

The Modified Bidimensional Empirical Mode Decomposition for Color Image Decomposition

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Abstract— This paper presents two proposed approaches to color image decomposition with Bidimensional Empirical Mode Decomposition (BEMD) technique. The first one applies the BEMD on each channel separately and the second is based on interpolation of each channel in the sifting process. The application of the two methods shows the same performance of each approach in terms of PSNR and visual quality, but they do not provide the same results in execution time which presents the most important criterion in real time applications. It was shown that the second BEMD approach based on interpolation of each channel in the sifting process, gives a gain in the point of view the execution time.

Index Terms— BEMD, IMF, Color image, interpolation, PSNR

I. INTRODUCTION

Color is one of the most basic important tools for object discrimination by human observers. But since a few years, it is generated large amounts of color images with easy use and treatment in the field of digital image processing [1]. In the last years, we have noted a rapid and enormous transition from grayscale images to color ones. Today, we are exposed to color images on many fields for example the photographs, television, computer displays and cinema movies, where color image have an important role in the advertising and dissemination of information throughout the media.

Among the methods of image decomposition existing in the literature for example wavelet [2], Empirical Mode Decomposition (EMD) [3] is a flexible technique of signal decomposition. The basic idea is to decompose a signal into a sum of components, each of is a zero mean waveform, modulated in amplitude and frequency. It has a self-adaptive nature that enables it to identify changes in the signal, whether in terms of amplitude or frequency.

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Research proved that it is a very powerful tool for adaptive multi-scale analysis of non-stationary and nonlinear signals and took a place among the best known decomposition filters.

It is an extension to two-dimensional case, helped to develop new approaches for processing and analyzing multi-scale images and its use has led to better results than other decomposition techniques [4]. The BEMD (Bidimensional EMD) is particularly suitable for texture analysis. Huang et al. compare their results with those obtained by methods based on wavelet decomposition or Gabor Transforms, or diffusion [2] and show that the BEMD method is similar to nonlinear filtering depending of time and is self-adaptive.

Interpolation is an important issue both in the field of image signal for the estimation and the extraction of the IMF's from extremas. Different procedures can be used to calculate average envelope [3]. A natural extension of cubic splines for image is the thin-plate that is a special case of the basic interpolation functions for radial basis (RBF), however we could use other functions as a function of basis for the RBF.

In this paper, we propose an extension of the BEMD color images decomposition with two techniques: the first applies the BEMD on each channel separately, and recombines the three decomposition components of the image. The second technique is based on interpolation of each channel in the sifting process and the different IMFs are obtained after the summation interpolation images. The experimental part includes a comparative study of these two techniques at the base of computing time and the quality of the reconstructed image.

The rest of this paper is organized as follows: Section 2 gives a brief overview of the BEMD process. Section 3 describes the two modified approaches of color image decomposition. Then the paper continues with Section 4 which contains the experimental results and discussions. Finally, Section 5 concludes the paper.

II. BIDIMENSIONAL EMPIRICAL MODE DECOMPOSITION

EMD is an adaptive decomposition of signals [5], introduced by Huang [3] for one dimensional data and then extended to Bidimensional signals [2].

The novel BEMD approach is either a highly adaptive decomposition [6]. It is based on the characterization of the image with this decomposition in Intrinsic Mode Function (IMF) where the image can be decomposed into a redundant set of composite images called IMF and a residue. Adding

all the IMFs with the residue reconstructs the original image without distortion or loss of information. An IMF is characterized by two specific properties [7]:

- The number of zero crossing and the number of extremas points is equal or differs only by one.
- It has a zero local mean.

The algorithm is described as follows [8]:

1. Initialization: $r_0 = A_0$ (the residual) and $k = 1$ (index number of IMF)

2. Extraction of the k^{th} IMF : $I_k(m,n)$

a. Initialization: $E_0(m,n) = r_{k-1}(m,n)$ and $j = 1$

b. Extract the local extremas of $E_{j-1}(m,n)$ (minima and maximum)

c. Interpolate the local extremas to construct the upper and the lower envelope respectively $Envmin_{j-1}(m,n)$ and $Envmax_{j-1}(m,n)$

d. Calculate the average of the two envelopes:

$$m_{j-1}(m,n) = \frac{Envmin_{j-1}(m,n) + Envmax_{j-1}(m,n)}{2} \quad (1)$$

e. Update :

$$E_j(m,n) = E_{j-1}(m,n) - m_{j-1}(m,n) \quad (2)$$

f. Calculate the stopping criterion

$$SD(j) = \frac{1}{N} \sum_{t=0}^T \left[\frac{(E_{j-1}(m,n) - E_j(m,n))^2}{E_{j-1}^2(m,n) + \xi} \right] \quad (3)$$

Where ξ is a term (low) to eliminate possible division by zero.

g. Decision: Repeat steps (b) to (f) until $SD_i \leq SD_{max}$,

and then put

$$I_k(m,n) = E_j(m,n)$$

3. Update residual

$$r_k(m,n) = r_{k-1}(m,n) - I_k(m,n) \quad (4)$$

4. Repeat steps 1-3 with $j = j + 1$ until the number of extremas in r_j is less than 2.

The sum of all modes, added to the residual component reconstructs the original image [7]:

$$A(m,n) = \sum_{k=1}^K I_k(m,n) + r(m,n), k \in N^* \quad (5)$$

III. THE MODIFIED BEMD APPROACH TO COLOR IMAGE DECOMPOSITION

Color images consist of three channels, such as red (R), green (G), and blue (B) channels. Thus, a color image can be viewed as a combination of three images channel [9].

If we consider a color image of size (256x256x3), image contains 65,536 pixels in total, and since we have three values for each pixel, the decomposition of such image directly by BEMD will very costly in execution time.

The color image can transformed into three channels R, G and B. So in this case, one applies the BEMD approach for each channel.

In this paper, we propose two possible approaches to BEMD color image decomposition:

The first approach is to apply the BEMD on each channel separately. We obtained a set of IMF in each channel and with the summation of this IMFs and the residue, we can be found the reconstructed image for each channel. With the summation of three reconstructed image for each channel we obtained the result image. The process decomposition approach with the first approach of BEMD is illustrated in Figure 1.

In the second approach we apply the BEMD approach in each channel separately. But in the interpolation phase, the three interpolated images are combined in a single interpolated image (reconstructed according RGB channels of color images). Then the BEMD approach is continued until extract all the IMFs and the residue, and finally the reconstructed image. The process of the second BEMD of color image decomposition is illustrated in Figure 2.

Another way, in the second approach we collect the three channels just after the interpolation step. So until the interpolation the two approaches are the same, why we can say that both approaches are mathematically equivalents and as a result they give the same visual quality.

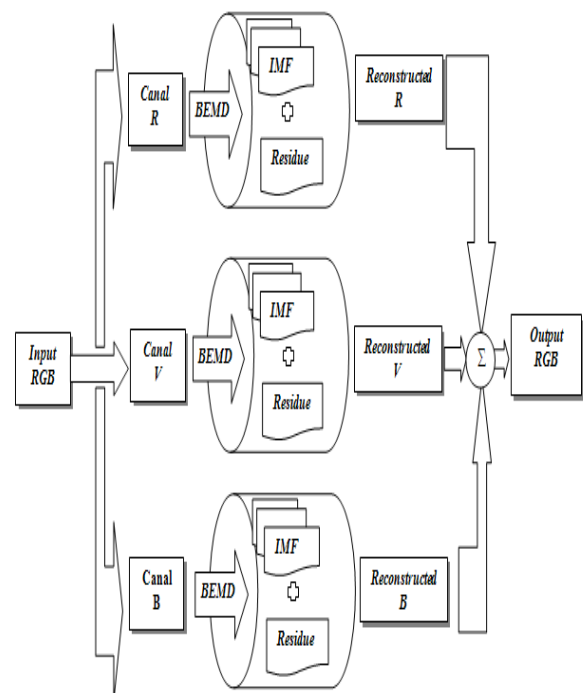


Fig. 1. The first BEMD approach for color image decomposition

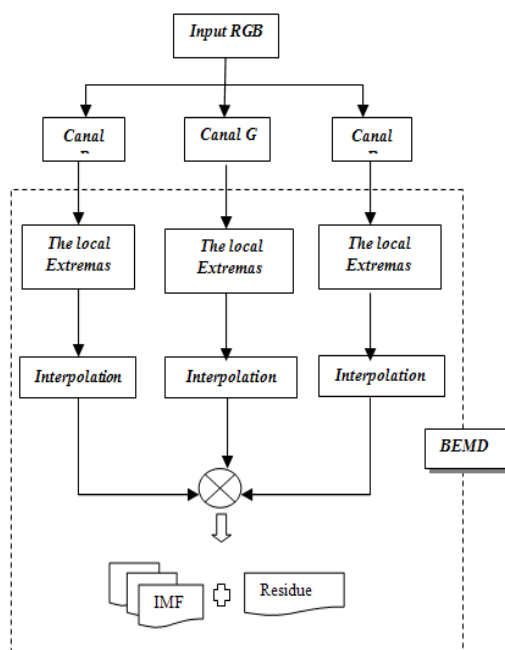


Fig. 2. The second BEMD approach for color image decomposition

IV. EXPERIMENTATION AND RESULTS

This section treats the implementation of two BEMD approaches to color image decomposition cited in the previous paragraph. The Figure 3 shows the results of two approaches of BEMD decomposition for color image of size (256x56x3).

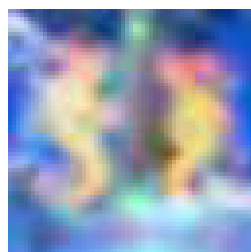
For each approaches, we have introduced the different IMFs with their residues. The last image (h) corresponds to the reconstructed image that permits a visual assessment of the BEMD efficiency.



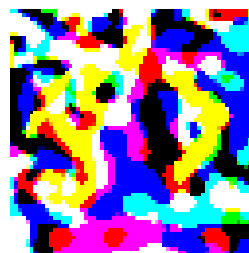
(A) Original RGB image



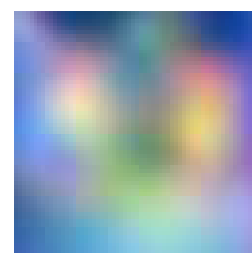
(B) First IMF



(C) First residue



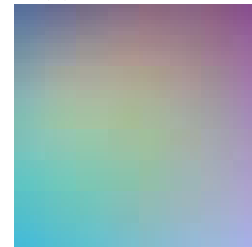
(D) Second IMF



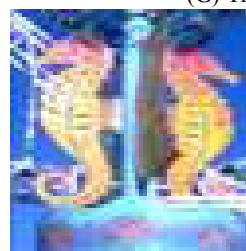
(E) Second residue



(F) Third IMF



(G) Third residue



(H) Reconstructed RGB image

Fig. 3. Color image decomposition with BEMD (first and second) approach

The table 1 presents the number of the max and the min of each decomposition of IMF.

TABLE 1. NUMBER OF EXTREMAS (MIN AND MAX) OF BEMD APPROACH

	max	min
First IMF	364	388
Second IMF	40	72
Third IMF	4	4

First, we observe that as in the case of grayscale images, the decomposition led to the successful extraction of IMFs. Each IMF has oscillations in different frequency ranges from the highest frequencies for the first IMF to lower frequencies for residue with the minimal extrema for the latter. The simulation result shows that the two BEMD approaches of decomposition are very similar in term of a PSNR index; it is equal to 46dB. The Table 2 presents the different values of execution time for the BEMD methods of the color image of figure 3.

TABLE 2. EXECUTION TIME BY THE TWO PROPOSED APPROACHES OF BEMD

The first approach			The second approach
R	G	B	11.274610 (s)
5.819518 (s)	5.78018 (s)	5.796493 (s)	
17.3962 (s)			

According to Table 2, which indicates the computational time of the two proposed approaches, the results show the interest of using the second approach if it is a large color pictures or an implementation in real time.

V. CONCLUSION

In this work, we presented two techniques for implementing the BEMD for color images decomposition. The BEMD applied for the RGB channels separately and the IMFs calculation from the summation of the interpolated image in each channel. Simulation results of decomposition images show that this second method is very interesting and promising for color images and can be applied in several areas that require the decomposition for the treatment of specific bands of frequencies in color images. In terms of comparison, the second technique is costly less in computation time. This technique seems better compared to the decomposition methods, and restoration of color images.

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