

Performance Evaluation of Low Inertia Multi-Stage Solar Still

Prem Singh, Parmpal Singh, Jagdeep Singh, Ravi Inder Singh and Krishnendu Kundu

Abstract— In an attempt to increase distillation yield per unit evaporation area by decreasing the thermal inertia of the water mass, a new type of multi-stage solar still of low inertia was designed, fabricated and tested. The energy balance equations for various parts of the still were solved by Gauss-seidel iteration method. Computer model was made to predict the performance of the still and experimentally validated. The computer model was used to estimate the annual performance and pay back period of the still for Indian city of Ludhiana. At optimum combination of absorption area of solar water heater and evaporation area, the annual distillate yield and annual average performance ratio for the still were 2223.0 litres/m² aperture area and 0.73 respectively assuming 300 clear days. Annual average performance ratio of distillation unit alone is 2.73. The pay back period of the still was estimated to be three years.

Index Terms— low inertia solar still, multi-stage solar still, solar still

I. INTRODUCTION

WATER is a basic necessity for all living beings along with food and air. Man has been dependent on rivers, lakes and underground water reservoirs for fresh water requirements in domestic life, agriculture and industry. However, use of water from such sources is not always possible or desirable on account of the presence of large amount of salts and harmful organisms. The impact of many diseases affecting mankind can be drastically reduced if fresh hygienic water is provided for drinking. Diversity of approaches are used for separation of salts from saline water such as reverse osmosis, electro dialysis, solvent extraction, flash distillation etc. However, these methods are expensive for the production of small amount of fresh water. Solar energy can be used for distillation purpose where weather conditions are favorable and demand is not too large.

Fernandez and Chargoy [1] built a solar still consisting of array of solar water heaters of 50 m² aperture area and a multi-stage distillation unit with eight trays including the

bottom tray. On a typical day, total experimental yield was 41.1 litres while theoretically it was found to be 44.7 litres. Adhikari et. al. [2] prepared a computer simulation model for the steady-state performance of a multi-stage stacked solar still. The experimental and theoretical distillate yields were 0.64, 2.0 and 0.646, 2.207 l/hr at 358 and 890 watts of heat supplied, respectively. Sangeeta Suneja [3] used a computer simulation model to solve the energy balance equations for a multi-basin inverted absorber distiller unit. The effect of reuse of latent heat from vaporization from respective lower basins on daily yield was studied for optimization of number of effects. It was observed that when the number of basins is increased beyond seven, there is only a marginal increase in the yield. Jubran [4] developed a mathematical model to predict the productivity and thermal characteristics of a multi-stage solar still with an expansion nozzle and recovery in each stage of the still. This model was used to conduct a parametric investigation on the proposed solar still. The results were obtained with heat input in the range of 100-1000 watt, which is equivalent to solar insolation of 120-1200 W/m² when a 1.2m² solar collector is used. Pierre Le Goff [5] reported a distillation unit which is stack of six rectangular cells in thermal series. In each cell, which is a 4 cm thick film of salty water is partially evaporated as it trickles over a heated vertical wall. The vapor produced is condensed on the opposite wall of the cell. The heat evolved by this condensation is used to evaporate the film trickling on the other side of the same plate, in the next cell. The unit produces about 20 liters of distilled water per m², per standard day, under the same conditions of sunshine that would give a production of 2.5 to 3 liters/m² day in a conventional, "single basin" solar still.

In the present study, effort has been made to increase the distillation yield of multi-stage solar still by decreasing thermal capacity of water mass in the trays. This was achieved by modifying the geometry of trays. A computer model was developed for prediction of distillation yield as a function of solar radiation and ambient temperature for any place. The model was experimentally validated by conducting experiments on the still under environment conditions of Ludhiana.

II. DESCRIPTION OF THE SYSTEM

The schematic diagram of the low inertia multi-stage solar still is shown in Fig. 1. It consists of a heating unit (flat plate collector) and a distillation unit. The heating unit

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of the experimental low inertia multi-stage solar still is a flat plate collector of a fin and tube type with single glass cover. The collector of size $229 \times 125 \times 14$ cm (aperture 216×107 cm) is made of galvanized iron sheet. Its absorber is blackened with black board paint. The total number of riser tubes is 15, each of diameter 15 mm. Each riser tube is connected to two header tubes one at the top

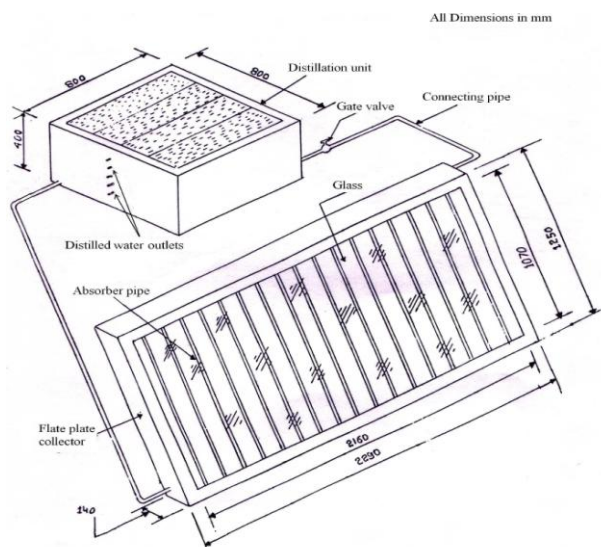


Fig.1: Low inertia multi stage solar still

and other at bottom, each of 35 mm diameter. Flat plate collector is insulated at bottom with glass wool of thickness 10 cm. The insulation of glass wool on sides is represented by the difference in dimensions of the outer frame and aperture. The lower and upper header pipes extend out of collector to act as inlet and outlet of the collector respectively.

Distillation unit of low inertia multi-stage solar still (Fig. 2) consists of three main parts namely: bottom tray, upper trays and collecting channels made from galvanized iron

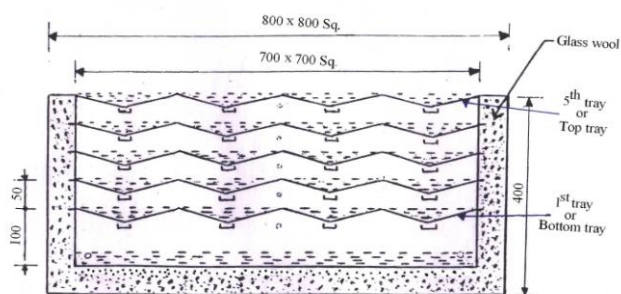


Fig.2: Cross-section of distillation of low inertia multi stage solar still

sheet. The size of bottom tray is $70 \times 70 \times 10$ cm. It has two pipes in its opposite sides for the circulation of hot water of collector though it. These pipes are diagonally opposite. The depth of water in the bottom tray is kept 3 cm with the help of waste water pipe. The total mass of water in the bottom tray is 14.7 kg. One of the five upper trays each of size $70 \times 70 \times 5$ cm is shown in Fig. 3(a). The bottom surface of each tray is bent at four places along one of its sides. So the bottom surface of each tray is sub divided into eight inclined surfaces, each inclined at an angle of 15° with horizontal. This was done to ensure that trays hold small amount of water in them and it also facilitates collection of condensate from the down facing surface. Water is fed to all

the trays though top most tray. The quantity of water filled in each tray except bottom tray is such that it is just sufficient to cover the bottom surface. There is provision in each tray so that when it is filled to the desired level, water starts flowing to the tray immediately below this tray. This way, all the trays get filled with water. Waste water is discharged out from the bottom tray through an overflow provided for this purpose. The mass of water in each upper tray is 6.125 kg. Five collecting channels (one such channel is shown in Fig. 3(b)) are provided to collect distilled water from the down facing surface of each tray excluding the bottom tray.

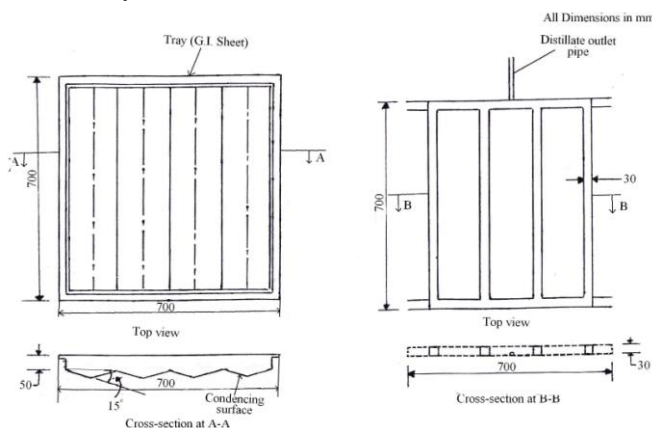


Fig.3 (a): Tray of distillation unit of low inertia multi-stage solar still

Fig.3 (b): Collecting channel under each tray of distillation unit of low inertia multi-stage solar still

Collecting channel having a slope of 1:50 is placed on the bottom tray, the upper tray is fitted on bottom tray with nuts and bolts by providing rubber seal in between them to make leak proof unit. In the similar way remaining four upper trays and channels are assembled one upon other. This assembled unit is placed in another tank of size $80 \times 80 \times 40$ cm, which provides insulation of 5 cm of glass wool on all vertical sides and 10 cm bottom side. The top tray is exposed to atmosphere.

III. EXPERIMENTATION

The still was tested in the month of December at Indian city of Ludhiana (latitude $31^\circ N$). Collector of the still was kept inclined at 45° facing south. Hot water of collector circulates through the bottom tray of the still due to thermosyphon effect. Ambient temperature, solar radiation on glass cover and horizontal surface, evaporating and condensing surface temperatures and distillation yield of each stage were recorded after every hour.

IV. COMPUTER MODEL

The following assumptions were made while making computer model for the still. (i) Mean water temperature in the bottom tray of the low inertia multi-stage solar still and in flat plate collector is same. (ii) Water is at uniform temperature in each tray. (iii) Heat capacity of glass cover of solar water heater is negligible. (iv) The system is air and vapour tight. (v) Evaporating and condensing surfaces are infinite parallel plates. (vi) The temperature of top most

tray is almost equal to the ambient temperature. Hence heat stored in the water mass of this tray, heat lost from sides and heats lost to ambient through evaporation have been neglected. The energy balance equations per unit area for the different elements are written as follows.

For bottom or 1st tray:

$$\begin{aligned} \text{Heat supplied by collector to still} &= \text{Heat transfer from 1st to 2nd tray by convection, evaporation and radiation} + \text{Heat loss to ambient from sides of 1st tray} + \text{Heat loss to ambient from bottom of 1st tray} + \text{Heat stored in water mass in 1st tray} \\ Q_{cs} &= Q_{1,2} + Q_{s1} + Q_{b1} + Q_{w,1} \end{aligned} \quad (1)$$

For 2nd tray:

$$\begin{aligned} \text{Heat transfer from 1st to 2nd tray by convection, evaporation and radiation} &= \text{Heat loss to ambient from sides of 2nd tray} + \text{Heat transfer from 2nd to 3rd tray by convection, evaporation and radiation} + \text{Heat stored in water mass in 2nd tray} \\ Q_{1,2} &= Q_{s2} + Q_{2,3} + Q_{w,2} \end{aligned} \quad (2)$$

For 3rd tray:

$$\begin{aligned} \text{Heat transfer from 2nd to 3rd tray by convection, evaporation and radiation} &= \text{Heat loss to ambient from sides of 3rd tray} + \text{Heat transfer from 3rd to 4th tray by convection, evaporation and radiation} + \text{Heat stored in water mass in 3rd tray} \\ Q_{2,3} &= Q_{s3} + Q_{3,4} + Q_{w,3} \end{aligned} \quad (3)$$

For 4th tray:

$$\begin{aligned} \text{Heat transfer from 3rd to 4th tray by convection, evaporation and radiation} &= \text{Heat loss to ambient from sides of 4th tray} + \text{Heat transfer from 4th to 5th tray by convection, evaporation and radiation} + \text{Heat stored in water mass in 4th tray} \\ Q_{3,4} &= Q_{s4} + Q_{4,5} + Q_{w,4} \end{aligned} \quad (4)$$

For 5th tray:

$$\begin{aligned} \text{Heat transfer from 4th to 5th tray by convection, evaporation and radiation} &= \text{Heat loss to ambient from sides of 5th tray} + \text{Heat transfer from 5th to 6th tray by convection, evaporation and radiation} + \text{Heat stored in water mass in 5th tray} \\ Q_{4,5} &= Q_{s5} + Q_{5,6} + Q_{w,5} \end{aligned} \quad (5)$$

For 6th tray:

$$\begin{aligned} \text{Heat transfer from 5th to 6th tray by convection, evaporation and radiation} &= \text{Heat transfer from 6th to ambient by convection and radiation} \\ Q_{5,6} &= Q_{6,a} \end{aligned} \quad (6)$$

Heat transfer from evaporating surface to condensing surface:

$$Q_{i,i+1} = (h_{r(i,i+1)} + h_{c(i,i+1)} + h_{e(i,i+1)}) \times A_{bi} \times (T_i - T_{i+1}) \quad i = 1 \text{ to } 5 \quad (7)$$

Heat loss to ambient from sides of trays:

$$Q_{si} = U_{si} \times A_{si} \times (T_i - T_a) \quad i = 1 \text{ to } 5 \quad (8)$$

Heat loss to ambient from bottom of 1st tray:

$$Q_{b1} = U_{b1} \times A_{b1} \times (T_1 - T_a) \quad (9)$$

Heat loss to ambient from top tray:

$$Q_{6,a} = (h_{c(6,a)} + h_{r(6,a)}) \times A_{b6} \times (T_6 - T_a) \quad (10)$$

Putting the values of $Q_{i,i+1}$, Q_{si} , Q_{b1} and $Q_{6,a}$ from equations (7) to (10) in equations (2) to (6), we get the following simultaneous linear equations:

$$\begin{aligned} h_{1,2} \times A_{b1} \times T_1 - (h_{1,2} \times A_{b1} + h_{2,3} \times A_{b2} + h_{s2} \times A_{s2} + m_w \times c_w / dt) \times T_2 + \\ h_{2,3} \times A_{b2} \times T_3 + m_w \times c_w \times T'_1 / dt + h_{s2} \times A_{s2} \times T_a = 0 \quad (11) \end{aligned}$$

$$h_{2,3} \times A_{b2} \times T_2 - (h_{2,3} \times A_{b2} + h_{3,4} \times A_{b3} + h_{s3} \times A_{s3} + m_w \times c_w / dt) \times T_3 + h_{3,4} \times A_{b3} \times T_4 + m_w \times c_w \times T'_2 / dt + h_{s3} \times A_{s3} \times T_a = 0 \quad (12)$$

$$h_{3,4} \times A_{b3} \times T_3 - (h_{3,4} \times A_{b3} + h_{4,5} \times A_{b4} + h_{s4} \times A_{s4} + m_w \times c_w / dt) \times T_4 + h_{4,5} \times A_{b4} \times T_5 + m_w \times c_w \times T'_3 / dt + h_{s4} \times A_{s4} \times T_a = 0 \quad (13)$$

$$h_{4,5} \times A_{b4} \times T_4 - (h_{4,5} \times A_{b4} + h_{5,6} \times A_{b5} + h_{s5} \times A_{s5} + m_w \times c_w / dt) \times T_5 + h_{5,6} \times A_{b5} \times T_6 + m_w \times c_w \times T'_4 / dt + h_{s5} \times A_{s5} \times T_a = 0 \quad (14)$$

$$h_{5,6} \times A_{b5} \times T_5 - (h_{5,6} \times A_{b5} + h_{6,a} \times A_{b6}) \times T_6 + h_{6,a} \times A_{b6} \times T_a = 0 \quad (15)$$

Heat supplied from still to collector (Q_{sc}):

$$Q_{sc} = Q_{ac} - Q_{lc} - (m_w \times c_w) \times (T_{c(t)} - T_{c(t-dt)}) / dt \quad (16)$$

Distillation yield:

$$Y_{(i)} = h_{e(i,i+1)} \times A_{bi} \times (T_{(i)} - T_{(i+1)}) \times dt / L_w \text{ Kg (or litres)} \quad (17)$$

To predict the distillation yield of the still theoretically, a computer program was written in quick basic language for the solution of the energy balance equations of the still elements. The flow chart is shown in Fig.4. The input parameters to the computer program include the climatic parameters (solar radiation, ambient temperature), thermo-physical parameters (properties of air & water, thermal conductivity etc.) and configurational parameters (dimensions of the still & solar water heater).

Initially, the temperatures of the different components of the still are assumed to be equal to the ambient air temperature at the sunrise time of the collector. Equations (2) to (6) are solved by Gauss-seidel iteration method for different tray temperatures. Then comparison is made between the heat supplied by collector from equation (1) and (16) respectively. If they are equal then this is the required condition. Then distillation yield of each tray of the still was determined from equation (17). This process is repeated for an additional time interval dt. For validation of computer model, measured solar radiation and ambient temperature data was used in the program. To predict yearly performance of the still, the validated computer model was run for the representative day of every month assuming 300 clear days in a year. The computer model was also run at different values of evaporation area of trays to find maximum distillate yield and hence to find optimum evaporation area of individual trays.

V. RESULTS AND DISCUSSION

Solar radiation on aperture and ambient temperature for a given day are shown in Fig. 5. Theoretical and experimentally measured water temperatures in different trays of low inertia multi-stage solar still are shown in Fig. 6. Maximum water temperature achieved is 62, 54, 48, 41 and 35°C in 1st, 2nd, 3rd, 4th and 5th tray respectively.

Distillation yield of different stages of low inertia multi-stage solar still is shown in Fig. 7 and 8. The distillation yield in lower trays is higher during daytime due to higher water temperature and large temperature different in these trays. During evening (after sunset) distillation in upper trays is higher than in lower trays. This is due to the fact that though lower trays are at higher temperature, there is

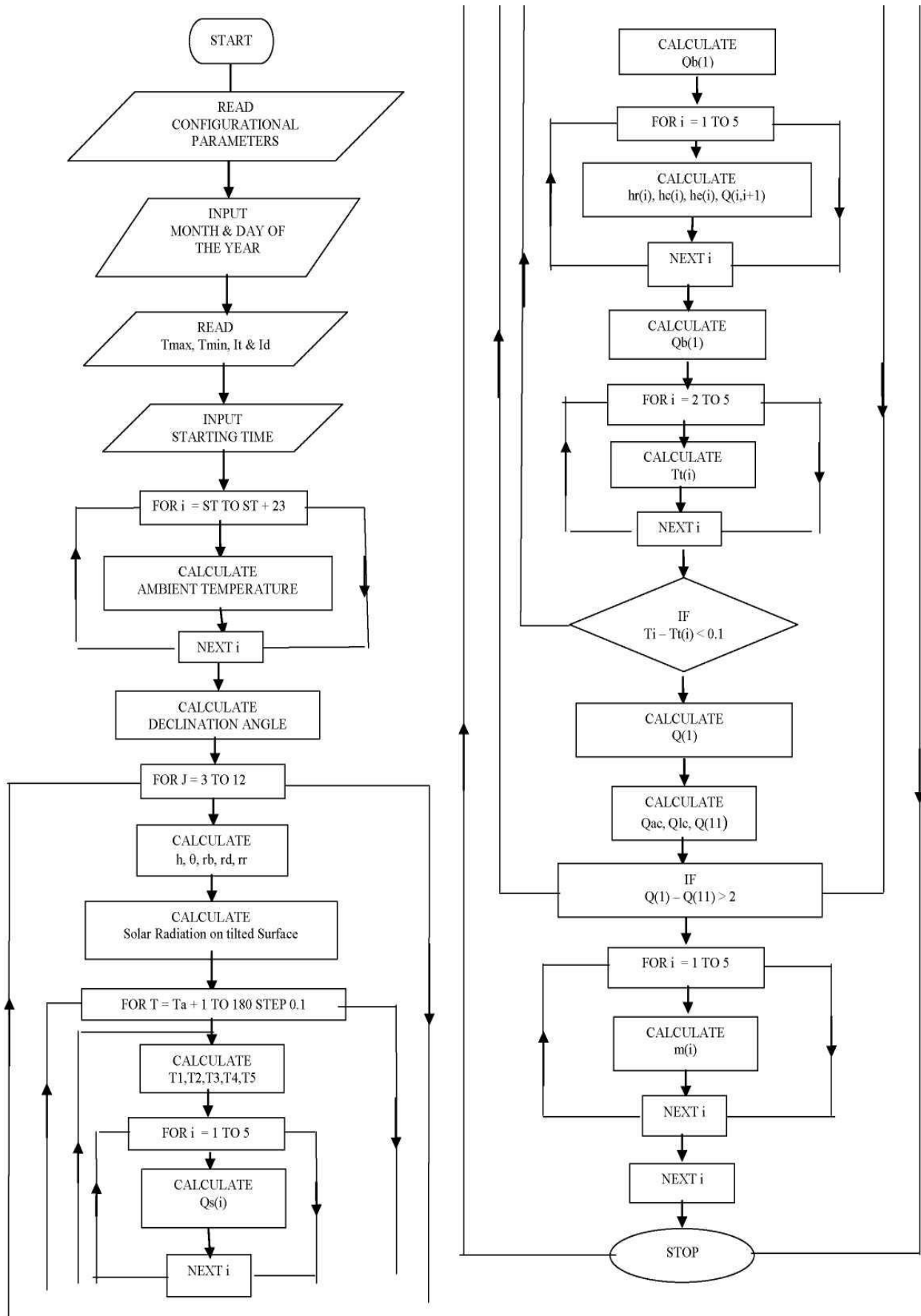


Fig. 4 : Flow chart of low inertia multi-stage solar still

large temperature difference in the upper trays than in lower trays. The predicted distillation yield is about 10% higher than the experimental yield. This is due to higher theoretical temperatures of trays than experimentally measured temperatures.

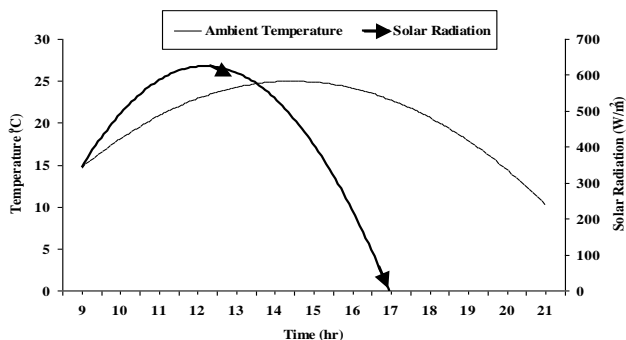


Fig.5: Variation of solar radiation on operature (inclined at angle of 45 degree) of low inertia multi-stage solar still and ambient temperature as function of time

Performance ratio of the still defined as latent heat required to evaporate given quantity of water to the energy falling on the aperture of the collector, is 0.264. This low value is due to the fact that ratio of evaporation area to the aperture area for the still is low. Maximum yield was found at an optimum evaporation area of 1.5 m² of each of five trays (ratio of evaporation area of individual tray to the collector area is 0.75). With this area, performance ratio of low inertia multi-stage solar still and distillation unit alone are 0.67 and 2.73 respectively. The performance ratio of the distillation unit is quite high. This is due to the lesser thermal inertia of the distillation unit due lesser quantity of water in the trays.

Monthly average distillation yield of low inertia multi-stage solar still is shown in Fig. 9. Annual yield was calculated for the still by computing yield for typical day of every month from the computer model. Yield of typical day of the year was calculated by averaging these values. Then annual yield at Ludhiana was calculated by assuming 300 clear days in a year. The annual distillation yield per square metre aperture area and annual performance ratio for low inertia multi-stage solar still, corresponding to optimum

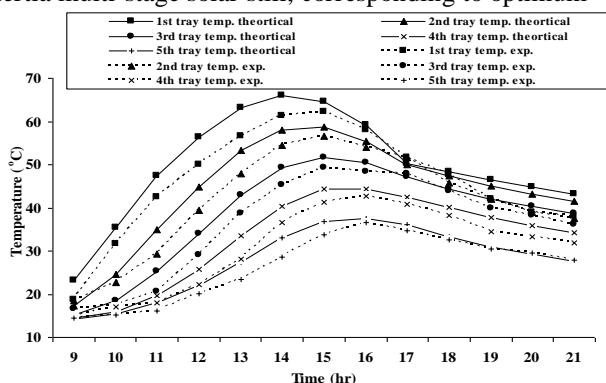


Fig.6: Hourly variations of the theoretical and experimental water temperature in different trays of low inertia multi-stage solar still

evaporation area of 1.5 m², are 2223 litres and 0.73 respectively. Performance ratio of distillation unit alone is 2.73 under these conditions. Pay back period of the still was estimated to be three years.

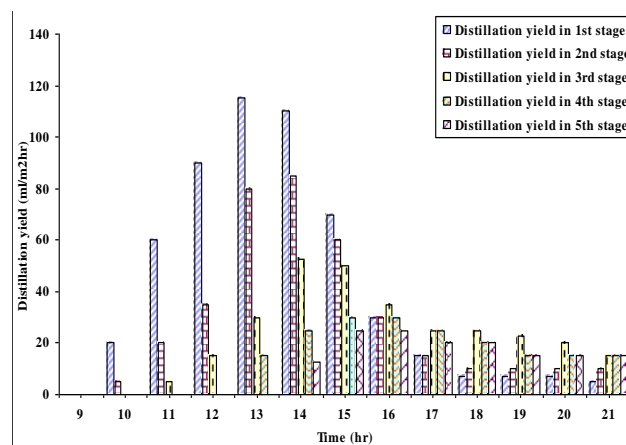


Fig.8: Distillation yield (experimental) in every stage of low inertia multi-stage solar still as function of time

VI. CONCLUSIONS

A multi-stage solar still with low inertia was designed and

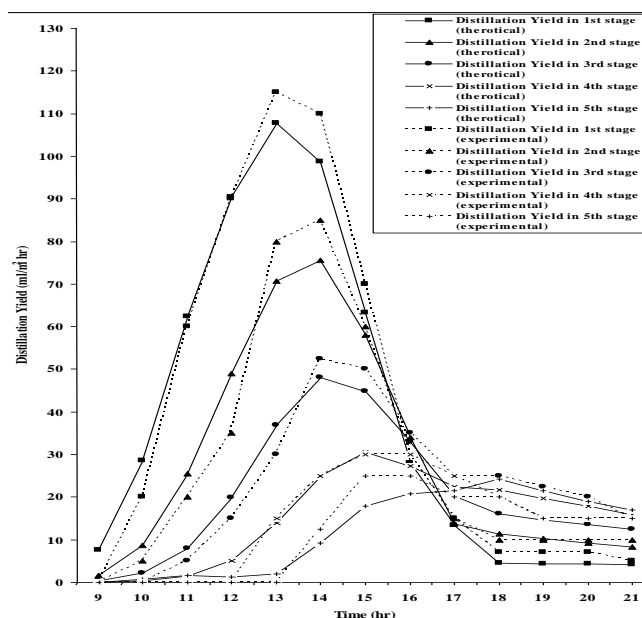


Fig.7: Hourly variation of distillation yield (Experimental and Theoretical) in different stages of low inertia multi-stage solar still as function of time

fabricated. Also a computer mode to predict the performance of multi-stage solar still has been developed. This model has been validated by comparison with the experimental results obtained at Ludhiana, hence can be

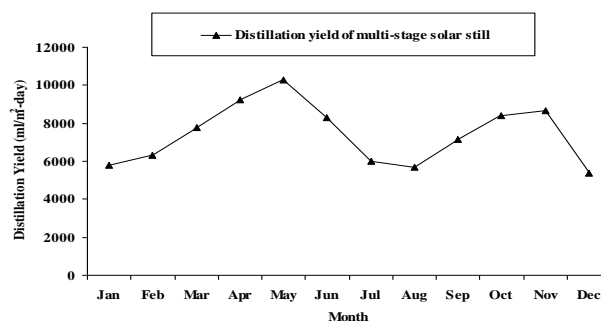


Fig.9: Theoretically predicted distillation yield for low inertia multi-stage solar still for the climatic condition of Ludhiana on typical day of each month

used for predicting the system performance for any other place. The new design of low inertia multi-stage solar still shows great potential in terms of distillation yield.

NOMENCLATURE

A	Area (m ²)
c	Specific heat (J/kg °C)
dt	Time interval (s)
dT	Change in temperature (°C)
h	Heat transfer coefficient (W/m ² °C)
I	Solar radiation on aperture (W/m ²)
L	Latent heat of Water (J/kg) / length (m)
m	mass (kg)
n	Day of the year (n = 1 for 1 st January)
P	Water saturation pressure (N/m ²)
Q	Heat loss / heat supplied / heat stored (W)
R	Reflectivity
r	Tilt factor
T	Temperature (°C)
U	Overall heat transfer coefficient (W/m ² °C)
Y	Distillation yield (litres)
Greek symbols	
α	Absorptivity
ω	Hour angle (deg)
ρ	Reflectivity of ground, density (kg/m ³)
τ	Transmittivity
θ	Angle of incidence (deg)
β	Slope of collector with horizontal (deg)
ω	Hour angle (deg)
φ	Latitude angle (deg)
δ	Declination angle (deg) / thickness (m)
ε _{eff}	Effective emissivity
ε	Emissivity
σ	Stefanboltzman constant (W/m ² K ⁴)
Subscripts	
a	ambient
ac	absorbed by collector
ag	absorbed by glass
b	beam radiation
bi	from / (corresponding to) bottom of i th tray
c	collector
cs	collector to still
c(i,i+1)	convective from i th to (i+1) th tray
d	diffuse radiation
e(i,i+1)	evaporative from i th to (i+1) th tray
g	glass
i	a given tray being identified by a number / insulation
i,i+1	from i th to (i+1) th tray
lc	loss from collector
r	reflected radiation
r(i,i+1)	radiative from i th to (i+1) th tray
sc	still to collector
t	time
si	from / (corresponding to) sides of i th tray
w	water
6,a	from sixth tray to ambient
Superscript	
'	after time interval dt

APPENDIX

The solar radiation falling on horizontal surface was converted to that falling on inclined surface (equations. a to g):

$$I_{ag} = I \times \alpha_g \dots\dots\dots (a)$$

$$\delta(\text{Degree})=23.45 \times \sin[360 \times (284+n)/365] \dots\dots (b)$$

$$r_b = \frac{\sin(\delta) \times \sin(\phi - \beta) + \cos(\delta) \times \cos(\omega) \times \cos(\phi - \beta)}{\sin(\delta) \times \sin(\phi) + \cos(\delta) \times \cos(\omega) \times \cos(\phi)} \dots\dots (c)$$

$$r_d = (1 + \cos(\beta)) / 2 \dots\dots\dots (d)$$

$$r_r = \rho \times (1 - \cos(\beta)) / 2 \dots\dots\dots (e)$$

$$I = (I_g - I_d) \times r_b + I_d \times r_d + I_g \times r_r \dots\dots\dots (g)$$

Where, I_g = Global (total) radiation flux on horizontal surface
I_d = Diffuse radiation flux on horizontal surface

$$\alpha_g = 1 - \tau_g - R_g$$

$$\theta = \text{Cos}^{-1} \{ \text{Sin}(\delta) \times \text{Sin}(\phi - \beta) + \text{Cos}(\delta) \times \text{Cos}(\omega) \times \text{Cos}(\phi - \beta) \}$$

$$h_{c(i,i+1)} = 0.844 \times [(T_i - T_{i+1}) + (P_i - P_{i+1}) \times (T_i + 273.15) / (268900 - P_i)]^{1/3} \text{ W/m}^2\text{C}$$

i = 1 to 5

$$P_i = \exp[25.317 - 5144 / (T_i + 273.15)] \text{ N/m}^2$$

$$P_{i+1} = \exp[25.317 - 5144 / (T_{i+1} + 273.15)] \text{ N/m}^2$$

$$h_{e(i,i+1)} = 16.273 \times 10^{-3} \times h_{c(i,i+1)} \times (P_i - P_{i+1}) / (T_i - T_{i+1}) \text{ W/m}^2\text{C}$$

$$h_{r(i,i+1)} = \epsilon_{\text{eff}} \times \sigma \times [(T_i + 273.15)^2 + (T_{i+1} + 273.15)^2] \times [(T_i + 273.15) + (T_{i+1} + 273.15)] \text{ W/m}^2\text{C}$$

$$\epsilon_{\text{eff}} = 1 / (1 / \epsilon_g + 1 / \epsilon_w - 1)$$

$$h_{i,i+1} = h_{c(i,i+1)} + h_{e(i,i+1)} + h_{r(i,i+1)} \text{ W/m}^2\text{C}$$

$$U_{\text{si}} \text{ or } U_{\text{b1}} = 1 / (1 / h_s + \delta_i / K_i)$$

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