# Optimal Replenishment Policy for Special Display Goods with Ramp-type Demand Rate

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Abstract—The present study discusses the retailer's optimal replenishment policy for seasonal products with a ramp-type demand pattern. In this study, we focus on "Special Display Goods", which are heaped up in end displays or special areas at retail store. They are sold at a fast velocity when their quantity displayed is large, but are sold at a low velocity if the quantity becomes small. We develop the model with a finite time horizon (period of a season) to determine the optimal replenishment policy, which maximizes the retailer's total profit. Numerical examples are also presented to illustrate the theoretical underpinnings of the proposed model.

Keywords: optimal replenishment policy, seasonal product, ramp-type demand rate, special display goods

## 1 Introduction

Inventory models with a finite planning horizon and timevarying demand patterns have extensively been studied in the inventory literature[1-7]. Resh et al.[1] and Donaldson[2] established an algorithm to determine both the optimal number of replenishment cycles and the optimal replenishment time for a linearly increasing demand pattern. Barbosa and Friedman[3] and Henery[4] respectively extended the demand pattern to a power demand form and a log-concave function. Hariga and Goyal[5] and Teng[6] extended Donaldson's work by considering various types of shortages. For deteriorating items such as medicine, volatile liquids and blood banks, Dye[7] developed the inventory model under the circumstances where shortages are allowed and backlogging rate linearly depends on the total number of customers in the waiting line during the shortage period. However, there still remain many problems associated with replenishment policies for retailers that should theoretically be solved to provide them with effective indices. We focus on a case where special display goods [8, 9, 10] are dealt in. The special display goods are heaped up in the end displays or special areas at retail store. Retailers deal in such special display goods with a view to introducing and/or exposing new products or for the purpose of sales promotions in many cases. They are sold at a fast velocity when their

quantity displayed is large, but are sold at a low velocity when their quantity becomes small. Baker[11] and Baker and Urban[12] dealt with a similar problem, but they expressed the demand rate simply as a function of a polynomial form without any practical meaning.

Traditional retailers of seasonal merchandise have to commit themselves to a single order to purchase before the beginning of the season since the most of seasonal products have a relatively long ordering lead-time[13, 14]. The retailers who deal with the seasonal merchandise have recently been able to reorder the products during the season since Quick Response (QR) system has widely been used by manufacturing industries. Quick Response is a vertical strategy where the manufacturer strives to provide products and services to its retail customers in exact quantities on a continuous basis with minimum lead times[15].

The demand of seasonal merchandise such as clothes, sporting goods, children's toys and electrical home appearances consists of the following three successive periods: in the first phase the demand rate of the product increases with time, and then its demand rate becomes steady. In the final phase the demand rate decreases with time up to the end of the selling season[16]. This type of demand is classified into a time dependant ramp-type demand pattern[16].

In this study, we develop an inventory model for seasonal products with a ramp-type demand pattern over a finite time horizon (period of a season) to determine the optimal replenishment policy, which maximizes the retailer's total profit. Numerical examples are also presented to illustrate the theoretical underpinnings of the proposed model.

### 2 Notation and Assumptions

The main notations used in this paper are listed below:

- *H*: planning horizon.
- *n*: the number of replenishment cycles during the planning horizon.
- $Q_U$ : maximum inventory level.
- $Q_j, q_j$ : the order-up-to level and the re-order point, respectively, in the *j*th replenishment cycle( $q_0 = 0$ ,

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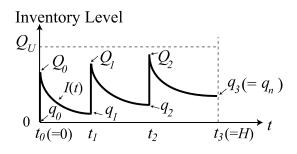


Figure 1: Transition of inventory level (n = 3)

- $$\begin{split} 0 &\leq q_j < Q_j \leq Q_U, \ j = 1, 2, \cdots, n ). \\ \text{the time of the $j$th replenishment $(t_{j-1} < t_j, t_0 = 0, $t_j > t_j = 0, $t_j > t_j = 0, $t_j > t_j = 0, $t_j < t_j < t_j = 0, $t_j < t_j < t_j < t_j = 0, $t_j < t_j <$$
   $t_j$ :  $t_n = H$ ).
- selling price per item. **p:**
- acquisition cost per item. c:
- inventory holding cost per item and unit of time. h:
- K: ordering cost per lot.
- salvage value, per item, of unsold inventory at the  $\theta$ : end of the planning horizon.
- a proportional constant of the demand rate.  $\lambda$ :
- $\mu(t)$ : demand rate, at time t, which is independent of the quantity displayed.

The assumptions in this study are as follows:

- (i) The finite planning horizon H is divided into n replenishment cycles.
- (ii) The demand rate,  $\mu(t)$ , which is independent of the quantity displayed is a time dependent ramp-type function and is of the form

$$\mu(t) = \begin{cases} \mu_1(t), & 0 \le t < \gamma_1, \\ \mu_2(t), & \gamma_1 \le t < \gamma_2, \\ \mu_3(t), & \gamma_2 \le t \le H. \end{cases}$$
(1)

We assume that  $\mu'_1(t) > 0$ ,  $\mu'_2(t) \le 0$ ,  $\mu'_3(t) < 0$ ,  $\lim_{t \to \gamma_1 = 0} \mu_1(t) = \mu_2(\gamma_1)$  and  $\lim_{t \to \gamma_2 = 0} \mu_2(t) =$  $\mu_3(\gamma_2).$ 

(iii) The demand rate is deterministic and significantly depends on the quantity displayed: the items sell well if their quantity displayed is large, but do not when their quantity displayed becomes small. We express such a behavior of special display goods in terms of the following differential equation:

$$\frac{d}{dt}m_j(t) = \lambda \left[Q_{j-1} - m_j(t)\right] + \mu(t) \qquad (2)$$

where  $m_i(t)$  denotes the cumulative quantity of the objective product sold during  $[t_{j-1}, t]$   $(t < t_{j+1})$  and  $Q_{i-1}$  signifies the order-up-to level at the beginning of the jth replenishment cycle. A mathematically identical equation has been used to express the behavior of deteriorating items and their optimal ordering policy has been obtained by Abad[17]. Under

the model proposed in this study, the demand depends on the quantity heaped and thus depends on time.

- (iv) The rate of replenishment is infinite and the delivery is instantaneous.
- (v) Backlogging and shortage are not allowed.
- (vi) The retailer orders  $(Q_j q_j)$  units when her/his inventory level reaches  $q_j$ . Figure 1 shows the transition of inventory level in the case of n = 3.

(vii) 
$$v = (p - c - h/\lambda) > 0.$$

#### **Total Profit** 3

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By solving the differential equation in Eq. (2) with the boundary condition  $m_j(t_{j-1}) = 0$ , the cumulative quantity,  $m_j(t)$ , of demand for the product at time  $t \geq t_{j-1}$ is given by

$$n_{j}(t) = Q_{j-1} \left[ 1 - e^{-\lambda(t-t_{j-1})} \right] + \int_{t_{j-1}}^{t} e^{-\lambda(t-u)} \mu(u) du.$$
(3)

Since we have  $I(t_j) = q_j$ , the inventory level of the product at time t becomes

$$I(t) = Q_{j-1} - m_j(t) = q_j e^{\lambda(t_j - t)} + \int_t^{t_j} e^{\lambda(u - t)} \mu(u) du.$$
(4)

Therefore, the initial inventory level in jth replenishment cycle is given by

$$Q_{j-1} = I(t_{j-1})$$
  
=  $q_j e^{\lambda(t_j - t_{j-1})} + \int_{t_{j-1}}^{t_j} e^{\lambda(u-t)} \mu(u) du.$  (5)

By letting  $Q_{j-1} = I(t_{j-1})$  in Eq. (3), the cumulative quantity of demand during  $[t_{j-1}, t_j)$  becomes

$$m(t_{j-1}, t_j) = q_j \left[ e^{\lambda(t_j - t_{j-1})} - 1 \right] + \int_{t_{j-1}}^{t_j} e^{\lambda(t_j - t_{j-1})} \mu(u) du.$$
(6)

There obviously exists a time  $t = t_i^U (> t_{i-1})$  when the inventory level reaches zero, where  $t_i^U$  is unique positive solution to

$$\int_{t_{j-1}}^{t_j} e^{\lambda(u-t_{j-1})} \mu(u) du = Q_{j-1}.$$
 (7)

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The left-hand-side of Eq. (7) indicates that the cumulative demand of the product in *j*th replenishment cycle when the re-order point  $q_j$  is zero. The maximum value of  $t_j$  can therefore be given by  $t_j^U$ .

On the other hand, the cumulative inventory,  $A(t_{j-1},t_j)$ , held during  $[t_{j-1},t_j)$   $(t_j \leq t_j^U)$  is expressed by

$$A(t_{j-1}, t_j) = \int_{t_{j-1}}^{t_j} I(t) dt$$
  
=  $\frac{1}{\lambda} \left[ m(t_{j-1}, t_j) - \int_{t_{j-1}}^{t_j} \mu(u) du \right].$  (8)

Hence, the total profit is given by

$$P_{n} = \sum_{j=1}^{n} \left[ p \cdot m(t_{j-1}, t_{j}) - c \cdot (Q_{j-1} - q_{j-1}) - h \cdot A(t_{j-1}, t_{j}) \right] + \theta q_{n} - nK$$
  
$$= v \sum_{j=1}^{n} m(t_{j-1}, t_{j}) + (\theta - c)q_{H} + h/\lambda \int_{0}^{H} \mu(u) du - nK, \qquad (9)$$

where  $v = (p - c - h/\lambda) (> 0)$ .

#### 4 Optimal Policy

This section analyzes the existence of the optimal policy  $(Q_{j-1}, q_j, t_j) = (Q_{j-1}^*, q_j^*, t_j^*)$  for a given n  $(j = 1, 2, \dots, n)$ , which maximizes  $P_n$  in Eq. (9). It is, however, very difficult to conduct analysis under  $\theta \neq c$ . For this reason, we focus on the case where  $\theta = c$ .

#### 4.1 Optimal Re-order Point

At retail stores, they have a maximum value for the inventory level arrowed for some reasons, which is denoted by  $Q_U$ . It can easily be shown from Eq. (5) that  $Q_{j-1}$  is a function of  $q_j$  ( $0 \le q_j < Q_{j-1} \le Q_U$ ), and furthermore,  $Q_{j-1} \le Q_U$  agrees with

$$q_j \leq e^{-\lambda(t_j - t_{j-1})} \times \left[ Q_U - \int_{t_{j-1}}^{t_j} e^{\lambda(u - t_{j-1})} \mu(u) du \right]. \quad (10)$$

Let  $R(t_{j-1}, t_j)$  express the right-hand-side of Inequality (10). We obviously have  $R(t_{j-1}, t_j) \ge 0$  for  $t_{j-1} \le t_j < \min(t_j^U, t_{j+1})$ .

By differentiating  $P_n$  in Eq. (9) with respect to  $q_j$ , we have

$$\frac{\partial}{\partial q_j} P_n = v \left[ e^{\lambda(t_j - t_{j-1})} - 1 \right] (> 0).$$
(11)

Since  $v(t_{j-1}) = [(p-c)g(t_{j-1}) - h] > 0$  from assumption (vii), we have  $\frac{\partial}{\partial q_j}P_n > 0$ , and consequently  $(Q_{j-1}^*, q_j^*) = (Q_U, R(t_{j-1}, t_j)).$ 

By letting  $(Q_{j-1}, q_j) = (Q_U, R(t_{j-1}, t_j))$  in Eq. (9), the total profit on  $(Q_{j-1}, q_j) = (Q_U, R(t_{j-1}, t_j))$  becomes

$$P_{n} = v \sum_{j=1}^{n} \left\{ Q_{U} - e^{-\lambda(t_{j} - t_{j-1})} \left[ Q_{U} - \tilde{m}(t_{j-1}, t_{j}) \right] \right\} + h/\lambda \int_{0}^{H} \mu(u) du - nK,$$
(12)

where

$$\tilde{m}(t_{j-1}, t_{j}) = \begin{cases} \int_{t_{j-1}}^{t_{j}} e^{\lambda(u-t_{j-1})}\mu_{1}(u)du, \\ t_{j-1} < t_{j} < \gamma_{1}, \\ \int_{t_{j-1}}^{\gamma_{1}} e^{\lambda(u-t_{j-1})}\mu_{1}(u)du \\ + \int_{\gamma_{1}}^{t_{j}} e^{\lambda(u-t_{j-1})}\mu_{2}(u)du, \\ t_{j-1} < \gamma_{1} \leq t_{j} < \gamma_{2}, \\ \int_{t_{j-1}}^{\gamma_{1}} e^{\lambda(u-t_{j-1})}\mu_{1}(u)du \\ + \int_{\gamma_{1}}^{\gamma_{2}} e^{\lambda(u-t_{j-1})}\mu_{2}(u)du, \\ + \int_{\gamma_{2}}^{t_{j}} e^{\lambda(u-t_{j-1})}\mu_{3}(u)du, (13) \\ t_{j-1} < \gamma_{1} < \gamma_{2} \leq t_{j}, \\ \int_{t_{j-1}}^{t_{j}} e^{\lambda(u-t_{j-1})}\mu_{2}(u)du \\ + \int_{\gamma_{2}}^{\gamma_{2}} e^{\lambda(u-t_{j-1})}\mu_{2}(u)du \\ + \int_{\gamma_{2}}^{\gamma_{2}} e^{\lambda(u-t_{j-1})}\mu_{3}(u)du, \\ \gamma_{1} \leq t_{j-1} < \gamma_{2} \leq t_{j}, \\ \int_{t_{j-1}}^{t_{j}} e^{\lambda(u-t_{j-1})}\mu_{3}(u)du, \\ \gamma_{1} \leq t_{j-1} < \gamma_{2} \leq t_{j}, \\ \int_{t_{j-1}}^{t_{j}} e^{\lambda(u-t_{j-1})}\mu_{3}(u)du, \\ \gamma_{2} \leq t_{j-1} < t_{j} \leq H. \end{cases}$$

#### 4.2 Optimal Replenishment Time

This subsection makes an analysis of  $t_j^*$  that maximizes  $P_n$ , for a given  $(t_{j-1}, t_{j+1})$ .

By differentiating  $P_n$  in Eq. (12) with respect to  $t_j$ , we have

$$\frac{\partial}{\partial t_j} P_n = v \left\{ \lambda e^{-\lambda(t_j - t_{j-1})} \left[ Q_U - \tilde{m}(t_{j-1}, t_j) \right] -\lambda Q_U e^{-\lambda(t_{j+1} - t_j)} +\mu(t_j) \left[ 1 - e^{-\lambda(t_{j+1} - t_j)} \right] \right\}$$
(14)

Let  $L(t_j)$  express the terms enclosed in braces { } in the right-hand-side of Eq. (14). Since it can easily be

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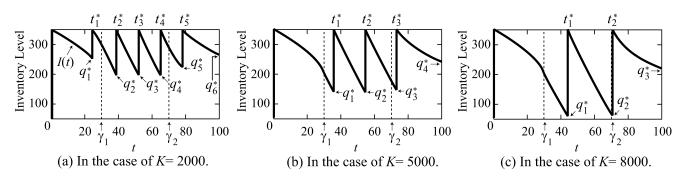


Figure 2: Sensitivity analysis

proven from assumption (vii) that the sign of v is positive,  $\frac{\partial}{\partial t_i}P_n \ge 0$  agrees with

$$L(t_j) \geq 0. \tag{15}$$

Furthermore, we have

$$L'(t_{j}) = -\lambda \left\{ \lambda e^{-\lambda(t_{j}-t_{j-1})} \left[ Q_{U} - \tilde{m}(t_{j-1}, t_{j}) \right] + \mu(t_{j}) + e^{-\lambda(t_{j+1}-t_{j})} \left[ \lambda Q_{U} + \mu(t_{j}) \right] \right\} + \mu'(t_{j}) \left[ 1 - e^{-\lambda(t_{j+1}-t_{j})} \right], \quad (16)$$

$$L(t_{j-1}) = \left[ \lambda Q_{U} + \mu(t_{j-1}) \right]$$

$$\begin{aligned} (t_{j-1}) &= & [\lambda Q_U + \mu(t_{j-1})] \\ &\times \left[1 - e^{-\lambda(t_{j+1} - t_{j-1})}\right] \ (>0), \end{aligned}$$
(17)

$$L(t_{j+1}) = -\lambda \left\{ e^{-\lambda(t_{j+1}-t_{j-1})} \tilde{m}(t_{j-1}, t_{j+1}) + Q_U \left[ 1 - e^{-\lambda(t_{j+1}-t_{j-1})} \right] \right\} (<0), \quad (18)$$

$$L(t_{j}^{U}) = \mu(t_{j}^{U}) \left[ 1 - e^{-\lambda(t_{j+1} - t_{j}^{U})} \right] -\lambda Q_{U} e^{-\lambda(t_{j+1} - t_{j}^{U})}.$$
(19)

In the case of  $t_{j+1} \ge t_j^U$ ,  $L(t_j^U) < 0$  coincides with

$$t_{j+1} < \frac{1}{\lambda} \ln \frac{\lambda Q_U + \mu(t_j^U)}{\mu(t_j^U)} + t_j^U.$$
 (20)

Let us denote, by  $\varphi(t_j^U)$ , the right-hand-side of Inequality (20).

It can easily be shown from Eq. (16) that  $L'(t_j) < 0$  in the case of  $t_j \ge \gamma_1$  since we have  $\mu'_2(t_j) \le 0$  and  $\mu'_3(t_j) < 0$ . In the case of  $t_j < \gamma_1$ , in contrast, the sign of  $L'(t_j)$  may possibly be positive since  $\mu'_1(t_j) > 0$ . The analysis with respect to existence of  $t_j^*$  becomes considerably complicated under  $L'(t_j) > 0$  for  $t_j < \gamma_1$ . For this reason, when  $t_j < \gamma_1$ , we focus on the case where

$$\mu_1'(t_j) < rac{\lambda}{1-e^{-\lambda(t_{j+1}-t_j)}}$$

$$\times \left\{ \lambda e^{-\lambda(t_j - t_{j-1})} \left[ Q_U - \tilde{m}(t_{j-1}, t_j) \right] + \mu_1(t_j) + e^{-\lambda(t_{j+1} - t_j)} \left[ \lambda Q_U + \mu_1(t_j) \right] \right\}.$$
 (21)

On the basis of the above results, for a given  $(t_{j-1}, t_{j+1})$ , we show below that an optimal replenishment time  $t_j^*$ exists:

(1)  $t_{j+1} < \varphi(t_j^U)$ :

In this subcase, the sign of  $\frac{\partial}{\partial t_j} P_n$  changes from positive to negative only once, and thus there exists a unique finite  $t_j^*$   $(t_{j-1} < t_j^* < \min(t_j^U, t_{j+1}))$  that maximizes  $P_n$ .

(2)  $t_{j+1} \ge \varphi(t_j^U)$ :

In this subcase,  $P_n$  is non-decreasing in  $t_j$ , and consequently we have  $t_j^* = t_j^U$ .

If there exists  $t_j^* < t_j^U$  for all  $j = 1, 2, \dots, n-1$ , the total profit is given by

$$P_{n} = \tilde{v} \left\{ \frac{1}{\lambda} \sum_{j=1}^{n-1} \left[ \lambda Q_{U} + \mu(t_{j}^{*}) \right] \left[ 1 - e^{-\lambda(t_{j+1}^{*} - t_{j}^{*})} \right] \\ m(t_{n-1}^{*}, H) \right\} + h/\lambda \int_{0}^{H} \mu(u) du - nK.$$
(22)

#### 5 Numerical Examples

This section presents numerical examples to illustrate the proposed model.

Suppose that the demand rate which is independent of the quantity displayed is given by

$$\mu(t) = \begin{cases} \alpha e^{\beta t}, & t < \gamma_1, \\ \alpha e^{\beta \gamma_1}, & \gamma_1 \le t < \gamma_2, \\ \alpha e^{\beta(\gamma_1 + \gamma_2 - t)}, & t \ge \gamma_2, \end{cases}$$
(23)

where  $\alpha > 0$  and  $\beta > 0[16]$ .

Figure 2 reveals the transition of inventory level along with behavior of  $(q_j^*, t_j^*)$  in the case of  $(H, Q_U, \lambda, p, c, h, \theta, \alpha, \beta, \gamma_1, \gamma_2) = (100, 350, 0.01, 600, 30$ 0, 1, 300, 0.1, 0.15, 30, 70) for K = 2000, 5000, 8000.

It is observed in Fig. 2 that the number of replenishment cycles decreases with increasing K. This is because when the ordering cost per lot becomes large, the total ordering cost should be slashed by means of increasing the time interval between replenishments.

We can also notice in Fig. 2 that  $q_j^*$  takes a constant value on the whole in the region of  $\gamma_1 < t \leq \gamma_2$ . In contrast, in the regions of  $t < \gamma_1$  and  $t \geq \gamma_2$ , the value of  $q_j^*$  relatively becomes larger, which signifies that, in these regions, the cumulative quantity displayed increases as the demand rate which is not affected by the inventory level decreases. Heaping up the products to a large quantity reflects the situation where the demand velocity is large. When the demand rate becomes small, the retailer can therefore maintain her/his profit as large as possible by increasing the quantity displayed.

# 6 Conclusions

In this study, we have proposed an inventory model for seasonal products with the ramp-type demand pattern over a finite time horizon (period of a season) to determine the optimal replenishment policy, which maximizes the retailer's total profit. We particularly focus on the case where the retailer is facing her/his customers' demand by dealing in the special display goods. They are sold at a fast velocity when their quantity displayed is large, but are sold at a low velocity if the quantity becomes small. We have clarified the existence of the optimal order quantity at time  $t_i$ , along with the optimal replenishment time which maximize the retailer's total profit. In the real circumstances, retailers frequently place a mirror at their display area, or they display products on a false bottom to increase their quantity displayed in appearance. Taking account of such factors is an interesting extension.

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