L}, \qquad (2.5)$$

On the physical sense, the quantity, located in the numerator of the fraction (2.5), is the total cost of both types of repairs. So, the expression in parentheses is the number of total converted repairs, i.e. the quantity $K \int_0^L \omega(l)\,dl$ turns the total number of unplanned repairs $\int_0^L \omega(l)\,dl$ into the cost-equivalent amount of planned repairs.
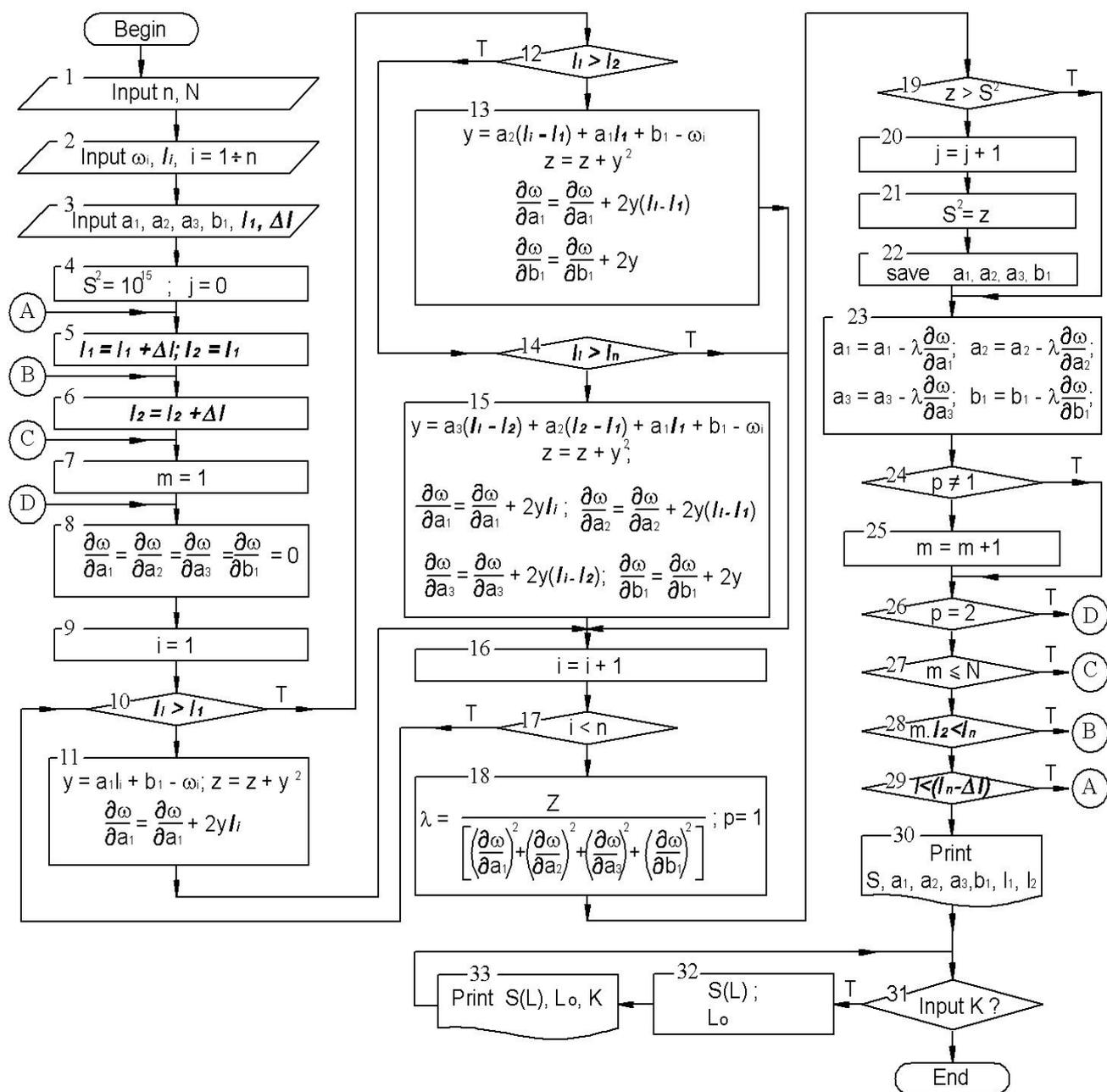
Figure 2.1. Algorithm for piecewise-linear approximation

The relationship *S(L)* is called the number of converted unit repairs during one unit of working time:

$$S(L) = \frac{\left[K \int_0^L \omega(l)dl + 1 \right]}{L} \quad , \qquad (2.6)$$

From the above theoretical basis, we set the algorithm for the approximation of the failure flow parameter, as shown in Fig 2.1.

Uppon enterring the number of values n – the amount of experimental data of the failure flow parameter (block 1), then assigning N - the number of repetitions of the coefficients until they were stable and the value of the objective function does not fall again .

Then, enter the experimental values of the failure flow parameter ω^*_i and the initial values of the coefficients $a_{1.1}$, $a_{2.1}$, $a_{3.1}$, $b_{1.1}$ of the failure flow parameter (in the blocks 2 and 3).

Given (in the block 4) the large initial values of the objective function, which later will be compared with the squared deviation of the theoretical from the experimental values of the failure flow parameter after the first calculation (in block 19).

Given (in the blocks 5 and 6) the initial boundary values l_1 and l_2 of the failure flow parameter and the initial calculating values; the variables used for the accumulation of totals are given by 0 (in the block 8).

Then we perform one cycle of counting to determine a_1, a_2, a_3, b_1 (through the blocks 9 to 17) and the value of the coefficient λ (block 18).

We remember the coefficients corresponding to the minimum value of the objective function z (through the blocks 19 to 22), and then calculate the new values of the coefficients a_1, a_2, a_3, b_1 (block 23).

The calculations by the "steepest descent method" should repeat (the blocks 24-27) until the total squared errors z will not decrease further during the N cycles.

Conduct one cycle of counting for all possible values of l_1 and l_2 (in the blocks 28 and 29). We send the calculated values of a_1, a_2, a_3, b_1 and the working times l_1, l_2 to the printer (block 30).

To calculate the value of the function S(L) by the coefficient *K*, we enter the value of *K* in the block 31; calculate the value of S(L) and L_0, in the block 32, and then print the L_0 The loop will proceed with all the input values of *K*. Finally, the program plots the graphs of S(L) and ends in the block 34.

Based on the theory mentioned, we can build the program for calculation of the function S(L), which denotes the relationship of the number of total converted unit repairs during the working time S(L) with the different values of K - the ratio of the cost of unplanned repairs to the cost of planned repairs. Corresponding each value of K we should find the optimal values of the repairing cycle and plot the graphs.

III. CONCLUSION

The programs, which calculating the relationships between the failure flow parameter ω*(l)* and the number of the total converted units repairs with the working time S(L) will be useful tools for the determination of the optimal repairing cycle of the parts and components of the means with regard the unexpected failures and the correlation between the costs of planned and unplanned repairs respectively.

Following the studies on the optimal repairing system based on the reliability [2], [3] and [4], this paper is a part of the R&D project on the optimizing locomotives repairing cycle based on the reliability (Proj. No. T-KTGT-2010-06) funded by the HCMUT.

REFERENCES

[1]. Đỗ Đức Tuấn. *"Đánh giá hao mòn, độ bền và độ tin cậy của chi tiết và kết cấu đầu máy diesel"*. NXB GTVT, (2005). (Do Duc Tuan. *Evaluation of wear, durability and reliability of details and constructions of diesel locomotives)*. Pub of Transport, Hanoi, (2005).

[2]. Đỗ Đức Tuấn. "Cơ sở tối ưu hoá chu kỳ sửa chữa các chi tiết và cụm chi tiết trên đầu máy có xét tới hư hỏng không tham số và chi phí sửa chữa". *Tạp chí KH Giao thông Vận tải*. Số 16, tr 125-136, (12/2006). /Do Duc Tuan. Optimizing fundamentals for repair period of details and units in locomotives with consideration of non-parameter failures and repair cost in and out of plan. / *Transport and Communications Science Journal*. No. 16, pp. 125-136, (Dec. 2006).

[3]. Đỗ Đức Tuấn, Võ Trọng Cang. "Cơ sở tối ưu hoá thời hạn sửa chữa các bộ phận chạy trên đầu máy-toa xe ở mức cho trước của độ tin cậy tham số". *Tạp chí KH Giao thông Vận tải*. Số 17, tr 134-142, (4/2007). /Do Duc Tuan, Vo Trong Cang. Optimizing repair periods for components in locomotives at pre-set parameter reliability/. *Transport and Communications Science Journal*. No. 17, pp. 134-142, (Apr. 2007).

[4]. Đỗ Đức Tuấn. "Cơ sở xác định cấu trúc tối ưu của chu trình sửa chữa đầu máy trên cơ sở giá thành sửa chữa và tuổi thọ gamma phần trăm chi tiết". *Tạp chí KH Giao thông Vận tải*. Số 21, tr 134-142, (3/2008). /Do Duc Tuan. Fundamentals for determination of optimal structure of locomotives repair cycle based on repair cost and gamma percent life cycle of elements./ *Transport and Communications Science Journal*. No 21, pp. 134-142, (Mar. 2008)

[5]. Галкин В.Г., Парамзин В.П., Четвергов В.А., *"Надежность тягового подвижного состава"*. Москва. Транспорт, (1981). /*Reliability of Locomotives/*. Moscow, Pub. of Transport, (1981)

[6]. Горский А.В, Воробьев А.А. *"Оптимизация системы ремонта локомотивов"*. Москва, Транспорт , (1994). /*Optimization of Locomotives' Repair System/*. Moscow, Pub. of Transport, (1994)

[7]. Пузанков А.Д. *"Надежность конструкций локомотивов"*. Москва. МИИТ, (1999). /*Reliability Design of Locomotives/*. Moscow, МИТ., (1999)

[8]. Võ Trọng Cang. *"Tối ưu hoá chu trình sửa chữa đầu máy trên cơ sở độ tin cậy"*. Đề tài NCKH T-KTGT-2010-06. ĐHBK TpHCM, (2011). /*Optimizing locomotive repair cycle based on reliability.* R&D Proj. Report T-KTGT-2010-06/. HCM City University of Technology, (2011)