Optimization of a Multiphase Multiproduct Production Line based on Virtual Cells

Luís Pinto Ferreira, Enrique Ares Gómez, Gustavo Peláez Lourido, Benny Tjahjono

Abstract—The work presented in this article consists of the development of a discrete event simulation model, based on a real case and implemented in an Arena simulation environment. This is aimed at a class of very specific multiphase multiproduct production lines, with a four closed-loop network configuration, which is very common in the automobile sector. Also included in this study is an index of economic and functional efficiency, which evaluates cost-efficiency in each of the simulated scenarios. From a conceptual perspective, the idea of a virtual cell, was used in the configuration modeling of the production line. The modeling of complex production systems, based on the concept of virtual cells, allows for a greater understanding of the functioning process of a production line, through the simplification of the production flow and the addition of buffers between the virtual cells. Thus, due to the facility presented by their dynamic configuration, virtual cells constitute an important modeling tool, which should always be used whenever one aims to optimize production flow, namely in the case of production lines with a rather complex configuration.

Index Terms— Virtual Cells, Simulation, Automobile Assembly Lines

I. INTRODUCTION AND LITERATURE REVIEW

Simulation is one of the tools of support in the decision-making process, which allows for the projection and analysis of performance in systems and complex processes. Simulation can be seen as the construction process of a model representing a real system, as well as that of undertaking experiments using the same model with the purpose of better understanding its behaviour and evaluating the impact of alternative operational strategies [1, 2, 3, 4].

Many of the advantages ensuing from the use of simulation can be found in pertinent literature in this field. Some of these advantages can be clearly stated as follows:

- It permits production engineers to test new configurations in the production process, without the need to compromise resources, whose costs would be high [5].
- It can be used to explore new resource grading policies, operational procedures, decision-making rules, organization structures and information flow, without

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Benny Tjahjono is with Cranfield University, School of Applied Sciences, Manufacturing Department, UK (e-mail: B.Tjahjono@cranfield.ac.uk). having to interrupt the normal functioning of the system [1, 6].

- Simulation allows one to identify the blocking and starvation points on the production line, as well as test the various options with a view to optimizing their performance, thus identifying the causes for delays in the flow of materials, information and other processes [1, 5, 7].
- It can be used for testing explanatory hypotheses as to how and why a specific phenomenon occurs in the system [2].
- Simulation allows one to study a system which encompasses a wide time-span in a compressed period of time, or alternatively, it allows one to make a detailed study of the system's performance over an extended time period [8].
- It can be used to know the system better and to identify which variables really influence its performance, acting as a support for an improved understanding of reality so as to explain and describe it, or as a support in decision-making [9, 10].
- It also enables users to test the system's behaviour when confronted with new and unexpected situations [1, 10], as well as constituting a support for decision-making regarding investment in new technologies and equipment, improving production capacity and the management of material and human resources [11].

Despite all the benefits one can gain from the use of simulation as a support tool in the decision-making process, it also presents a few relevant drawbacks, the most significant of which are:

- Simulation does not provide optimal solutions for casestudy problems - it does, however, allow one to evaluate the system's behaviour in accordance with specific scenarios, which are created by the analyst for the purposes intended [1,2].
- If the model does not constitute a valid representation of the system being studied, the simulation results will not produce much useful information about the real system [8, 10].

The work described in this article consists of the development of a simulation model in an Arena environment, based on a real case, and is aimed at a very specific class of production lines, with a four closed-loop network configuration, commonly used in the automotive sector. This study is a sequence of another, developed by Resano *et al.* [12,13,14,15], who designed one of the first analytical models for an assembly line in the vehicle sector as a network of four closed loops of machines, decoupled by intermediate buffers formed by conveyors. They consider that machines process pallets which are not univocally related to each other. Both in the analytical model, as well as in the simulation presented here, one can analyse the

blocking and starvation phenomena on a complex production line; these models also consider the proportion of four- and two-door cars between the door disassembly and assembly stations. There is no knowledge of any other work in specialized literature, in the area of simulation, which includes all these factors, considered to be of such specific relevance in the performance of these types of manufacturing systems [16,17,18].

There are, in fact, very few studies undertaken which use simulation as a support tool in the decision-making process in the context of networks of closed-loop production lines. There is, however, a wider range of bibliography whenever the purpose of the study presupposes the development of analytical models for these types of configurations. [19] developed a simulation model based on the Siman language, with the purpose of maximizing the production line rate, with a closed-loop configuration, through the optimization of time distribution over the entire cycle, in all the different work stations. [20] developed a model for a network configuration to be used on a production line, comprising various machines, where assembly and disassembly operations are undertaken. This model is based on the first simulator for continuous flow, introduced by [21], where the discrete traffic of components is likened to a continuous flow. However, this study does not consider the phenomena of blockage transmission and starvation in a network of various closed loops. [22] proposed an analytical model to estimate the performance parameters of a closed-loop production line, characterized by limited capacity buffers and failure-prone machines. [23] resorted to the "Quest" language in order to develop a simulation model for a production line with a closed-loop configuration. Their purpose was to optimize its functioning through a better balance in the production flow. In fact, various rules and conditions were evaluated so as to ensure a more effective planning and control of the entire production system. Yet, for this study, the authors did not take into account the phenomena of machine blockage and starvation. Neither did they consider an external variable (x). These factors were included in the simulation model developed in this study. [24] created a tool to be used in the analysis of production lines with a network configuration of various closed loops. He developed a graphic and induction model to analyze efficiently the phenomena of blockage and starvation. Nevertheless, for the construction of the model, this author did not introduce an external variable (x), which is represented by the four-door car body proportion in the simulation model developed within the framework of this study. [25] developed an analytical model to evaluate and optimize the performance of an assembly line of semiconductors, characterized by a two closed-loop configuration. This study aimed to evaluate the impact of several parameters on the performance of the system, such as the number of circulating pallets and machine processing times, amongst others.

II. CONCEPTUAL MODELING BASED ON VIRTUAL CELLS

From a conceptual perspective, one used the concept of a virtual cell in the modeling of the production line. This cell is also known as a reconfigurable cell. The concept of the virtual cell was first introduced by [26] in order to develop control *software* for an automated production line of small

lots of parts. According to [27], the greatest difference between a virtual cell and the traditionally manufactured cell resides in the dynamic nature of the former. In the case of traditionally manufactured cells, the location of work stations is fixed and perfectly identifiable. The same does not happen with virtual cells, since they will vary according to the requirements at hand. According to [28], a virtual cell is any production scenario, from the lowest levels in a manufacturing hierarchy (for example, a CNC machine), to the highest (for example, a factory). Its internal organization allows for the manufacture of different types of products, as well as that of establishing significant parameters in its production capacity.

Figure 1 represents the main automobile line, as well as the door and front axle preassembly lines, as a network of four closed loops of machines (M) and intermediate buffers (B) formed by conveyors. Each of the intermediate buffers possesses a limited capacity, in accordance with the number of pallets it can contain. The time cycle for each machine is fixed and deterministic.



Figure 1. Main automobile assembly line and preassembly lines.

The sum of the car bodies, door and front axle assembly pallets stored in each of the intermediate buffers of the three first closed-loops remain, respectively, constant at any time and are defined by Equations (1) to (3). This fact, as well as other analyses undertaken to evaluate the influence of different variables which interfere in the performance of the automobile assembly line being studied, was previously analysed in [12, 13, 14, 15].

$$n_{12} + n_{23} + n_{34} + n_{41} = 237$$
 (1)

$$n_{25} + n_{56} + n_{64} + n_{42} = 450$$
 (2)

$$n_{37} + n_{73} = 138$$
 (3)

The fourth closed-loop defines the relationship between the number of pallets with doors in different preassembly states and the number of pallets of cars with disassembled doors via an external variable (x), according to Equation (4). This variable represents the four-door car ratio between the doors' disassembly stations, located at M_2 , and the doors' assembly stations, located at M_4 . This variable can take on values of between 0 and 1.

Equation (4): $n_{25} + n_{56} + n_{64} + n_5 + n_6 = (n_2 + n_3 + n_4 + n_{23} + n_{34})(1 + x)$ Proceedings of the World Congress on Engineering 2011 Vol I WCE 2011, July 6 - 8, 2011, London, U.K.

Where n_5 and n_6 are the numbers of stations M_5 and M_6 , n_2 is the number of stations at M_2 , from the door disassembly stations, n_3 is the number of stations at M_3 , and n_4 is the number of stations at M_4 to the door assembly stations. The values n_2 , n_3 , n_4 , n_5 and n_6 remain constant. Replacing the sum of their values in Eq. (4) the following is obtained [12, 13, 14, 15]:

$$n_{25} + n_{56} + n_{64} + 60 = (216 + n_{23} + n_{34}) \cdot (1 + x)$$
 (5)

The simulation model presented in this article is based on these equations in order to determine the number of pallets which must circulate on each of the 4 closed-loops which exist on the analyzed automobile assembly line.

On the first three loops, the velocity (V) of the intermediate buffers formed by conveyors is: $V_{1,2}=16m/minute$, $V_{2,3}=16m/minute$, $V_{3,4}=16m/minute$, $V_{4,1}=16m/minute$, $V_{2,5}=25m/minute$, $V_{5,6}=25m/minute$, $V_{6,4}=25m/minute$, $V_{4,2}=25m/minute$, $V_{3,7}=45m/minute$, $V_{7,3}=45m/minute$.

Figure 2 presents the automobile assembly line analyzed for this study. In the same manner as [12], 7 virtual cells were constituted so as to better understand the trajectories of the state of the intermediate buffers formed by conveyors, positioned between each virtual cell and thus ensuring supply to the cells and avoiding starvation points. These virtual cells are represented by each of the machines (M) presented in figure 2. In the automobile production line being analyzed, each of these constitutes a set of different types of stations (for example, manual stations, automatic stations, semi-automatic stations, etc.), which are logically grouped with the purpose of undertaking a specific set of tasks. For this study, one used this modeling of line configuration to develop a decision-making support system based on a discrete event simulation model for a multiphase multiproduct automobile production line. The main objective here was to compare the results obtained by [12], which is based on analytical methods, with those obtained through the simulation models.



Figure 2. The modeling of the automobile assembly line based on 7 virtual cells.

Another line configuration modeling option based on 3 virtual cells could be used for the analysis and optimization of the automobile assembly line being studied, as is presented in figure 3.



Figure 3. Modeling of the automobile assembly line based on 3 virtual cells.

Another modeling example based on the concept of virtual cells is presented in figure 4, in which the automobile assembly line is structured on the basis of 2 virtual cells.



Figure 4. Modeling of the automobile assembly line based on 2 virtual cells.

III. CHARACTERISTICS OF THE DECISION-MAKING SUPPORT SYSTEM DEVELOPED

In the context of this project, all the work was developed in an Arena simulation environment [29]. Its simulation language constitutes a visual and flexible programming tool, directed at the object, since it simultaneously combines the construction of simulation models with the integration of different commonly used languages: Visual Basic, C, C⁺⁺. This language is based on the SIMAN simulation language [30].

The purpose of the use of an Arena simulation environment was that of enabling the production engineer to evaluate the performance of the automobile assembly line, through the variation of different parameters, thus contributing to an improved specification, characterization and definition of the most efficient control system. With this objective in mind, a support system for decision-making was developed; this enables the automatic generation of different simulation models. In the initial stage of simulation, the user is able to interact with the system to be developed, through the introduction of various parameters such as:

- The four-door car ratio (x);
- The processing time for each machine;

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- The production sequence in accordance with each type of car (two- or four-door);
- The speed and length of the intermediate buffers formed by conveyors;
- Simulation time;
- The number of pallets circulating on the first three closed-loops.

Figure 5 presents the graphic interface which allows the user to configure the above mentioned parameters.

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	Insert Machine Processing Times	Simulation Time Definition (minutes)
	Insert Conveyor Speed	3960
	Insert the information - Conveyor Length	Number of Pallets on each Loop Loop 1 Loop 2 Loop 3
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Figure 5 – Parameterization of the automobile assembly line.

Another contribution made by this study was that of integrating an automatic report generator in the simulation environment; this presents information on the main performance indexes of the simulated models, using graphic visualization, which required the integration of various applications in the Arena simulation environment, such as: Visual Basic for Applications (VBA), Visual Basic (VB), *Microsoft Access* (Database), *Crystal Report* (Graphics Edition). In this context, it is worth highlighting the visual aspects of the graphics produced (three examples are presented in figures 6, 7 and 8), which allow the user to have a better perception of the performance of the simulated models.

From among those considered, the following performance indicators are highlighted:

- Machine Usage Levels;
- Number of Cars for each of the types produced;
- Number of operations undertaken on each of the machines;
- Production time/vehicle;
- Relationship between the time cycle of each machine and the number of pallets on each upstream buffer.



Figure 6. Number of operations undertaken on each of the machines.





Figure 8. Automobile production time.

IV. VALIDATION OF THE SIMULATION MODEL PROPOSED

In [12, 14, 15] the incompatibility between equations (2) and (5) (see section 2) was demonstrated. These define the sum of the number of pallets on the intermediate buffers which constitute the second and fourth closed loop, with some of the maximum and minimum capacities of the corresponding intermediate buffers, for the specific values of variable x. This incompatibility reveals that the automobile assembly line cannot operate in practice for x < 0.37, in both the stationary and transitory regimes, and for x>0,97, in the stationary regime. As with any simulation project, an important phase is the validation of the model constructed; this ensures that it is a faithful representation of reality and can then be used for decision-making. Through the simulation model developed in the context of this study, and for the automobile production line being analyzed, one also verified that the system did not function for the values of x<0,37 and x>0,97, due to the phenomena of blockage and starvation occurring on the machines integrating the analyzed model. In the same way, one also noticed that, once the minimum buffer capacity mentioned in [12, 13] was reached, a continuous supply of transport and assembly pallets to machines was assured [16]. In the context of this work, the validation of the simulation model proposed was confirmed, on the basis of these two presuppositions.

V. INDEX OF ECONOMIC AND FUNCTIONAL EFFICIENCY

It is important to quantify the benefit obtained whenever various parameters are altered in the multiphase multiproduct production line being studied. One is then able to quantitatively assess the efficiency of each of the simulated scenarios. One sought to develop an indicator of an economic type which, for a given period of time, would calculate the most representative costs for each of the simulated alternatives. Thus, based on the economic function index developed by [31, 32, 33, 34], a new economic function index (EFI), was elaborated, which considered the specific aspects pertaining to the multiphase multiproduct automobile production line being studied. Table 1 below presents the variables used in the development of the (EFI) so as to evaluate its cost-effectiveness.

TABLE 1		
VARIABLES USED IN THE DEVELOPMENT OF THE EFI		
N _{ij}	Total number of type i parts produced for each j machine	
PT _{ij}	Processing time for the type i part on machine j	
MC _{ij}	Manufacturing cost of the type i part on machine j	
	per time unit	
CNUj	Cost of non-usage of machine j per time unit	
TIj	Time of inactivity of machine j	
CPIFD	Costs of penalties incurred due to failure to meet delivery	
	deadlines	
TDO	Time of delay in completing an order	
CPz	Cost based on the number of pallets circulating on loop z	
	(z =1,2,3)	
ECLz	Energy costs for loop z (based on the loop's velocity, the	
	number of pallets, etc.) $(z = 1, 2, 3)$	
CLCLz	Cost associated to the length of the conveyors on loop z	
	(z =1,2,3)	

All the variables are real and the costs are obtained on the basis of a pre-established time unit. The EFI includes the following components:

EFI = Fixed cost of manufacture + Cost of machine non-usage + Cost of failure to meet delivery deadline + Cost of pallets + Energy costs + Cost associated to the length of the conveyors

In this manner, and considering the previously described variables, the following economic index function was obtained. This will allow one to calculate the most representative costs for each of the simulated scenarios:

$$EFI = \sum_{j=1}^{7} Nij * PTij * MCij + \sum_{j=1}^{7} CNUj * TIj +$$

$$CPIFD * TDO + \sum_{z=1}^{3} CPz + \sum_{z=1}^{3} ECLz + \sum_{z=1}^{3} CLCLz$$

In the same way, one can calculate the most representative costs for each of the simulated scenarios, in accordance with the first three *loops* on the production line. Thus, considering that EFI 1, EFI 2 and EFI 3 respectively represent the economic index function associated to *loop* 1, *loop* 2 and *loop* 3, one can then obtain the following economic indicators:

$$EFI1 = \sum_{j=1}^{4} Nij * PTij * MCij + \sum_{j=1}^{4} CNUj * TIj +$$

CPIFD * TDO + CP1 + ECL1 + CLCL1

EFI2=
$$\sum_{j=2,4,5,6}$$
 Nij* PTij* MCij + $\sum_{j=2,4,5,6}$ CNUj*TIj +

CPIFD * TDO + CP2 + ECL2 + CLCL2

EFI3=
$$\sum_{j=3,7}$$
 Nij*PTij*MCij + $\sum_{j=3,7}$ CNUj*TIj +

VI. CONCLUSION

In this paper, an automobile assembly line and different preassembly lines were modelled as a network of four closed-loop machines and intermediate buffers formed by conveyors, constituting a configuration which is widely used in these kinds of assembly lines. Using an Arena simulation environment, a representative model of this line was developed with the purpose of providing the production engineer with a better understanding and assessment of its performance; it represents, on the computer screen, each moment in the state of the system and its evolution over time, thus allowing for improved communication between the model and the user. In fact, the great visual component of the models developed allows for a clear understanding on the part of the decision-making agents who will eventually use them, since they will be able to view the interaction occurring between the entities which make up the model, allowing for a better understanding of the simulation results. The authors believe that, by producing this study, they have contributed to emphasising the importance of the use of simulation in the development, on computer, of virtual environments which reproduce the behaviour of many real systems.

As perspectives of future work, some actuation lines stand out, as a natural continuation of the proposals presented here:

• Evaluated the impact of the pallet numbers circulating on the first three closed loops on the performance of the production line, translated into the number of cars produced/hour, in order to improve the availability of the entire manufacturing system for any value of x.

• Assess the impact of the length of intermediate buffers on the performance of the production line, translated into the number of cars produced / hour, in order to improve the availability of the entire manufacturing system for any value of x.

• Impact evaluation that the sequence of production of different types of cars in the automobile assembly line performance.

• Behaviour evaluation of the production line when a new car type is inserted.

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