

2-Stage 4-Phase Switched-Capacitor Boost DC-AC Inverter with Sinusoidal PFM Control

Yuen-Haw Chang, Chin-Ling Chen, and Po-Chien Lo

Abstract— A new closed-loop scheme of 2-stage 4-phase switched-capacitor (SC) boost DC-AC inverter is proposed by combining 4-phase phase generator and sinusoidal pulse-frequency-modulation (SPFM) controller for low-power step-up inversion and regulation. In this SC inverter, the power part of the inverter is composed of 2-stage 4-phase SC booster and DC-link inverter. This SC booster contains 2 pumping capacitors and 4 switches operation for boosting the step-up gain up to $2^2 = 4$ at most. For improving total harmonic distortion (THD), a $4x/3x/2x/1x$ selector is presented to select a proper gain in order to make the maximum of the practical output close to the desired output voltage as much as possible. The DC-link inverter like H-bridge structure consists of 4 switches controlled by SPFM to realize full-wave DC-AC operation. Besides, the SPFM is employed for the closed-loop realization to enhance the output realization capability for the different output peak and frequency. Finally, the 2-stage 4-phase SC boost inverter is simulated by OrCAD, and all results are illustrated to show the efficacy of the proposed scheme.

Index Terms— switched-capacitor (SC), boost DC-AC inverter, sinusoidal pulse-frequency-modulation (SPFM).

I. INTRODUCTION

With the popularity of portable electronic equipments, e.g. digital camera, e-book, mobile phone, notebook, and pad ... etc., the power modules of these products always ask for some good characteristics: small volume, light weight, higher efficiency, and better regulation capability. Generally, the traditional power converters have a large volume and a heavy weight because of magnetic elements. Therefore, more manufactures and researchers pay much attention to this topic, and ultimately, requiring DC-DC/DC-AC converters realized on a compact chip by mixed-mode VLSI technology.

The switched-capacitor (SC) power converter has received more and more attention because it has only semiconductor switches and capacitors. Thus, this kind of SC converters is one of the good solutions for low-power DC-DC/DC-AC conversion. Unlike the traditional converter, the SC converter needs no magnetic element, so they always have the small volume and light weight. The SC converter is usually designed for an output higher than supply voltage or a reverse-polarity voltage. This function fits many applications, e.g. drivers of electromagnetic luminescent (EL) lamp, white

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light emitting diode (WLED), op-amp, and LCD drivers. Up to now, the various SC types have been suggested for power conversion. In 1990, the first SC step-down converters were proposed by Japan researchers [1], and their idea is to switch MOSFETS cyclically according to 4 periods of capacitors charging/discharging for step-down conversion. In 1993, Cheong *et al.* suggested a modified SC converter with two symmetrical SC cells working in the two periods [2]. In 1995, Chung and Ioinovici suggested a current-mode SC for improving current waveforms [3]. In 1998, Mak and Ioinovici suggested an SC inverter with high power density [4]. In 2004, Chang proposed design and analysis of power-CMOS-gate-based SC boost DC-AC inverter [5]. The advantage of this SC inverter is to reduce the electromagnetic interference (EMI) problem. In 2007, Chang proposed CPLD-based closed-loop implementation of SC step-down DC-DC converter for multiple output choices [6]. In 2010, Hinago and Koizumi proposed a single-phase multilevel inverter using switched series/parallel DC voltage sources based on multiple independent voltage sources in order to reach the higher number of levels so as to reduce the THD value [7]. In 2011, Chang proposed an integrated SC step-up/down DC-DC/DC-AC converter/inverter [8-11].

In this paper, by using the 2-stage 4-phase SC boost and SPFM control, the boost DC-AC inverter is proposed not only to enhance full-wave output regulation via SPFM technique, but also to improve the THD value and provide the maximum gain proportional to the number of pumping capacitors.

II. CONFIGURATION

Fig.1 shows the configuration of the 2-stage 4-phase SC boost DC-AC inverter proposed, and it contains two parts: power part and control part. The discussions are as follow.

A. Power Part

This SC boost inverter as in the upper of Fig. 1 is composed of a 2-stage 4-phase booster and a DC-link inverter for DC-AC conversion. The 2-stage 4-phase booster consists of four switches (S1-S4) and two pumping capacitors (C1, C2) between supply source V_s and DC-link inverter, where each pumping capacitor is assumed with the same value C ($C_1=C_2=C$). The main function of this booster is to obtain a voltage up to $4x$, $3x$, $2x$, and $1x$ the voltage of V_s , and then DC-link inverter is to invert this voltage for reaching the sinusoidal output. Thus, this power part can provide the output range of $+4V_s \sim -4V_s$ for realizing DC-AC conversion. Fig. 2 shows the theoretical waveforms of these switches S1-S4, S_a , S_b , and V_{out} . These operations are discussed below.

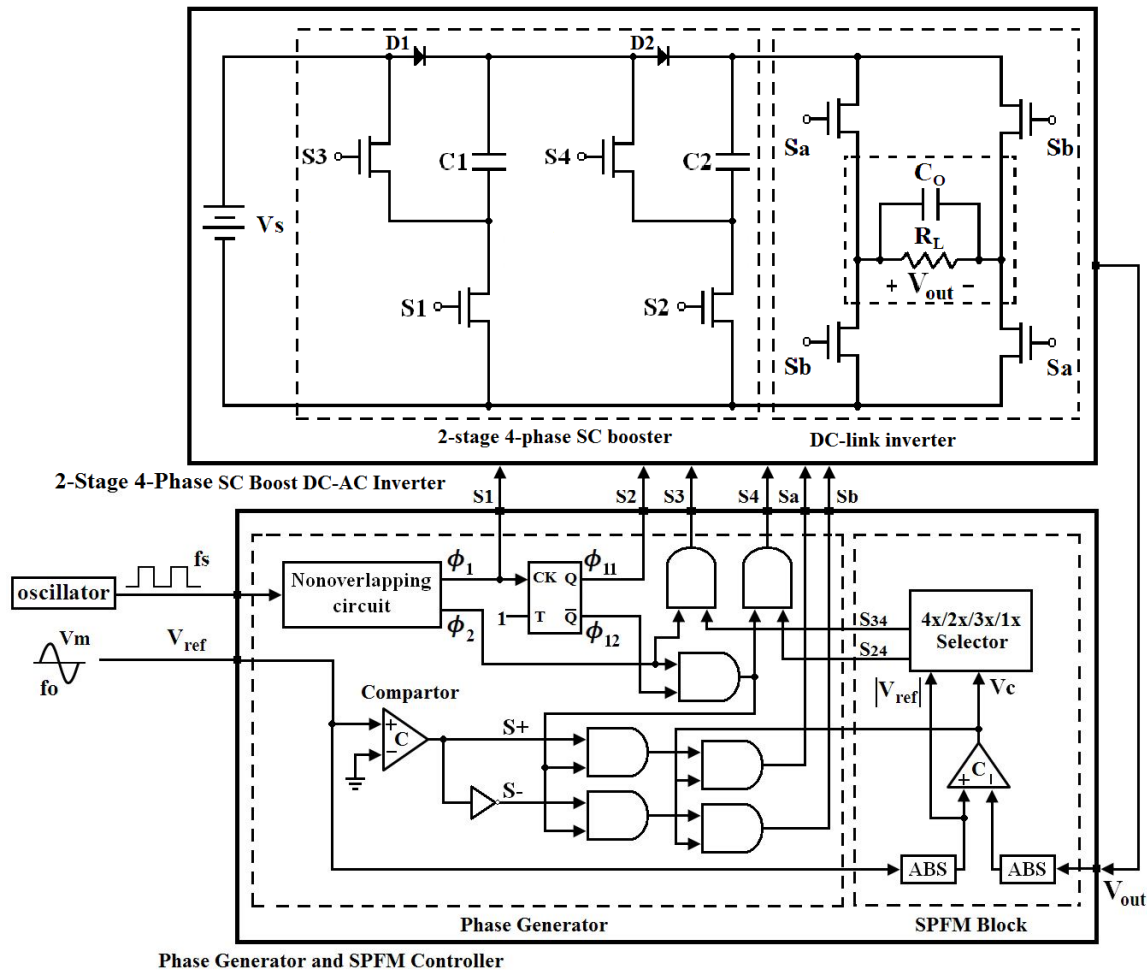


Fig. 1. Configuration of closed-loop 2-stage 4-phase SC boost DC-AC inverter.

1) Positive Half-Wave (PHW):

a) Phase I:

S1, S2 turn on, and S3, S4, Sa, Sb turn off. The relevant topology is shown in Fig. 3(a). C1, C2 are charged by Vs in parallel.

b) Phase II:

S2, S3 turn on, and S1, S4, Sa, Sb turn off. The relevant topology is shown in Fig. 3(b). C2 is charged by Vs and C1 in series.

c) Phase III:

S1 turns on, and S2, S3, S4, Sa, Sb turn off. The relevant topology is shown in Fig. 3(c). The only C1 is charged by Vs.

d) Phase IV:

In the PHW for various voltage gains (4x, 3x, 2x, 1x), the different phase IV operations (switches and topologies) are explained below.

(i) 4x:

S3, S4, Sa, turn on, and S1, S2, Sb turn off. The current flow is passing from Vs, C1, and C2 in series connection through S3, S4 to the DC-link as in Fig. 3(d). And with the help of Sa, the positive 4x function can be achieved (V_{out}: ~ +4Vs).

(ii) 3x:

S4, Sa turn on, and S1, S2, S3, Sb turn off. The current flow is passing from Vs and C2 in series connection through S4 to the DC-link as in Fig. 3(e). And with the help of Sa, the positive 3x function can be achieved (V_{out}: ~ +3Vs).

(iii) 2x:

S3, Sa turn on, and S1, S2, S4, Sb turn off. The current flow is passing from Vs and C1 in series connection through S3 to the DC-link as in Fig. 3(f). And with the help of Sa, the positive 2x function can be achieved (V_{out}: ~ +2Vs).

(iv) 1x:

Sb turn on, S1, S2, S3, S4, S3, Sb turn off. The current flow is passing from Vs to the DC-link as in Fig. 3(g). And with the help of Sa, the positive 1x function can be achieved (V_{out}: ~ +1Vs).

2) Negative Half-Wave (NHW):

a) Phase I:

S1, S2 turn on, and S3, S4, Sa, Sb turn off. The relevant topology is shown in Fig. 3(a). C1, C2 are charged by Vs in parallel.

b) Phase II:

S2, S3 turn on, and S1, S4, Sa, Sb turn off. The relevant topology is shown in Fig. 3(b). C2 is charged by Vs and C1 in series.

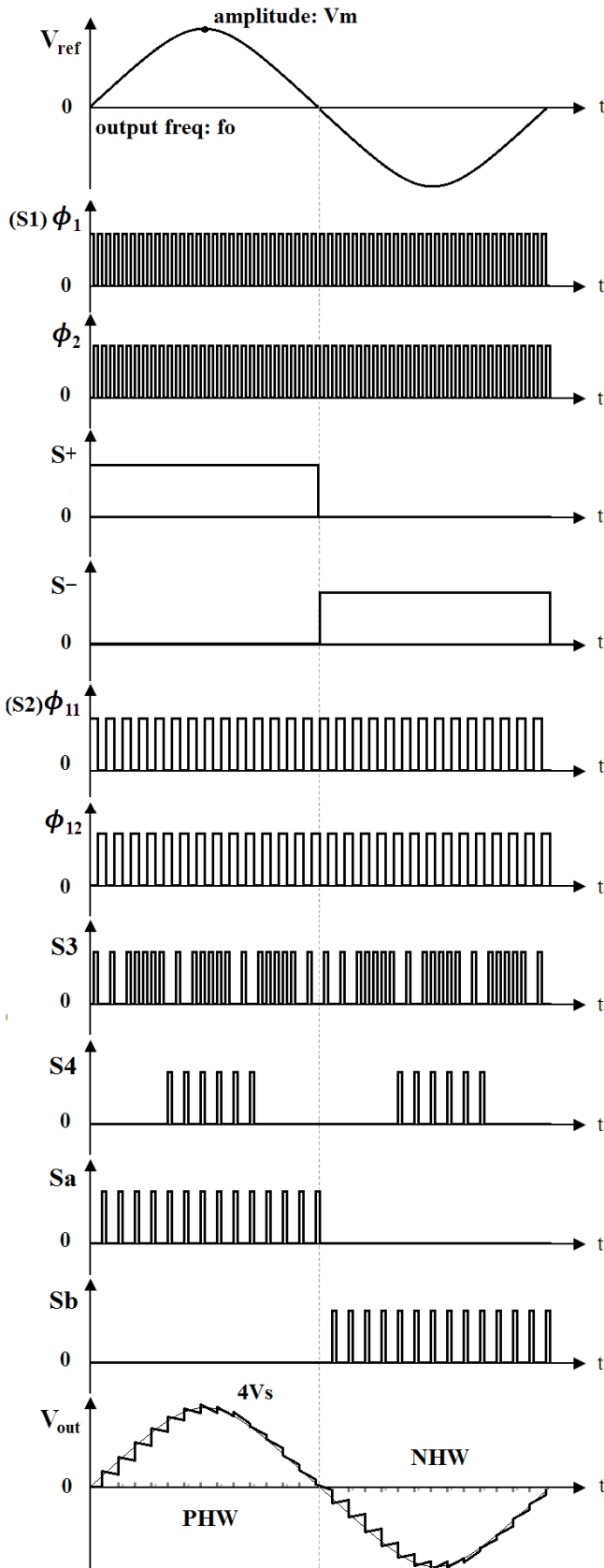


Fig. 2. Theoretical waveforms of the proposed inverter.

c) Phase III:

S1 turns on, and S2, S3, S4, Sa, Sb turn off. The relevant topology is shown in Fig. 3(c). The only C1 is charged by Vs.

d) Phase IV:

In the NHW for various voltage gains (4x, 3x, 2x, 1x), the different phase IV operations (switches and topologies) are explained below.

(i) 4x

S3, S4, Sb, turn on, and S1, S2, Sa turn off. The current flow is passing from Vs, C1, and C2 in series connection through S3, S4 to the DC-link as in Fig. 3(d). And with the help of Sb, the negative 4x function can be achieved (Vout: ~ -4Vs).

(ii) 3x:

S4, Sb turn on, and S1, S2, S3, Sa turn off. The current flow is passing from Vs and C2 in series connection through S4 to the DC-link as in Fig. 3(e). And with the help of Sb, the negative 3x function can be achieved (Vout: ~ -3Vs).

(iii) 2x:

S3, Sb turn on, and S1, S2, S4, Sa turn off. The current flow is passing from Vs and C1 in series connection through S3 to the DC-link as in Fig. 3(f). And with the help of Sb, the positive 2x function can be achieved (Vout: ~ -2Vs).

(iv) 1x:

Sb turn on, S1, S2, S3, S4, Sa, Sb turn off. The current flow is passing from Vs to the DC-link as in Fig. 3(g). And with the help of Sb, the positive 1x function can be achieved (Vout: ~ -1Vs).

B. Control Part

In the proposed inverter, the SPFM-based controller is used as shown in lower of Fig. 1. The controller is composed of SPFM block and phase generator. From the view of signal flow, V_{out} is firstly sent into the SPFM block. After the operation of absolute value, V_{out} is compared with the desired output signal V_{ref} (sinusoidal reference) to obtain a control signal V_c as:

$$\text{If } |V_{ref}| \geq |V_{out}|, \text{ then } V_c = 1,$$

$$\text{If } |V_{ref}| < |V_{out}|, \text{ then } V_c = 0.$$

Next, according to V_c and |V_{ref}|, the 4x/3x/2x/1x selector as in Fig. 4 can generate the boosting control signals (S₂₄, S₃₄) for a proper gain level, and the relevant rules are shown as below:

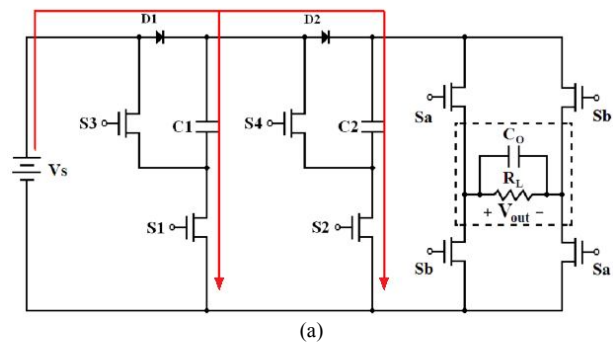
$$1) \text{ If } |V_{ref}| \geq \frac{3}{4}V_{dd} \text{ and } V_c = 0, \text{ then } S_{24} = 0, S_{34} = 0;$$

$$2) \text{ If } |V_{ref}| \geq \frac{3}{4}V_{dd} \text{ and } V_c = 1, \text{ then } S_{24} = 1, S_{34} = 1;$$

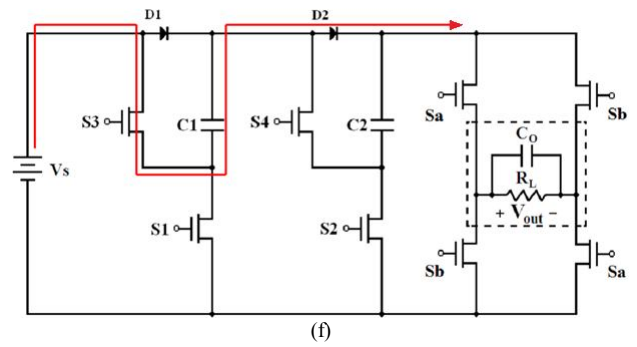
$$3) \text{ If } \frac{2}{4}V_{dd} \leq |V_{ref}| < \frac{3}{4}V_{dd} \text{ and } V_c = 0, \text{ then } S_{24} = 0, S_{34} = 0;$$

$$4) \text{ If } \frac{2}{4}V_{dd} \leq |V_{ref}| < \frac{3}{4}V_{dd} \text{ and } V_c = 1, \text{ then } S_{24} = 0, S_{34} = 1;$$

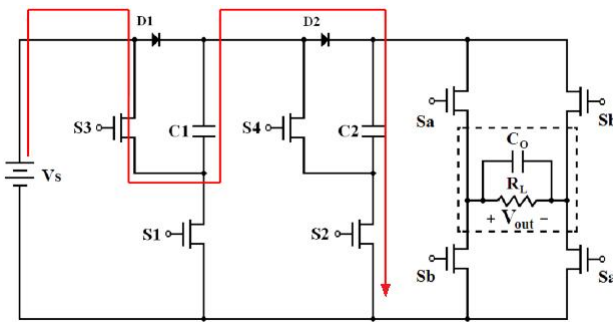
$$5) \text{ If } \frac{1}{4}V_{dd} \leq |V_{ref}| < \frac{2}{4}V_{dd} \text{ and } V_c = 0, \text{ then } S_{24} = 0, S_{34} = 0;$$



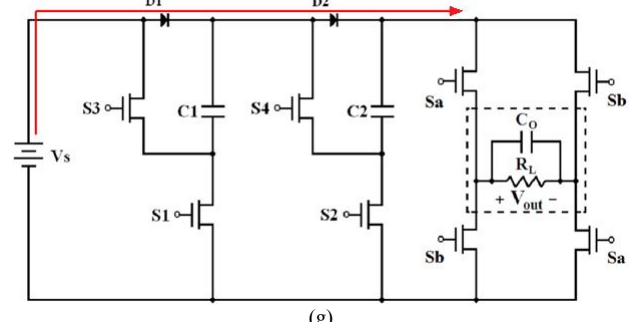
(a)



(f)

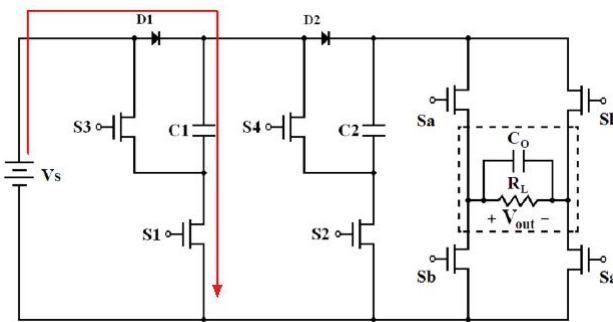


(b)

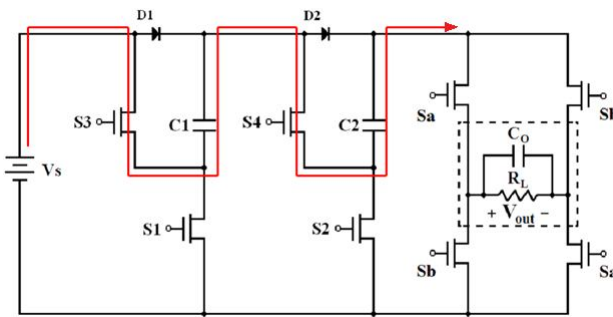


(g)

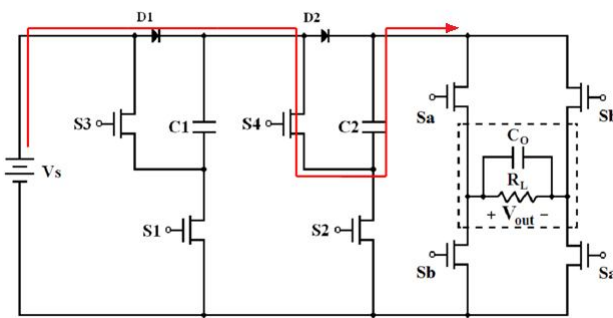
Fig. 3. Topologies of the proposed inverter for (a) Phase I, (b) Phase II, (c) Phase III, (d) Phase IV of 4x, (e) Phase IV of 3x, (f) Phase IV of 2x, and (g) Phase IV of 1x.



(c)



(d)



(e)

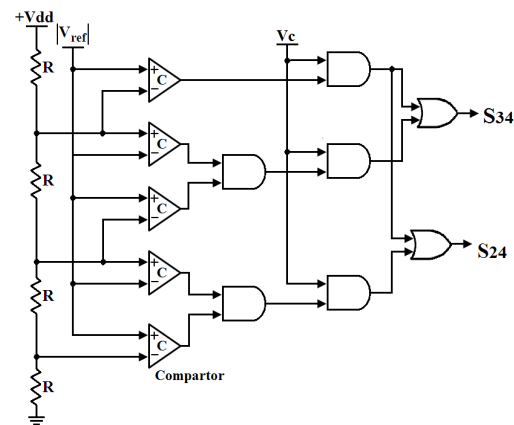


Fig. 4. 4x/3x/2x/1x selector control circuit.

- 6) If $\frac{1}{4}V_{dd} \leq |V_{ref}| < \frac{2}{4}V_{dd}$ and $V_c = 1$, then $S_{24} = 1, S_{34} = 0$;
- 7) If $0V \leq |V_{ref}| < \frac{1}{4}V_{dd}$ and $V_c = 0$, then $S_{24} = 0, S_{34} = 0$;
- 8) If $0V \leq |V_{ref}| < \frac{1}{4}V_{dd}$ and $V_c = 1$, then $S_{24} = 0, S_{34} = 0$.

With the digital logic gates, the phase generator can be easily designed to obtain a set of nonoverlapping complementary signals ϕ_1 and ϕ_2 . Based on ϕ_1 and ϕ_2 , the switch signals S1-S4, Sa and Sb can be operated just like the waveforms in Fig. 2, where the frequency of ϕ_{11} is exactly half of that of ϕ_1 , and ϕ_{12} is the antiphase signal of ϕ_{11} . Here, all detailed Boolean relationships of S1-S4, Sa and Sb are shown as follows: (“ \cdot ”: logic AND).

$$\begin{aligned}
 S1 &= \phi_1, \\
 S2 &= \phi_{11}, \\
 S3 &= \phi_2 \cdot S_{24},
 \end{aligned}$$

$$S4 = \phi_2 \cdot \phi_{12} \cdot S_{34},$$

$$S_a = \phi_2 \cdot \phi_{12} \cdot S^+ \cdot V_c,$$

$$S_b = \phi_2 \cdot \phi_{12} \cdot S^- \cdot V_c.$$

The goal is to generate these SPM control signals S1-S4, Sa and Sb for realizing phase I- IV topologies as in Fig. 3.

III. EXAMPLES

In this paper, the 2-stage 4-phase SC boost inverter is simulated by OrCAD, and then the results are illustrated to verify the efficacy of the proposed inverter. All the parameters are listed in Table I. There are 3 cases ($f_o=1.2$ kHz, 1 kHz, and 0.8 kHz), each including two different V_m , to be discussed as follows.

1) Case 1: $f_o=1.2$ kHz

a) $V_m=18.9V$:

Let the supply source V_s be DC 5V, load R_L be 500Ω , and the peak value and output frequency of V_{ref} are $V_m=18.9V$, $f_o=1.2kHz$. The waveform of V_{out} is obtained as in Fig. 5(a). V_{out} has the peak value of 18.88V, and the practical output frequency is about 1.2 kHz. The efficiency is 77%, and THD is 4%.

b) $V_m=14V$:

Let the supply source V_s be DC 5V, load R_L be 500Ω , and the peak value and output frequency of V_{ref} are $V_m=14V$, $f_o=1.2kHz$. The waveform of V_{ou}

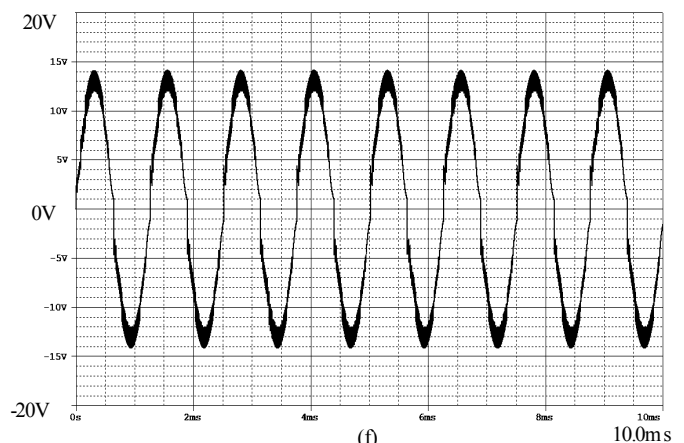
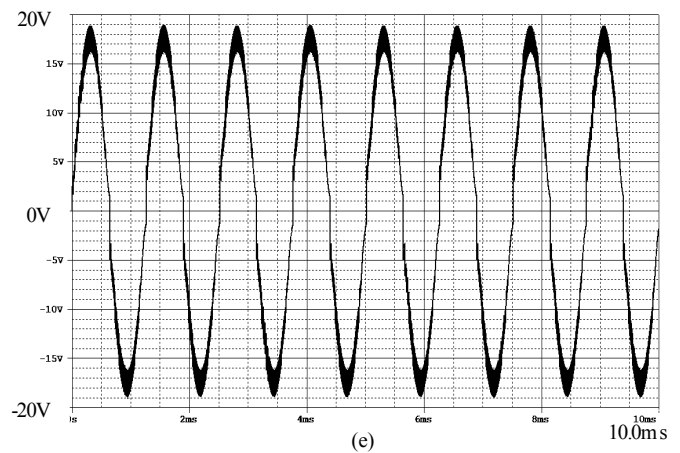
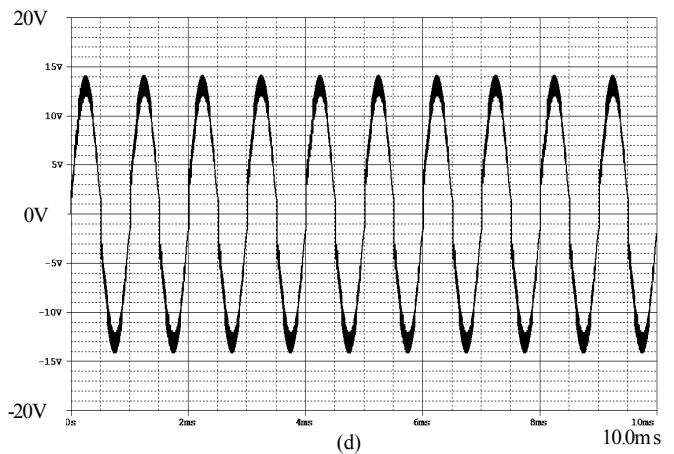
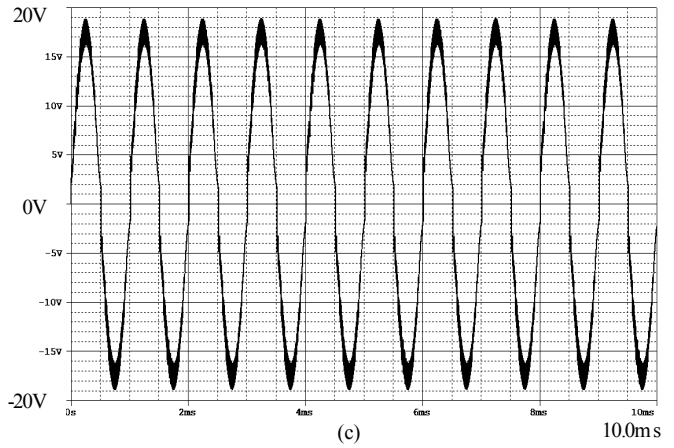
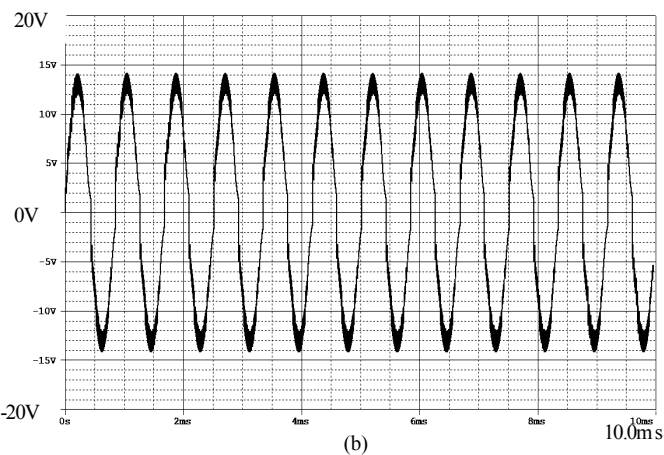
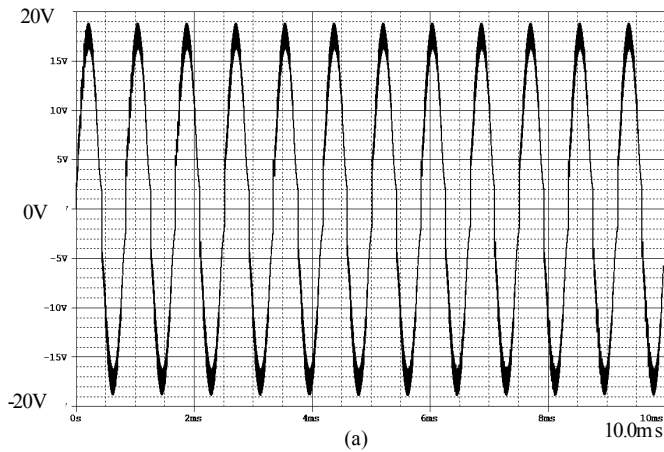


Fig. 5. Output V_{out} for V_{ref} : (a) $V_m=18.9V$, $f_o=1.2kHz$, (b) $V_m=14V$, $f_o=1.2kHz$, (c) $V_m=18.9V$, $f_o=1kHz$, (d) $V_m=14V$, $f_o=1kHz$, (e) $V_m=18.9V$, $f_o=0.8kHz$ and (f) $V_m=14V$, $f_o=0.8kHz$.

TABLE I
Components of 2-Stage 4-Phase SC boost DC-AC inverter

Supply source (V_s)	5V
Pumping capacitor ($C1, C2$)	20 μ F
Output capacitor (C_o)	0.1 μ F
Power MOSFETs	MbreakN ($W=0.5, L=2\mu$)
On-state resistor of MOSFETs	28m Ω
Diode (D)	SD41
Load resistor (R_L)	500 Ω
Switching frequency (f_s)	200kHz
Output frequency (f_o)	1.2 kHz, 1kHz, 0.8kHz

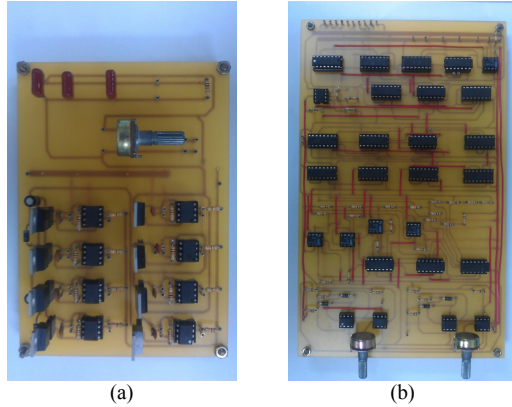


Fig. 6. Prototype circuit of the proposed inverter : (a) power part, (b) control part.

is obtained as in Fig. 5(b). V_{out} has the peak value of 14.14V, and the practical output frequency is about 1.2 kHz. The efficiency is 75%, and THD is 5.6%.

2) Case 2: $f_o=1$ kHz

a) $V_m=18.9V$:

Let the supply source V_s be DC 5V, load R_L be 500 Ω , and the peak value and output frequency of V_{ref} are $V_m=18.9V$, $f_o=1kHz$. The waveform of V_{out} is obtained as in Fig. 5(c). V_{out} has the peak value of 18.87V, and the practical output frequency is about 1 kHz. The efficiency is 77%, and THD is 4%.

b) $V_m=14V$:

Let the supply source V_s be DC 5V, load R_L be 500 Ω , and the peak value and output frequency of V_{ref} are $V_m=14V$, $f_o=1kHz$. The waveform of V_{out} is obtained as in Fig. 5(d). V_{out} has the peak value of 14.15V, and the practical output frequency is about 1 kHz. The efficiency is 74%, and THD is 5.8%.

3) Case 3: $f_o=0.8$ kHz

a) $V_m=18.9V$:

Let the supply source V_s be DC 5V, load R_L be 500 Ω , and the peak value and output frequency of V_{ref} are $V_m=18.9V$, $f_o=0.8kHz$. The waveform of V_{out} is obtained as in Fig. 5(e). V_{out} has the peak value of 18.88V, and the practical output frequency is about 0.8kHz. The efficiency is 77%, and THD is 3.8%.

b) $V_m=14V$:

Let the supply source V_s be DC 5V, load R_L be 500 Ω , and the peak value and output frequency of V_{ref} are $V_m=14V$, $f_o=0.8kHz$. The waveform of V_{out}

is obtained as in Fig. 5(f). V_{out} has the peak value of 14.15V, and the practical output frequency is about 0.8kHz. The efficiency is 77%, and THD is 5%.

According to the above results, it is obvious that V_{out} is following V_{ref} for the different output peaks and frequencies. These results show that this proposed inverter has a good closed-loop steady-state performance.

IV. CONCLUSION

A new closed-loop scheme of 2-stage 4-phase switched-capacitor (SC) boost DC-AC inverter is proposed by combining 4-phase phase generator and sinusoidal pulse-frequency-modulation (SPFM) controller for low-power step-up inversion and regulation. The advantages of the scheme are listed as follows. (i) This SC boost inverter needs no magnetic element, so IC fabrication will be promising. (ii) Here, this proposed can provide the voltage gain of $2^2 = 4$ at most just with 2 pumping capacitors. As compared with the structure of [11], this proposed inverter needs a fewer number of pumping capacitors to reach the same step-up gain. Even though using the phase number of 4 (more than that of [11]), we still get profits from the area/volume reduction due to using the fewer number of pumping capacitor. At present, we have implemented the hardware circuit of the this inverter as the photo in Fig. 6. Next, some more experimental results will be measured for the verification of this scheme.

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