

Selection of Multiphase Governmental Projects, Related Contractors and Master Planning under Fuzzy Environment

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Abstract— Portfolio optimization is one of the most important problems in organizations. In this regard managers face to many decision making problems. In governmental dimensions they often engage with multiphase projects in which three major problems arise: selecting the best projects, selecting qualified contractors, budgeting and scheduling the projects according to the constraints. In this paper we propose a method for selecting multiphase projects, assigning the most qualified contractor to each phase, determining financial strategies and scheduling the selected projects to maximize net present value (NPV).

In this proposed method firstly contractors that have not minimal qualifications are eliminated from consideration, then closeness coefficient of contractors to each phase of projects will be computed by Fuzzy TOPSIS method and finally these coefficients as a successful indicators of each contractor will be fed in to a linear programming model to select most profitable projects, related contractors, budgeting and scheduling the projects with respect to the constraints.

Index Terms— Project selection, contractor selection, Fuzzy TOPSIS, mixed integer linear programming.

I. INTRODUCTION

Selecting most profitable projects is an important and prevalent activity in many organizations. Project selection is a process of selecting one or more promising project within some limitations while corporate goals or objectives are satisfied. Project selection, generally is limited by available resources such as capital research talent, laboratory space, lack of equipments, etc. Often in governmental dimensions we face with multiphase projects in which each phase requires especial knowledge and abilities such as feasibility study, construction, etc.

In the past decades, a variety of decision models have been developed to support the project selection. Recently, decision support systems (DSS) have been developed and used for project selection [6,13,15,16,23].

An integrated DSS has been proposed for R&D project selection [10]. It uses scoring method for project screening, AHP for criterion weight, Delphi for collecting information on requirements, ILP with heuristics for resource allocation, and NPV for analysis of benefit interactions. A DSS [6] has been developed that uses linear goal programming (LGP) and AHP methods to integrate multiple objectives into a single

objective, and Integer LP to maximize the overall objective of the portfolio.

Nowadays most of project owners especially in the public sector tend to outsource their projects. Thus contractors play a major role in such projects. The selection process should embrace investigation of contractors' potential to deliver a service of acceptable standard, on time, and within determined budget. Some methods are used for selecting contractors in order to award public projects are based on the principle of acceptance of the lowest bid price [20,17]. An integrated hierarchical method has been developed for construction contractor selection [25]. In this paper it takes in to consider many criteria such as organizational expertise, ability to timely complete projects, financial status and workloads to rank contractors in construction context. In many papers, contractor selection has been considered independent on project selection process [25,24,9].

From outsourcing view, some criteria should be considered in project and contractor selection. For example we will screen out projects that we haven't any related contractor for them or contractors requested to do have a high risk rate to complete that project. Also from this viewpoint some limitations may be added to decision process. For example work load of projects selected in especial field shouldn't be more than capacities of selected contractors. Thus it seems that it is essential to provide a method for solving project and contractor selection simultaneously. From a practical view point we cannot select projects and related contractors neglecting the available resources in any time. Thus it seems essential to consider budgeting and scheduling of the projects during the selection process.

II. PROPOSED METHOD

In this paper a method is proposed which utilizes both qualitative and quantitative data to select multiphase projects, related contractors and scheduling the selected projects. Contractor dependent criteria such as contractor experiences in that field, having related experts and necessary equipments, success rate of contractor in similar projects, finishing similar projects timely, and innovation are used in fuzzy TOPSIS method to calculate closeness coefficient of each contractor to each phase under each criterion. Also contractor independent criteria in project selection such as NPV are used in a linear programming model to select most profitable projects with respect to the constraints. This linear model besides assigning each phase to the most qualified contractor will determine the scheduling of each project according to some constraints such as available budget and equipment and work load of each selected contractors.

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In this paper firstly those of contractors that have not minimal qualifications are screened out. For example applicators that haven't any related experiences or applicators whose cash credit is less than expected amount are eliminated from consideration. As a result, a list of promised projects and qualified contractors would be available. To assess each contractor's abilities in each phase of project fuzzy TOPSIS method is used. The inputs of this stage are the importance of the criteria and the rating of the contractors in each phase of project under each criterion. These two categories of data are evaluated by decision makers in terms of linguistic variables. Then the fuzzy TOPSIS steps are followed to find the closeness coefficient (CC) of each contractor-phase of project. These closeness coefficients can be considered as indicators to show the probability of contractor's success in each phase of project. Finally these coefficients will be fed in to a linear programming to select most profitable projects and related contractors with respect to the constraints. In this step some economic characteristics of each project, closeness coefficient of each contractor-projects and some constraints such as budget available and strategic limitations are taken into consideration.

The proposed method tries to select projects and related contractors in three phases:

Phase 1: prequalification

Step1: Make a list of promised projects and split projects to phases.

Step2: Make an appraisal about the duration of each phase.

Step3: Make a list of applicator contractors. These contractors can apply for one or more phases in one or more projects.

Step4: Contractors prequalification. Eliminate some contractors that haven't minimal qualifications.

Phase 2: Compute the closeness coefficient (CC) of each contractor-phase of project

Step1: Determine decision maker committee for each category.

Step3: Determine project and contractor selection criteria.

Step4: Determine fuzzy positive-ideal solution (FPIS) and fuzzy negative-ideal solution (FNIS) for each criterion.

Step5: Choose the appropriate linguistic variables for the importance weight of the criteria and the linguistic ratings for alternatives with respect to criteria.

Step6: Assess the importance \tilde{w}_j of criterion C_j by decision-makers, using linguistic variables.

Step7: Evaluate the rating of each contractor in each phase of project under each criterion by decision-makers, using the linguistic variables.

Step8: Convert the linguistic evaluation into triangular fuzzy numbers to construct the fuzzy decision matrix with fuzzy weight of each criterion.

Step9: Pool the decision makers' opinions to get the aggregated fuzzy weight \tilde{w}_j of criterion C_j and to get the aggregated fuzzy rating \tilde{x}_{ij} of contractor A_i under criterion C_j in phase P_{mn} . Then the importance of the criteria and the rating of alternatives with respect to each criterion can be calculated as

$$\tilde{w}_j = \frac{1}{K} [\tilde{w}_{j1}(+) \tilde{w}_{j2}(+) \dots (+) \tilde{w}_{jk}] \quad (1)$$

Where \tilde{w}_{jk} is the importance weight of the k^{th} decision maker.

Also the aggregated rating \tilde{x}_{ij} of each contractor-project under criterion C_j can be calculated as

$$\tilde{x}_{ij} = \frac{1}{K} [\tilde{x}_{ij1}(+) \tilde{x}_{ij2}(+) \dots (+) \tilde{x}_{ijk}] \quad (2)$$

Where \tilde{x}_{ijk} is the rating of the k^{th} decision maker.

Step10: Construct the normalized fuzzy decision matrix. If we describe the linguistic variables by triangular fuzzy numbers, $\tilde{x}_{ij} = (a_{ij}, b_{ij}, c_{ij})$ and $\tilde{w}_{ij} = (w_{j1}, w_{j2}, w_{j3})$ then we can obtain the normalized fuzzy decision matrix denoted by \tilde{R} , and $\tilde{R} = [\tilde{r}_{ij}]_{m \times n}$. B and C are the set of benefit criteria and cost criteria, respectively, and

$$\tilde{r}_{ij} = (\frac{a_{ij}}{c_j^*}, \frac{b_{ij}}{c_j^*}, \frac{c_{ij}}{c_j^*}), j \in B; \quad (3)$$

$$\tilde{r}_{ij} = (\frac{a_j^-}{a_{ij}}, \frac{a_j^-}{b_{ij}}, \frac{a_j^-}{c_{ij}}), j \in C; \quad (4)$$

$$c_j^* = \text{Max}_i C_{ij} \quad j \in B; \quad (5)$$

$$a_j^- = \text{Min}_i a_{ij} \quad j \in C; \quad (6)$$

Step11: Construct the weighted normalized fuzzy decision matrix. We can construct the weighted normalized fuzzy decision matrix as

$$\tilde{V} = [\tilde{v}_{ij}]_{m \times n}, i=1,2,\dots,m, j=1,2,\dots,n$$

Where $\tilde{v}_{ij} = \tilde{r}_{ij}(\cdot) \tilde{w}_j$.

Step12: Calculate the distance of each contractor-phase of project from FPIS and FNIS, in each criterion. We can define the fuzzy positive-ideal solution (FPIS, A^+) as $A^+ = (\tilde{v}_1^+, \tilde{v}_2^+, \dots, \tilde{v}_n^+)$ and fuzzy negative-ideal solution (FPIS, A^-) as $A^- = (\tilde{v}_1^-, \tilde{v}_2^-, \dots, \tilde{v}_n^-)$, Where $\tilde{v}_j^+ = (1,1,1)$ and $\tilde{v}_j^- = (0,0,0)$, $j=1,2,\dots,n$. The distance of each alternative from A^+ and A^- can be currently calculated as

$$d_i^+ = \sum_{j=1}^n d(\tilde{v}_{ij}, \tilde{v}_j^+), \quad i = 1,2,\dots, m \quad (7)$$

$$d_i^- = \sum_{j=1}^n d(\tilde{v}_{ij}, \tilde{v}_j^-), \quad i = 1,2,\dots, m \quad (8)$$

Where $d(\cdot, \cdot)$ is the distance measurement between two fuzzy numbers.

Step13: Calculate the closeness coefficient (CC) of each contractor-phase of project in each criterion. The closeness coefficient of each alternative is calculated as

$$CC_i = \frac{d_i^+}{d_i^- + d_i^+}, \quad i = 1,2,\dots, m \quad (9)$$

Phase 3: Selecting the best projects and related contractors

Step1: Determine the selection limitations.

Step2: Determine quantitative criteria for project selection.

Step3: Model of the problem as a mathematical programming.

Mathematical Model:

Sets

- i index for project, for all $i=1,2,\dots,p$
- j index for phase, for all $j=1,2,\dots,N_i$
- t index for time period, for all $t=1,2,\dots,N_{per}$
- k index for contractor, for all $k=1,2,\dots,N_c$
- l index for loan type, for all $l=1,2,\dots,L$

Objective function

- z Net present value to be maximized

Parameters

- CF_{ij}^- Negative cash flow of phase j of project i (cost).
- CF_{ij}^+ Positive cash flow of phase j of project i (profit)
- M_{ij} Minimal expected cash credit for phase j of project i
- D_{ij} Duration of phase j of project i
- C_k Cash credit of contractor k
- cc_{ijk} Closeness coefficient of contractor k to phase j of project i
- $comp_{ijk}$ 1 if contractor k can be assigned to phase j of project i , otherwise 0.
- α_t Constant for maximum value of loaning in period t .
- B Total available budget
- N_p Number of projects
- N_{per} Number of periods
- N_c Number of contractors
- n_l Number of period for paying back of loan type l .
- r Interest rate
- r_l Interest Rate of loan type l .
- rs Interest Rate of alternate investment

Variables

- X_{ijkt} Binary variable, 1 if contractor k is assigned to phase j of project i during time period t , otherwise 0.
- w_{ijkt} Binary variable, 1 if contractor k starts phase j of project i during time period t , otherwise 0.
- Z_i Binary variable, 1 if project i is selected, otherwise 0.
- z_{lt} Binary variable, 1 if loan type l is selected in period t , otherwise 0.
- cm_{ij} Completion time of phase j of project i
- I_t Investment for period t
- lo_{lt} amount of loan with type of l in period t .
- PB_t amount of Loan Pay Backs in period t .

$$\text{Maximize } z = \sum_{t=1}^{N_{per}} (P/F, R\%, T) \left[\sum_{k=1}^{N_c} \sum_{i=1}^{N_p} \sum_{j=1}^{N_i} [CC_{ijk} CF_{ij}^+ + (1 - CC_{ijk}) CF_{ij}^-] (F/P, r\%, t) w_{ijkt} \right] \quad (10)$$

$$x_{ijkt} \leq comp_{ijk} \quad \forall i = 1 \dots p; \forall j = 1 \dots N_p; \forall k = 1 \dots N_c; \forall t = 1 \dots N_{per} \quad (11)$$

$$\sum_{i=1}^p \sum_{j=1}^{N_p} M_{ij} x_{ijkt} \leq C_k; \quad \forall k = 1 \dots N_c; \forall t = 1 \dots N_{per} \quad (12)$$

$$w_{ijkt} \geq x_{ijkt} - x_{ijkt-1} \quad \forall i = 1 \dots p; \forall j = 1 \dots N_p; \forall k = 1 \dots N_c; \forall t = 1 \dots N_{per} \quad (13)$$

$$w_{ijkt} \leq x_{ijkt} \quad (14)$$

$$w_{ijkt} \leq 3 - (x_{ijkt} + 2x_{ijkt-1}) \quad (15)$$

$$\sum_{j=1}^{N_p} \sum_{k=1}^{N_c} x_{ijkt} \leq 1 \quad \forall i = 1 \dots p; \forall t = 1 \dots N_{per} \quad (16)$$

$$cm_{ij} \geq cm_{ij-1} + D_{ij} \sum_{k=1}^{N_c} \sum_{t=1}^{N_{per}} x_{ijkt} \quad \forall i = 1 \dots p; \forall j = 1 \dots N_p \quad (17)$$

$$\sum_{k=1}^{N_c} \sum_{t=1}^{N_{per}} x_{ijkt} = Z_i D_{ij} \quad \forall i = 1 \dots p; j = 1 \dots N_p \quad (18)$$

$$cm_{ij} = \sum_{k=1}^{N_c} \sum_{t=1}^{N_{per}} w_{ijkt} (t + D_{ij} - 1) \quad \forall i = 1 \dots p; \forall j = 1 \dots N_p \quad (19)$$

$$\sum_{k=1}^{N_c} \sum_{t=1}^{N_{per}} w_{ijkt} \leq 1 \quad \forall i = 1 \dots p; \forall j = 1 \dots N_p; \quad (20)$$

$$\sum_{k=1}^{N_c} \sum_{t=1}^{N_{per}} \sum_{j=1}^{N_i} CF_{ij} (F/P, r\%, t) w_{ijkt} = I_t \quad \forall t = 1 \dots N_{per} \quad (21)$$

$$lo_{lt} \leq z_{lt} \alpha_t \quad \forall l = 1 \dots L; \forall t = 1 \dots N_{per} \quad (22)$$

$$\sum_{l=1}^L z_{lt} \leq 1; \quad \forall l = 1 \dots L; \forall t = 1 \dots N_{per} \quad (23)$$

$$PB_t = \sum_{l=1}^L \sum_{i=t-n_l}^t lo_{lt} (A/P, r_l\%, n_l) \quad \forall t = 1 \dots N_{per} \quad (24)$$

$$\sum_{t=1}^{N_{per}} \left(I_t - \sum_{l=1}^L lo_{lt} + PB_t \right) (P/F, rs\%, t) \leq B \quad (25)$$

$$x_{ijkt}, y_{ijt}, w_{ijkt}, Z_i, z_{lt} \in \{0, 1\} \quad (26)$$

$$cm_{ij}, I_t, lo_{lt}, PB_t \geq 0; \quad (27)$$

Equation (10) denotes the objective function that is the NPV to be maximized. Closeness coefficients of contractor-phase have been used in objective function to take contractors capabilities into consideration. It should be noted that cash flows of phases of projects have been calculated according to present circumstances, thus they should be converted to future value with inflation rate consideration. Also it is supposed that cash flows of each phase are related to the first period of starting the phase.

Constraint (11) denotes that only a qualified contractor can be assigned to a phase. This parameter will be determined at the prequalification step of the proposed approach. Constraint (12) ensures that projects will not be assigned to a contractor whose cash credit is less than the total minimal expected cash credit for these projects. Constraints (13), (14) and (15) are related to determination of phases' start time.

Constraint (16) ensures that only one contractor is assigned to one phase of a project at each time period. Constraint (17) is related to sequencing of phases and Constraint (18) determines duration of each phase. Completion time of each phase is calculated by constraint (19). Constraint (20) ensures that each phase of projects starts only once. Investment strategy is determined by constraint (21). Constraint (22) limits amount of loan to predetermined parameter α_t in each period. It is supposed in this paper that each kind of loan can be selected at most once. This supposition is reflected in constraint (23). Constraint (24) calculates paybacks of each

kind of loan. Constraint (25) is to limit investments to total available budget. Constraint (26) and (27) provide the decision variable definition.

The proposed model is a single objective mixed integer linear model whose parameters are deterministic. By the use of this model managers would be able to select the most profitable projects, assign the most qualified contractors to each selected project, make decision on financial strategies and budgeting and schedule projects according to organizational goals and constraints. Fig.1 illustrates outputs of a numerical case. In this case there are 5 promising projects which should be completed in time horizon with 40 periods. Also there are 13 applicier contractors; five of them remained for further evaluations after prequalification phase. Table I shows number of phases in each promising project and related duration.

	Phase 1	Phase 2	Phase 3	Phase 4
Project 1	5	3	5	4
Project 2	6	3	5	5
Project 3	6	4	6	-
Project 4	5	4	-	-
Project 5	4	5	4	3

It can be observed that three projects are selected by the proposed approach, project 1, project 3 and project 4. Also a contractor is assigned to each phase of project and there is no assignment to contractors 1 and 4. All selected projects will be completed at the end of 36th period.

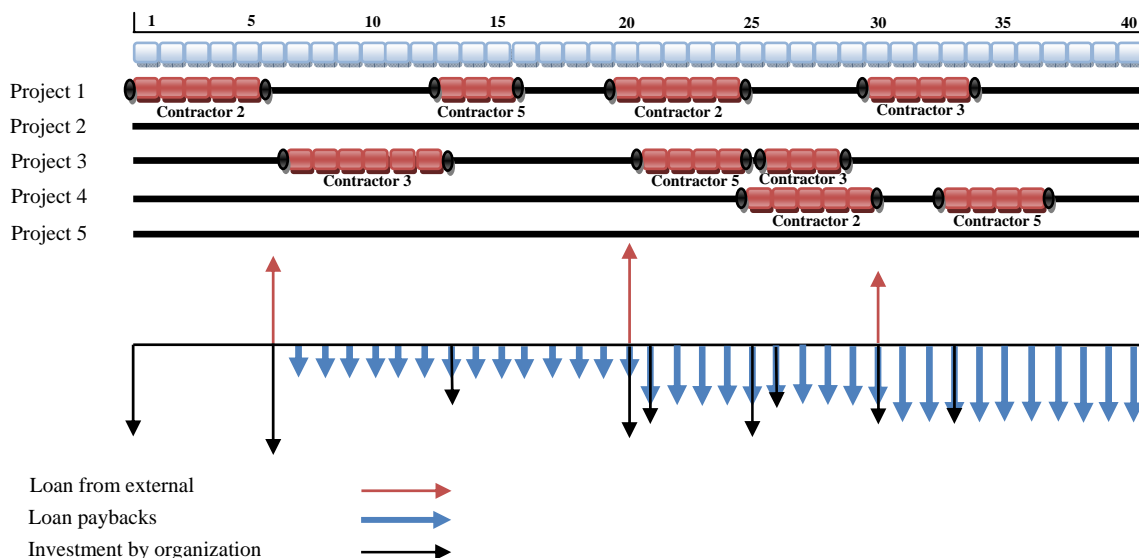


Fig.1. Schematic results of the numerical example

Cash flows of projects have been illustrated in this figure as well. It can be observed that first and second phase of the project 1 are fully funded by the organization, while in two last phases only a part of budget is funded by organization and loans from external institutions are taken to complete needed investment. Other financial decisions can be seen in

this figure.

Some advantages of the proposed approach could be as follows:

1. Selecting projects with respect to contractors' capabilities and equipments.
2. This method considers both qualitative and quantitative criteria.
3. This method considers closeness coefficients of each contractor- phase as an index to reducing failure risk rate of each project.
4. The proposed method considers budgeting and scheduling of projects during selection process.
5. Integrated decision making is one of the most important features of the proposed approach.

III. CONCLUSION

In this paper we proposed a method for project and contractor selection, budgeting and scheduling the selected projects for multi phase projects. This method tries to select most profitable projects as well as their related contractors with respect to budgetary and strategic constraints. The proposed method uses fuzzy TOPSIS to find closeness coefficient (CC) of each contractor for each project phase in specified criteria. Afterward CC's are used in a mixed integer linear model to minimize the failure risk rate of each project. The proposed method adopts an integrated approach for project and contractor selection. This method uses both qualitative and quantitative data in decision making process and can be simply implemented in organizations involved in any kind of projects.

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