

# A Sample Size Calculation of Bayesian Design for Superiority Trials with Rare Events

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**Abstract**—Traditional approaches used in sample calculation for superiority trials comparing two low proportions usually provide very large sample sizes. Furthermore, such calculations may be inaccurate due to asymptotic normality that is often assumed but may not hold in such cases. Bayesian approach could reduce sample size by integrating historical information prior to data collection. It allows also single arm design to be conducted e.g. when it would not be ethical to enroll participants into a control group. In this analysis, a 1:1 randomized two-arm Bayesian trial designed to test for superiority was compared in terms of power and Bayesian Type I error with 1) a single-arm Bayesian trial and 2) a two-arm frequentist trial. Via Monte Carlo simulations, sample sizes required and trial powers were compared for various scenarios of efficacy results, using various prior distributions. Our analysis was applied to a real-world case study in the area of a trial to test the efficacy of a strategy to reduce mother-to-child transmission of HIV.

As a result, regardless of the prior distributions used, power to detect superiority was found systematically higher with single-arm Bayesian design compared to two-arm Bayesian

design. However when the size of the effect becomes smaller, the power of a two-arm Bayesian design becomes higher than single-arm. In our case study, using the model predictive prior for the experimental arm (transmission rate decrease from 2.3% to 0.7%), power to detect superiority ( $RR < 1$ ) could reach 80% with optimistically as low as 50 subjects. In the two-arm frequentist design, using Farrington and Manning method, the power to demonstrate superiority of the experimental over control arm would be far below 80% with 350 subjects (34% power). Similarly, in a two-arm Bayesian design, the power would not reach 80% using a prior set identical to the predictive prior in the control arm or the inflated 170% coefficient of variation (CV). Finally, based on single-arm Bayesian design, power reaches 80% with 350 subjects when using the inflated 170% CV to the control arm predictive prior.

**Index Terms**—Bayesian approach, rare outcome, relative risk, superiority, historical prior

## I. INTRODUCTION

Superiority testing of a new medical treatment or new strategy over the standard of care (control) is often required for regulatory registration. When the standard of care is highly efficacious the probability of the outcome may be very low, thus a large sample size is required to demonstrate superiority. When a superiority test is based on the absolute difference, it is poorly meaningful to compare low proportions (i.e. standard of care ( $\theta_1$ ) with a new treatment ( $\theta_2$ )) when the reference  $\theta_1$  is close to zero. It is then more relevant to use relative risks and odds ratios to test for superiority since both  $\theta_1$  and  $\theta_2$  are positive numbers between 0 and 1. When the probability of the outcome is low, relative risks and odds ratios are quite similar but relative risks are easier to interpret.

Based on relative risk, Farrington and Manning [1] proposed to replace the sample proportions with the restricted maximum likelihood estimates of  $\theta_1$  and  $\theta_2$  under the null hypothesis to improve the accuracy of the sample size calculation. However, this frequentist approach is based on asymptotic normality and may be inaccurate for the risk distribution of rare event.

Bayesian methods are powerful alternatives to sample size calculation for sequential study designs. Bayesian calculations combine historical information with data to be prospectively collected [2]. Typically, historical data are only available from a control arm and act as prior information for the concurrent control. Non-informative

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prior distributions are used when prior information is not available.

The objective of the present analysis is to compare the statistical performances (power to detect superiority and Bayesian Type I error) of different clinical trial designs based on a Bayesian or frequentist framework using relative risk to determine superiority. Based on a simulation study, a two-arm Bayesian study design was compared with 1) a single-arm Bayesian design [3]; and 2) a two-arm frequentist design. The sample size calculation based on Bayesian predictive probability [4], [5] was used for Bayesian design whereas Farrington and Manning methodology was used for frequentist design.

Finally, we apply our analysis to a case study: PHPT-5 clinical trial (NCT01511237) [6], phase III clinical trial to evaluate the efficacy of an antiretroviral (ARV) intensification strategy to reduce the risk of transmission of HIV from mother to infant during labor and delivery. This clinical trial used a single-arm Bayesian design as the inclusion since a control arm was not possible for ethical reasons. Prior knowledge was obtained from historical data collected within other perinatal trials performed in the same clinical setting. The statistical power to detect superiority of the proposed strategy over the standard of care in the PHPT-5 second phase trial—a single-arm Bayesian trial—was compared to a two-arm Bayesian and to a frequentist study design.

## II. PROCEDURE FOR SAMPLE SIZE CALCULATION USING A BAYESIAN APPROACH

Suppose that in a two-arm study,  $n_{CONT}$  subjects are randomized to receive the standard treatment (active control) and  $n_{EXP}$  subjects randomized in the experimental arm. Let  $y_{CONT}$  and  $y_{EXP}$  denote the number of outcomes in the corresponding treatment groups observed over a pre-defined follow-up study period, we further assume that  $y_{CONT}$  and  $y_{EXP}$  are independent and follow binomial distribution with probability of interest  $\theta_{CONT}$  and  $\theta_{EXP}$ , respectively.

$$y_{CONT} \sim \text{Binomial}(\theta_{CONT}, n_{CONT})$$

$$y_{EXP} \sim \text{Binomial}(\theta_{EXP}, n_{EXP})$$

The sample size to demonstrate the superiority of the new strategy over standard of care was calculated under the following hypothesis:

$$H_0 : \theta_{EXP} \geq \theta_{CONT} \text{ versus } H_1 : \theta_{EXP} < \theta_{CONT}$$

$$\text{or } H_0 : RR \geq R_0 \text{ versus } H_1 : RR < R_0$$

Under  $H_0$ , we chose a relative risk  $R_0=1$ . Accordingly, the sample size to achieve 80% power can be determined. The procedure for sample size calculation based on predictive probability was as follow:

### a) Step 1: Computing the posterior distribution

For each implementation of the simulations, we assumed that the risk distribution in the control arm and in the experimental arm followed Beta distributions.

$$\hat{\theta}_{CONT} \sim \text{Beta}(a_{CONT}, b_{CONT})$$

$$\hat{\theta}_{EXP} \sim \text{Beta}(a_{EXP}, b_{EXP})$$

This is determined for each arm, based on the observed data and the prior distribution. The posterior probability distributions for each group follow a beta form as follow:

$$\tilde{\theta}_{CONT} \sim \text{Beta}(a_{CONT} + y_{CONT}, b_{CONT} + n_{CONT} - y_{CONT})$$

$$\tilde{\theta}_{EXP} \sim \text{Beta}(a_{EXP} + y_{EXP}, b_{EXP} + n_{EXP} - y_{EXP})$$

### b) Step 2: Simulating outcomes

Outcomes  $\hat{y}_{CONT}$  and  $\hat{y}_{EXP}$  to be observed were simulated from predictive distributions based on  $\theta_{CONT}$  and  $\theta_{EXP}$  given the respective sample sizes  $n_{CONT}$  and  $n_{EXP}$ :

$$\hat{y}_{CONT} \sim \text{Binomial}(n_{CONT}, \theta_{CONT})$$

$$\hat{y}_{EXP} \sim \text{Binomial}(n_{EXP}, \theta_{EXP})$$

In the single-arm design,  $n_{EXP}$  subjects enroll only in the experimental arm.

$$n_{TOTAL} = n_{EXP}$$

For the two-arm design, a 1:1 randomization scheme is considered.

$$n_{CONT} = n_{EXP} = n$$

$$n_{TOTAL} = 2n$$

### c) Step 3: Simulating posterior distributions on risk of events

In the single-arm design, the posterior outcome risk in the experimental arm,  $\tilde{\theta}_{EXP}$  was simulated, whereas the risk in the control group could only be predicted from the historical estimate ( $\hat{\theta}_{CONT}$ ).

In the two-arm design, the simulated risk for each arms are:

$$\tilde{\theta}_{CONT} \sim \text{Beta}(a_{CONT} + \hat{y}_{CONT}, b_{CONT} + n_{CONT} - \hat{y}_{CONT})$$

$$\tilde{\theta}_{EXP} \sim \text{Beta}(a_{EXP} + \hat{y}_{EXP}, b_{EXP} + n_{EXP} - \hat{y}_{EXP})$$

### d) Step 4: The relative risk prediction

For single-arm and two-arm designs, the prediction of relative risks were  $\tilde{\theta}_{EXP} / \hat{\theta}_{CONT}$  and  $\tilde{\theta}_{EXP} / \tilde{\theta}_{CONT}$ , respectively. Where  $\hat{\theta}_{CONT}$  was estimated from the historical data.

e) Step 5: Predictive power

We repeated 20,000 replicates from step (1) to step (4) to obtain the set of predicted relative risk. The prospective sample size  $n_{TOTAL}$  can demonstrate the superiority of the new strategy to the standard care if the probability of  $RR < R_0$  was higher than 80%.

III. CHOICE OF PRIOR DISTRIBUTION

The choice of the prior distribution impacts the sample size calculation. When historical data are not available, a non-informative prior is typically used for proportion parameters. Alternately, when relevant data from previous trials are available, prior distribution informed by historical data can be used [2]. A prior estimated using historical data could be used for the control arm. We investigated the performance of the designs using different sets of non-informative prior distributions for the experimental including flat prior, Beta (1, 1) and Jeffreys' prior, Beta (0.5, 0.5)[7].

We also proposed the three different historical priors for the experimental arm as follows.

1) A model predictive prior: a prior estimated through linear mixed model using historical data.

2) A prior similar to the control arm prior: a prior set identical to the control arm.

3) A prior with a 170% inflated coefficient of variation (CV) in the control arm. The CV corresponds to the standard deviation divided by the mean of the distribution of the risk. Since the CV of the model predictive prior for the control arm was assumed to at 85%, we used an inflated CV set to twice the CV of model predictive prior (170%) to reflect the hypothesis that the distribution of the risk in the experimental arm was close to the distribution of the risk in the control arm but less likely than a prior set identical to the control arm.

Shape parameters based on estimates from historical data were computed given the mean and variance [8]. For a beta density with mean  $m$  and standard deviation  $s$  the shape parameters,  $a$  and  $b$  are

$$\theta \sim \text{Beta}(a, b)$$

$$a = m \left( \frac{m(1-m)}{s^2} - 1 \right) \tag{1}$$

$$b = (1-m) \left( \frac{m(1-m)}{s^2} - 1 \right) \tag{2}$$

IV. SIMULATION STUDY

In this section, using several sets of simulated data we compared sample sizes from three designs including 1) single-arm Bayesian design, 2) two-arm Bayesian design and 3) frequentist design (Farrington and Manning method).

In the two-arm design, the sizes were set such as  $n_{CONT} = n_{EXP} = \{25, 50, 75, 100, 125, 150, 175\}$ . Therefore the total sample sizes including the control and the experimental arm in the 1:1 randomization scheme, is  $n_{TOTAL} = n_{CONT} + n_{EXP} = \{50, 100, 150, 200, 250, 300, 350\}$ . To be comparable with

the single-arm design, the sample sizes of the experimental arm  $n_{EXP}$  should be = {50, 100, 150, 200, 250, 300, 350}.

a) Evaluation of power to detect superiority

Power to detect superiority = 1-Probability ( $RR \geq 1/H_1$  is true).

Assuming that  $H_0$  was true, the true  $\theta_{CONT}$  value was 0.03 and the true  $\theta_{EXP}$  values were {0.003, 0.006, 0.015}. Various  $\theta_{EXP}$  values were used in order to evaluate power when the true effect size varies. The dataset was simulated 20,000 times assuming that the distribution of the outcome followed a binomial distribution with  $n_{CONT} = n_{EXP} = 10,000$ .

b) Evaluation of Type I error

Bayesian Type I error=Probability ( $RR < 1/H_0$  is true)

Assuming that  $H_0$  was true, true  $\theta_{CONT}$  values were {0.003, 0.006, 0.015} and the true  $\theta_{EXP}$  value was 0.03. Various  $\theta_{CONT}$  values were used to evaluate the Type I error when effect sizes differ. Using 20,000 replicates, the binomial data were simulated with  $n_{CONT} = n_{EXP} = 10,000$ .

c) Simulated historical prior

In the control arm, historical prior of risk distribution was defined with 85% CV of the true parameter assuming that some uncertainty could not be explained by using the model based tool with the historical data. A 85% CV was also assumed for the experimental arm as model predictive prior (optimistic prior).

V. CASE STUDY: MOTHER-TO-CHILD TRANSMISSION (MTCT) OF HIV

The high efficacy of current preventive strategies lead to MTCT rates as low as 2% or less. Consequently, the demonstration of the superiority of a new drug, drug combinations or strategies for the prevention of mother to child transmission (PMTCT) over an active control with already high efficacy requires large sample sizes.

PHPT-5 second phase was a single arm, Bayesian phase III clinical trial to evaluate the efficacy of an experimental strategy, i.e. ARV intensification to reduce the transmission risk during labor and delivery (*intra-partum* transmission) in women initiating ZDV+3TC+LPV/r late during pregnancy (cARV duration  $\leq 8$  weeks). The ARV intensification was defined as single dose NVP at onset of labor for women, and for neonates ZDV+3TC+NVP for 2 weeks followed by 2 weeks ZDV+3TC (experimental arm).

In our study, this designed was compared with an hypothetical two-arm design, with a control arm composed of women also initiating therapy late during pregnancy (received ZDV+3TC+LPV/r for 8 weeks or less) but who did not receive the experimental strategy, i.e. ARV intensification.

a) Historical prior

A previous analysis [9] had investigated the predictors of *intra-partum* transmission using previous perinatal trials, (PHPT-1(NCT00386230) [10], PHPT-2(NCT00398684) [11] and PHPT-5 first phase (NCT00409591) [12]).

The transmission risk was predicted using the observed data from 28 women who received combination of antiviral

therapy (cART) less than 8 weeks in these previous trials and did not receive any ARV intensification. The prediction of the model provided the prior information that was used in the clinical trial design.

The predicted risks of *intra-partum* transmission of the control arm and experimental arm were  $\hat{\theta}_{CONT} = 0.023 \pm 0.028$  and  $\hat{\theta}_{EXT} = 0.007 \pm 0.016$ , respectively.

1) *Prior distribution for control arm*

Shape parameters were computed given the means and variances using (1) and (2).

$$\hat{\theta}_{CONT} \sim \text{Beta}(0.64, 27)$$

2) *Prior distribution for experimental-arm.*

We used the model historical prior estimate for the experimental arm together with two different choices of prior including a prior set identical to the control arm and a prior with 170% inflated CV to the control arm.

VI. RESULTS

a) *Power comparison*

Table I, Table II and Table III show the power to detect superiority with the  $\theta_{EXP}$  varying as 0.003, 0.006, 0.015 compared to a  $\theta_{CONT} = 0.03$  in order to evaluate the power when the effect size varies.

TABLE I  
POWER (%) WITH  $\theta_{CONT} = 0.03$  AND  $\theta_{EXP} = 0.003$   
BASED ON VARIOUS PRIOR DISTRIBUTIONS FOR  
EXPERIMENTAL ARM AND SAMPLE SIZES.

Designs	Sample Sizes						
	50	100	150	200	250	300	350
Farrington and Manning	18	28	36	44	51	58	63
<b>Two-arm Bayesian design</b>							
Non-informative prior	45	63	74	81	85	89	91
Jeffreys' prior	67	78	85	89	91	93	94
Historical prior							
Model predictive prior	95	96	97	98	98	99	99
Same as control arm	62	72	79	84	87	90	92
170% CV control arm	82	87	90	92	94	95	96
<b>Single-arm Bayesian design</b>							
Non-informative prior	61	74	80	83	85	87	88
Jeffreys' prior	77	84	87	88	90	91	90
Historical prior							
Model predictive	95	94	94	94	94	95	94
Same as control arm	69	77	80	84	86	87	88
170% CV control arm	86	89	90	91	92	92	92

TABLE II  
POWER (%) WITH  $\theta_{CONT} = 0.03$  AND  $\theta_{EXP} = 0.006$   
BASED ON VARIOUS PRIOR DISTRIBUTIONS FOR  
EXPERIMENTAL ARM AND SAMPLE SIZES.

Designs	Sample Sizes						
	50	100	150	200	250	300	350
Farrington and Manning	16	23	29	36	41	47	52
<b>Two-arm Bayesian design</b>							
Non-informative prior	43	60	69	75	79	83	86
Jeffreys' prior	63	74	80	83	86	88	90
Historical prior							
Model predictive	89	90	92	93	95	95	96
Same as control arm	61	70	76	79	83	86	88
170% CV Control arm	79	83	86	87	90	91	92
<b>Single-arm Bayesian design</b>							
Non-informative prior	57	69	74	77	78	80	81
Jeffreys' prior	72	78	81	82	83	84	84
Historical prior							
Model predictive prior	88	87	88	88	88	88	87
Same as control arm	66	72	76	78	79	81	81
170% CV control arm	81	83	84	85	86	86	86

TABLE III  
POWER (%) WITH  $\theta_{CONT} = 0.03$  AND  $\theta_{EXP} = 0.015$   
BASED ON VARIOUS PRIOR DISTRIBUTIONS FOR  
EXPERIMENTAL ARM AND SAMPLE SIZES.

Designs	Sample Sizes						
	50	100	150	200	250	300	350
Farrington and Manning	10	13	15	18	20	22	24
<b>Two-arm Bayesian design</b>							
Non-informative prior	38	48	56	60	63	66	68
Jeffreys' prior	56	62	66	68	70	71	74
Historical prior							
Model predictive prior	71	73	75	76	78	80	80
Same as control arm	57	61	65	68	70	72	74
170% CV control arm	70	71	72	73	75	77	77
<b>Single-arm Bayesian design</b>							
Non-informative prior	48	55	58	60	61	62	62
Jeffreys' prior	61	63	64	65	65	65	65
Historical prior							
Model predictive	69	68	68	68	68	68	68
Same as control arm	58	61	62	63	63	64	65
170% CV control arm	70	68	67	67	67	67	67

Based on our simulation study, we found that when the size of the effect is large, even non-informative prior can be used when historical data are not available. However, historical prior improve the power compared to non-informative prior. Regardless the prior distributions used, the power to detect superiority ( $RR < 1$ ) was generally higher in single-arm Bayesian design compared to two-arm Bayesian design with larger effect size. In contrast, when the size of the effect was smaller, the power became higher in two-arm Bayesian design.

b) *The evaluation of Type I error based on simulation study*

Of the two non-informative priors, the flat prior produces smaller type I error than the Jeffrey's prior. Using the historical prior, model predictive prior provided the smallest Type I error followed by inflated 170% CV control arm prior and then the prior set identical to the control arm. The Type I error was generally higher for the two-arm Bayesian

design compared to the single-arm Bayesian design for all prior distributions. Patterns of Type I errors are similar regardless the effect size.

c) *Power evaluations in case study*

TABLE IV  
POWER IN CASE STUDY: MTCT OF HIV BASED ON  
VARIOUS PRIOR DISTRIBUTIONS FOR  
EXPERIMENTAL ARM AND SAMPLE SIZES.

Designs	Sample Sizes						
	50	100	150	200	250	300	350
Farrington and Manning	12	16	20	24	27	31	34
<b>Two-arm Bayesian design</b>							
Non-informative prior	32	44	49	53	56	58	59
Jeffreys' prior	51	59	64	65	66	67	68
Historical prior							
Model predictive prior	80	79	79	79	79	78	79
Same as control arm	57	61	63	65	66	66	67
170% CV Control arm	68	71	72	73	74	74	74
<b>Single-arm Bayesian design</b>							
Non-informative prior	45	55	62	64	67	69	70
Jeffreys' prior	60	68	71	73	75	75	76
Historical prior							
Model predictive prior	80	80	81	81	81	81	82
Same as control arm	62	67	70	72	74	74	76
170% CV control arm	72	75	76	77	78	78	80

Table IV shows power according to different design with sample sizes ranging from 50 to 350 and  $\hat{\theta}_{CONT}$  and  $\hat{\theta}_{EXP}$  defined as 0.023 and 0.007, respectively. The power is higher in the single-arm design using all prior distribution compared to the two-arm design. Power does not reach 80 % when using a non-informative prior or the same prior in the experimental and control arm. Using the model predictive prior for the experimental arm, power to detect superiority ( $RR < 1$ ) could reach 80% with optimistically as low as 50 subjects.

Using the Farrington and Manning method, the power to demonstrate superiority of the experimental over control arm would be far below 80% with 350 subjects (34% power only) and it would require 1,426 subjects to reach 80% power. Similarly, power could not reach 80% with 350 subjects in a two-arm design using a prior set identical to the predictive prior in the control arm or the inflated 170% CV. However, with the single-arm design using the inflated 170% CV to control arm predictive prior, the power would reaches 80% with only 350 subjects.

VII. CONCLUSION

When the effect size is large, non-informative priors can be used in the experimental arm. However, increased power could be provided by using the priors set identical to the model predictive prior of the control arm or with an inflated 170% CV. Generally, power is higher in single-arm design than in two-arm design regardless of the prior distribution when the effect size is large. In contrast, when the true effect size is smaller, power is higher in the two-arm Bayesian design.

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