Dynamic Tests on Ring Shear Apparatus

G. Di Massa Member IAENG, S. Pagano, M. Ramondini

Abstract—Ring shear apparatus are used to determine the ultimate shear strength of soils when it is sheared to large displacements.

Since recent investigations have shown that the soil ultimate strength can rise, if sheared by a large intermittent movement, the paper describes the peculiarities of these tests and the upgrade of a ring shear apparatus to perform this test. In the final part of the paper, the first experimental results are reported and commented.

Index Terms — cyclic rotation, ring shear apparatus, soil, ultimate strength

I. INTRODUCTION

Ring shear apparatus allows to evaluate the residual shear strength of soils also termed the ultimate shear strength. This is the strength of soil when it is sheared to large displacements, for example along the failure plane of a landslide or in a fault zone [1, 2].

To determine ultimate shear strength value, the ring apparatus consolidates a thick sample to the required stress. A slip surface is formed in the sample as part of the test procedure. The sample is displaced between two rings (Fig. 1): the upper one is fixed while the lower one, driven by an electric motor, rotates at a constant speed. A continuous shearing action is so applied to the sample until the constant residual strength value is achieved.

Recent investigations [3] have shown that in clay formations, the co-seismic reactivation of pre-existing landslides involves dynamic shear actions on sliding surfaces characterised by attritive states.

II. EQUIPMENT DESCRIPTION

The soil testing equipment adopted for this kind of tests is the Wykeham Farrance mod. 25850 that, in its original configuration, is constituted by (Fig. 2-5):

- a rotating sample container or shear box, placed in the lower part of the sample turret, characterized by an annular groove whose mean diameter is equal to 85 mm, filled with the soil sample.

To put in evidence this peculiarity, an intermittent rotating motions must be applied to the lower ring, after the attainment of fully softened and residual conditions.

The paper describes the upgrade of a ring shear apparatus that has been equipped with an electric motor by which it is possible to adjust the characteristics of the intermittent motion of the ring below.

The test rig will perform an extensive test campaign to evaluate the combination of the motion characteristics and the vertical load able to maximize the ultimate shear strength.

By way of example, in the final part of the paper, some preliminary tests are shown and commented.
load hanger;
- a torque arm assembly, placed in the upper part of the sample turret which prevents upper ring rotation due to the shear actions exerted by the soil sample; the torque arm is constrained by means of to force sensors through which it is possible to measure the friction torque;
- two force sensors, each constituted by a deformable ring and a mechanical comparator to detect the ring deformation (load rings, $\Phi_{\text{ext}}=178$ mm; thick = 3 mm); in the current equipment configuration the comparators have been replaced with two LVDT sensors that can measure up to 500 N.

Fig. 2. Friction force measurement

Fig. 3. Ring shear apparatus side view

Fig. 4. Ring shear apparatus plan view

Fig. 5. Ring shear mechanical transmission

III. EQUIPMENT UPGRADE

To move the sample container with an intermittent rotating law motion, the apparatus was equipped with a servomotor joined to the worm shaft, by means of an helical joint, in place of the hand-wheel, as schematically represented in Fig. 6. When the servomotor operates, the chain drive must be disconnected. The servomotor installation did not require any irreversible changes of the equipment; its bracket (constituted by two aluminum alloy components, for mounting reasons) was connected to the frame machine adopting the threaded holes of the protecting cover of the shaft rolling bearing (Fig. 7). A hole, drilled on the lateral bracket surface, allows to screw the helical joint on the worm shaft.

Fig. 6. Servomotor installation

Fig. 7. Servomotor mounting

IV. SAMPLE CONTAINER MOTION

The servomotor drives the sample container so that it can perform an intermittent motion. The motion law considered in the following is characterized by a profile velocity that has an initial trapezoidal form, followed by a time interval during which the container is at rest (Fig. 8).

Fig. 8. Desired velocity profile

The sample annular housing has a mean radius ($R$) of about 42.5 mm; the two force sensors, adopted to detect the sample shear resistance, exert their reactions on the (160
mm long) torque arm. The sensor have a full-scale range of 500 N and therefore, the maximum measurable torque is equal to about: $M_t = 80$ Nm.

To choose the power of the electric motor it was assumed that the maximum compressive stress, provided by the loading device is equal to 3 daN/cm² and that the maximum coefficient of friction provided by the soil sample is equal to 0.6 ($\phi = 33°$).

The maximum friction torque exerted by the soil sample, whose annular cross section (A) is equal to 40 cm², results therefore:

$$M_p = ApR = 30 \text{ Nm}.$$ 

The mechanical transmission between servomotor and sample container is constituted by a worm drive with a 55:1 gear ratio (ratio between the number of teeth of the worm wheel and the number of worm threads).

The maximum torque, reduced to the servomotor axis, is:

$$M_{rm} = \frac{30}{55} = 0.54 \text{ Nm}.$$ 

The reference intermittent motion is characterized by the following values:

- linear acceleration: $\alpha = 0.25 \div 0.45 \text{ g}$;
- mean linear velocity: $v = 1 \div 10 \text{ mm/s}$;
- frequency = 1 \div 10 Hz.

The servomotor power was chosen considering a tangential acceleration for the annular sample equal to:

$$a_t = 4.5 \text{ m/s}^2.$$ 

The correspondent angular acceleration of the sample container and of the servomotor are respectively:

$$\alpha = a/R = 113 \text{ rad/s}^2 \quad \alpha_m = \alpha \cdot \varepsilon = 6160 \text{ rad/s}^2.$$ 

In the following, it is neglected the moment of inertia of the sample container and of the worm wheel. In fact, their reduced values are very small in comparison of other inertias.

Considering servomotor rotor and worm inertia, equal to about $I = 0.7 \cdot 10^{-4} \text{ kgm}^2$, the inertia torque is equal to:

$$M_I = 0.7 \cdot 10^{-4} \cdot 6160 = 0.43 \text{ Nm}.$$ 

The maximum torque that the servomotor must provide is therefore:

$$M_{tor} = M_I + M_{em} = 0.43 + 0.54 = 1.0 \text{ Nm}.$$ 

To define the maximum rotating speed for the servomotor it must be considered the most demanding operating cycle is characterized by the following parameters:

- angular acceleration: $\alpha = a/R = 4.5/0.04 = 113 \text{ rad/s}^2$;
- mean linear velocity: $v_m = 10 \text{ mm/s} = 0.010 \text{ m/s}$; the correspondent mean angular velocity is:
  $$\omega_m = \frac{v_m}{R} = 0.010/0.04 = 0.25 \text{ rad/s};$$
- cycle frequency: $f = 1 \text{ Hz}$ (T = 1.0 s).

Considering the gear ratio of the mechanical transmission ($\varepsilon = 55$), in the following table the main kinematic parameters for the sample container and for the servomotor are summarized:

<table>
<thead>
<tr>
<th>Shear box</th>
<th>Servomotor</th>
</tr>
</thead>
<tbody>
<tr>
<td>Angular acceleration</td>
<td>$\alpha = 112.5 \text{ rad/s}^2$</td>
</tr>
<tr>
<td>Mean angular velocity</td>
<td>$\omega_m = 0.25 \text{ rad/s}$</td>
</tr>
<tr>
<td>rotations per cycle (with: $T = 1 \text{ s}$)</td>
<td>$0 = 0.25 \text{ rad}$ ($= 14.3°$)</td>
</tr>
</tbody>
</table>

The maximum rotation speed is reached for the velocity profile reported in Fig. 9, characterized by a triangular shape diagram of the first part of the cycle (degeneration of the trapezoidal profile) followed by a zero velocity value.

![Fig. 9. Velocity profile with maximum rotation speed](image)

The first part of the cycle ends for $t = t_f$. For: $t = t_f/2$, the angular velocity reaches its maximum value $\omega_b$. Adopting the kinematic parameters reported in Tab. I, it follows:

a) $\omega_b$ is reached with a constant acceleration, so that: $\omega_b = \alpha_t t_f/2 = 6187 t_f/2 = 3094 t_f$;

b) a complete cycle, having period of 1 s, involves a servomotor rotation equal to: $\theta_M = 13.75 \text{ rad}$. Taking into account the triangular shape law, the following two relationships may be obtained:

$$\theta_M = \frac{1}{2} \cdot t_f \cdot \omega_b = 13.75 \text{ rad}; \quad t_f \cdot \omega_b = 27.5 \text{ rad}.$$ 

It follows:

$$\omega_b = 291 \text{ rad/s}; \quad t_f = 0.094 \text{ s}.$$ 

The maximum inertia torque is practically equal to that already calculated:

$$M_I = I \cdot \alpha_m = 0.7 \cdot 10^{-4} \cdot 6187 = 0.43 \text{ Nm}.$$ 

The worm gear mechanical efficiency could be estimated by means of the following expression:

$$\eta = \left(1 - \frac{p}{2 \pi f}ight) \left(1 - \frac{2 \pi f}{p}ight).$$ 

Being $f$ the friction coefficient that in case of adequate lubrication can be assumed equal to 0.05, $p$ the pitch of the
The power required for the electric motor is therefore:

\[ P = \frac{M_{\text{tot}} \cdot \omega \cdot \eta}{0.40} = 728 \text{ W} \]

### 3. Motor selection

On the basis of the intermittent motion characteristics for the sample container a 930 W brushless servomotor was chosen (Kollmorgen, mod.: AKM24D-ACDNC-00 505573) having the following main characteristics:

- maximum rotating speed: 8000 rpm;
- maximum torque: 1.41 Nm;
- maximum current: 2.21 A;
- voltage constant \( K_{\text{E rms}} = 40.8 \text{ mV/min} \);
- torque constant \( = 0.63 \frac{\text{Nm}}{\text{A}} \);
- rotor inertia: 0.270 kg cm\(^2\);
- shaft diameter: 9 mm.

In unloaded operating condition, it is found that the servomotor is able to follow the desired speed profile with good approximation (Fig. 10). In such condition the load is only due by the system rotating inertia; Fig. 11 shows the corresponding motor torque curve.

In load operating condition, the mechanical efficiency of the transmission between the motor and the container was evaluated; in steady-state condition, the torque provided by the electric motor was detected together with the one measured by the load rings; the mechanical efficiency results equal to about 30%. So the maximum torque that the servomotor can deliver on the sample container is:

\[ M_{\text{max}} = 1.41 \times 55 \times 0.3 = 23 \text{ Nm} \]

A planetary gear box may be used for speed reduction and torque multiplication. There are specifically designed planetary gear box that can meet the motor mounting dimensions without any modification of the motor support (Fig. 12). A self aligning hub is adopted to maintain concentricity between motor shaft and gear-head.

For this gear box, the minimum gear ratio is 3:1 which would result in tripling of the torque acting on the sample container maintaining the maximum rotation speed at about 48 rpm.

The correct gear ratio must be chosen through a tradeoff between the maximum torque and the maximum rotating speed of the sample container.

![Fig.12. Servomotor with planetary gearbox](image-url)

### 4. Tests and data acquisition

Each test consists of three phases: the first phase is the standard one, during which the rotating sample container rotates at a constant speed fixed at 0.05 mm/min and the torque slowly grows until it reaches an asymptotic value (the residual shear strength) usually reached after a displacement of 10 cm. Reached the asymptotic torque value, the second phase starts: the sample container is forced to rotate, according to the assigned intermittent law motion. In the third phase, similar to the first one, the rotating speed turns to be constant and an increase of the torque, with respect to the previous residual shear value, is expected.

As said above, the friction torque exerted by the soil sample is detected by means of two load rings, each instrumented with an LVDT sensor. This measuring system has a good static characteristic but, due to the high deformability of the rings, when the input signal rapidly varies, it introduce the effects of the dynamic behavior of the rings, modifying the response. The sensor are so inadequate to follow the second phase of the test as it can excite the rings to vibrate altering the torque measure. As the aim of the test is to detect the torque only in the first and in the third test phases, which involves a quasi-static phenomenon, the use of the load rings may be considered acceptable.

In Fig. 13, two torque diagrams, for two different applied loads, are reported; the displacement scale was cutted around the impulsive load phase. In both cases, it can be noted an increase of the shear strength during the intermittent load phase; in the third phase a reduction of the
shear strength was measured in the new final state characterized by strength value higher than those measured in the first phase. This behavior can be explained by assuming that the application of impulsive load induce a different arrangement of soil particles on the slip surface, with the formation of a new shearing surface. Opening a window around the second phase (Fig. 13), characterized by displacements of about 70 cm, it can be observed that during the impulsive load, shear stress value oscillations are influenced by the applied vertical load.

Fig.13. Residual shear stress at different vertical load

![Residual shear stress at different vertical load](image)

Fig.14. Shear stress during phase 2

![Shear stress during phase 2](image)

V. CONCLUSION

The first experimental tests performed on the updated equipment have shown its effectiveness for the study of the effects of shock loading on the residual strength of the clay soils. During the transient phase (phase 2), the deformability of the load rings does not allow a reliable measurement of shear stresses acting on the sample; therefore, to check if the intermittent motion of the sample container follows the desired law motion, the rig will be equipped with rigid load cells.

REFERENCES

