Abstract—Induction motors are widely used in most of the industrial applications due to their ruggedness, reliability and low cost. Even a small amount of improvement in efficiency will have a bigger effect in conserving energy. This paper incorporates an efficiency optimization scheme to operate the single phase induction machine at its maximum efficiency point. Efficiency is improved by operating the machine at an optimum slip. Optimum slip is obtained by testing the machine in open loop. Simulation results to prove the concept of optimum slip are presented and are validated through LabVIEW based implementation for a fan motor to operate it at its maximum efficiency point for a given speed. An online efficiency control is implemented using Perturb and Observe (P&O) algorithm so that errors in parameter estimation do not affect the performance.

Index Terms—Efficiency optimization, Optimum V/f, Perturb and Observe (P&O), Single Phase Induction Motors (SPIM)

I. INTRODUCTION

Among electrical motors, induction motors are the most used both for home appliances and in various industries. Most of the electrical energy produced is consumed by these motors. In an effort to improve the efficiency, there have been improvements in materials, design and construction techniques. However motor losses are still greatly dependent on control strategies, especially when the motor operates at light load.

Single Phase Induction Motors (SPIMs) is a highly efficient machine when operated close to its rated torque and speed. However, at light loads, no balance in between copper and iron loss, results in considerable decrease in efficiency. To achieve better efficiency induction motor has to be controlled by some control techniques. Variable frequency drives serve the purpose to a good extent but it is not economical to use inverters for a low rating motor as the cost of inverter might exceed the cost of motor.

II. EQUIVALENT CIRCUIT OF CAPACITOR START AND RUN SPIM

Let

\[ E_{fa} \] Forward voltages of the magnetizing branch of the auxiliary winding
\[ E_{ba} \] Backward voltages of the magnetizing branch of the auxiliary winding
\[ E_{fm} \] Forward voltages of the magnetizing branch of the main winding
\[ E_{bm} \] Backward voltages of the magnetizing branch of the main winding
\[ E_{mf} \] Forward induced electromotive force of main winding
\[ E_{mb} \] Backward induced electromotive force of main winding
\[ I_a \] Auxiliary windings current
\[ I_m \] Main windings current

Efficiency improvement of single phase capacitor run motor started with stator voltage control [1]. The traditional voltage control technique was further modified to control the voltage of only main winding keeping auxiliary winding voltage constant [2]. This reduces the harmonic content in the auxiliary winding and thus resulting in loss reduction. Although advancements in technology have enabled the employment of variable frequency drive for three phase ac machines, they have not been widely used in the single phase counter parts [5, 6, 7]. V/f control in SPIM does not provide constant torque operation for the entire speed range since the maximum available torque rapidly decays below half of the base frequency.

An efficiency improvement control scheme for capacitor start and run machine by operating at optimum slip was proposed [3, 4, 8]. In this paper, the concept of optimum slip is being incorporated with the interfacing capabilities of LabVIEW for efficiency optimization. Also it is proved that the efficiency at light loads can be matched to a good extend with that of full load. Perturb and Observe (P&O) method is adopted to account for uncertainties in parameter estimation.
where
\[ V = V_m = V_c \] (3)

Current through the forward and backward component can be written as
\[ I_{fm} = \frac{R_{cf}}{R_{cf} + Z_f}(I_m + j\alpha I_a) \] (4)
\[ I_{bm} = \frac{R_{cb}}{R_{cb} + Z_b}(I_m + j\alpha I_a) \] (5)

Using (4) and (5) in (1) and (2) and simplifying, a ratio between winding currents is obtained as
\[ \frac{I_a}{I_m} = \frac{Z_m + Z_{d} + Z_{db} - j\alpha (Z_{d} - Z_{db})}{Z_c + Z_{a} + \alpha^2 (Z_f + Z_b - Z_{db}) - j\alpha (Z_{d} - Z_{db})} \] (6)

From (6) we can conclude that the ratio of winding currents is a function of frequency and slip.
\[ \frac{I_{fm}}{I_{m}} = r_f(f, s) \] (7)
\[ \frac{I_{bm}}{I_{m}} = r_b(f, s) \] (8)

Electromagnetic torque of an SPIM is represented by
\[ T_e = \frac{|I_{fm} - j\alpha I_a|^2 R_{cf} |Z_f|}{\omega_c} - \frac{|I_{bm} + j\alpha I_a|^2 R_{cb} |Z_b|}{\omega_c} \] (10)

From (10), it can be inferred that the electromagnetic torque is also a function of slip and frequency.
\[ T_e = \frac{I_{m}^2}{R_{m}} Func(f, s) \] (11)

and electrical power loss is obtained as
\[ P_{el} = P_{in} - P_m = I_{m}^2 Z_{in} \cos \theta - T_e \omega_m \] (12)

where
\[ Z_{in} = \frac{V}{I_m} = \frac{(Z_m + r_f Z_f + r_b Z_b) - j\alpha r_m (Z_f - Z_b)}{(1 + r)} \] (13)

\[ P_{el} = T_e (Z_{in} \cos \theta Func(f, s) - \omega_m) \] (14)
\[ P_{el} = T_e Func(f, s) \] (15)

According to (15), under a specific load and frequency, the motor electrical losses depend on motor slip only. So there may exist an optimum slip at which the loss is a minimum for a fixed frequency. The optimum slip can found as follows:

\[ \text{Optimal Motor Slip} = \frac{Z_{db}}{Z_f} \]
\[
\frac{\partial P_{el}}{\partial s} \bigg|_{s_0} = 0
\]  
(16)

\[
\frac{\partial P_{el}}{\partial s} \bigg|_{s_0} = \frac{\partial \text{Func}(f, s)}{\partial s} \bigg|_{s_0} = 0 \Rightarrow s = s_{opt}
\]  
(17)

From (17), the optimum slip is a function of frequency under a specific load.

III. SIMULATION RESULTS USING MATLAB/SIMULINK

Simulation results of capacitor start and run motor in open loop is shown in figure [2]. Here the SPIM is made to operate at different slip by varying voltage for a given load and frequency and the losses at each case have been tabulated. The same experiment has been carried out for different load keeping the frequency same as that of fundamental as we are not interested in variable frequency control due to reasons mentioned earlier. The simulation parameters used are given in TABLE I.

\[\text{TABLE I} \quad \text{MOTOR PARAMETERS USED IN SIMULATION}\]

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>(R_{1m})</td>
<td>4 (\Omega)</td>
<td>(L_{1m})</td>
<td>0.0203 H</td>
</tr>
<tr>
<td>(R_{1a})</td>
<td>6.5 (\Omega)</td>
<td>(L_{1a})</td>
<td>0.0210 H</td>
</tr>
<tr>
<td>(R_2)</td>
<td>3.61 (\Omega)</td>
<td>(L_2)</td>
<td>0.0304 H</td>
</tr>
<tr>
<td>(\alpha)</td>
<td>1.1293</td>
<td>(J_m)</td>
<td>0.001424 Kgm²</td>
</tr>
<tr>
<td>(C)</td>
<td>40 (\mu F)</td>
<td>(V_{\text{rated}})</td>
<td>220 V</td>
</tr>
<tr>
<td>(f)</td>
<td>50 Hz</td>
<td>(I_{\text{rated}})</td>
<td>5.8 A</td>
</tr>
</tbody>
</table>

The results obtained using MATLAB are plotted in MS Excel and given in figure [2].

Figure [2] gives the variation of losses(in watts) with different slips for loads of 1Nm, 2Nm, 3Nm and 4Nm. The slip at which losses are minimum varies with load. It is observed from the plot that the variation of optimum slip do not vary considerably with small variations in load.

IV. LABVIEW BASED EFFICIENCY MONITORING

For experimental verification, a fan motor has been used. The name plate details are presented in TABLE II. Unlike the case in simulation, fan motor’s load is proportional to the square of the speed. It is expected and experimentally verified that the concept of optimum slip with fixed frequency cannot be applied for fan type motors. Hence for fan type motors, variable voltage and variable frequency control is applied. Even though the use of inverters for a fan motor is not economical, but for higher rating machines (both single/three phase) with similar characteristics it can be applied. Hence for hardware implementation fan motor is connected to an inverter and the control signals are given using LabVIEW.

Figure [3] gives an estimation of efficiency improvement when different loads are applied to the machine. Maximum improvement in efficiency is observed at light loads. Also it can be validated that the induction motors can be operated at full load efficiency even in light load conditions. In the case of 1 Nm load applied to the machine the improvement in efficiency is 28% which is quiet large. There can be considerable saving of power in industries especially during light load conditions by employing this technique than the traditional delta to star change over.

\[\text{Fig. 3. Variation of efficiency (in %) with slip}\]

\[\text{Fig. 4. Graph showing variation of input power(P)}_i\text{ and }\omega^3_{\text{normalized}}\text{ (Experimental)}\]
Figure [4] shows the variation of input power with $\omega_3^{\text{norm}}$ for a fan motor for different frequencies. As described earlier, load is proportional to the square of the speed and hence output power is proportional to the cube of the speed. The slope of the curve given in figure [4] gives the efficiency. It is observed from the graph that there is an optimum $V/f$ for the machine at which it gives maximum efficiency. For lower speed range, it is better to operate the machine at lower frequency to get maximum efficiency.

Controller implementation is done from the values obtained from experimental results. A simple closed loop control is implemented using LabVIEW. An inverter is used to obtain variable voltage and frequency. Pulses are generated from LabVIEW to vary the voltage and frequency in accordance with the maximum efficiency operation. In the actual implementation, the designed values may not be the optimum efficiency point. Hence, Perturb and Observe (P&O) algorithm to retune the voltage (with frequency kept constant at optimum point) is used to improve the efficiency.

Table II

<table>
<thead>
<tr>
<th>Variables</th>
<th>Values</th>
<th>Variables</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>$1.5\mu F$</td>
<td>$N_{\text{rated}}$</td>
<td>1300 RPM</td>
</tr>
<tr>
<td>$f_{\text{rated}}$</td>
<td>50 Hz</td>
<td>$V_{\text{rated}}$</td>
<td>220 V</td>
</tr>
<tr>
<td>Poles</td>
<td>4</td>
<td>$I_{\text{rated}}$</td>
<td>0.239 A</td>
</tr>
<tr>
<td>$P$</td>
<td>55W</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Hardware setup is shown in figure [5] and figure [6]. A comparison of the presented technique with the existing technique is presented in Table III.

Table III

<table>
<thead>
<tr>
<th>Reference No</th>
<th>Design</th>
<th>Control</th>
<th>Converter</th>
<th>Measured Variables</th>
<th>Advantage</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ref. 2</td>
<td>Offline design</td>
<td>Open loop</td>
<td>Triac</td>
<td>$I_a$</td>
<td>Reduced harmonics in auxiliary current.6% improvement in efficiency for fan motor achieved by this technique.</td>
</tr>
<tr>
<td></td>
<td>without considering parameter variations</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ref. 3</td>
<td>Offline design and offline parameter variation</td>
<td>Closed loop</td>
<td>Triac</td>
<td>Ratio of currents $I_a$ and $I_m$</td>
<td>Nearly 28% improvement in efficiency is achieved for constant load.</td>
</tr>
</tbody>
</table>

Fig. 5. Hardware setup with fan and inverter

Fig. 6. Hardware setup interfaced using LabVIEW
V. CONCLUSION

In this paper, single phase induction motor efficiency improvement is done by operating the machine at optimum slip. Simulation results are included for different loads and variations of losses with slip in each case are plotted. Result shows a considerable improvement in the efficiency of motor especially at light loads. Fan motor is used for hardware implementation using LabVIEW. Perturb and Observe (P&O) algorithm is used for online efficiency optimization.

REFERENCES