

# Gait Parameter and Speed Estimation from the Frontal View Gait Video Data Based on the Gait Motion and Spatial Modeling

Kosuke Okusa and Toshinari Kamakura

**Abstract**—We study the problem of analyzing and classifying frontal view gait video data. In this study, we suppose that frontal view gait data as a mixing of scale changing, human movements and speed changing parameters. We estimate these parameters using the statistical registration and modeling on a video data. Our gait model is based on human gait structure and temporal-spatial relations between camera and subject. To demonstrate the effectiveness of our method, we conducted two sets of experiments, assessing the proposed method in gait analysis for young/elderly person and abnormal gait detection. In abnormal gait detection experiment, we apply K-nearest-neighbor classifier, using the estimated parameters, to perform normal/abnormal gait detect, and present results from an experiment involving 120 subjects (young person), and 60 subjects (elderly person). As a result, our method shows high detection rate.

**Index Terms**—Gait Analysis, Human Gait Modeling, Statistical Registration, Abnormal Gait Detection

## I. INTRODUCTION

WE study the problem of analyzing and classifying frontal view gait video data. A study on the human gait analysis is very important in the field of the sports/health managements. For instance, gait analysis is one of the important method to detect the Alzheimer disease, infantile paralysis, and any other diseases [1], [2], [3].

Gait analysis is mainly based on motion capture system and video data. The motion capture system can give the precise measurements of trajectories of moving objects, but it requires the laboratory environments and we cannot be used this system in the field study. On the other hand, the video camera is handy to observe the gait motion in the field study.

Gage [4] had been proposed brain paralysis gait analysis using gait video data. Kadaba *et al.* [5] had been discussed importance of lower limb in the human gait using gait video data too. Many gait analysis have recently analyzing using video analysis software (e.g. Dartfish, Contemphas, Silicon Coach). For example, Borel *et al.* [6] and Grunt *et al.* [7] had been proposed infantile paralysis gait analysis using lateral view gait video data.

On the other hand, from the standpoint of statistics, Olshen *et al.* [8] proposed the bootstrap estimation for confidence intervals of the functional data with application to the gait cycle data observed by the motion capture system. Soriano *et al.* [9] proposed the human recognition method based on the data matching techniques using the dynamic time warping of human silhouettes.

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However, most studies have not focused on frontal view gait analysis, because such data has many restrictions on analysis based on the filming conditions. The video data filmed from the frontal view is difficult to analyze, because the subject getting close in to the camera, and data includes the scale-changing parameters [10], [11]. To cope with this, Okusa *et al.* [12] and Okusa & Kamakura [13] proposed a registration for scales of moving object using the method of nonlinear least squares, but Okusa *et al.* [12] and Okusa & Kamakura [13] did not focus on the human leg swing.

Okusa & Kamakura [14] focus on the gait analysis using arm and leg swing model estimated parameters. However, their work was not enough to describe and verification about further details of human gait and spatial modeling and its parameter and speed estimation. In this paper, we describe further details and verification about Okusa & Kamakura [14] models and its applications.

In this study, we focus on the gait analysis using arm and leg swing model estimated parameters. We suppose that frontal view gait data as a mixing of scale changing, human movements and speed changing parameter. We estimate these parameters using the statistical registration and modeling on a video data. Our gait model is based on the human gait structure and temporal-spatial relations between camera and human.

To demonstrate the effectiveness of our method, we conducted two sets of experiments, assessing the proposed method in gait analysis for young/elderly person and abnormal gait detection.

In young/elderly gait analysis experiment, we analyze young 120 subjects and elderly 60 subjects (normal gait: 46, abnormal gait: 14). We discuss the normal and abnormal gait features using the estimated parameters from proposed model. In abnormal gait detection experiment, we apply a K-nearest-neighbor (K-NN) classifier, using the estimated parameters, to perform abnormal gait detection, and present results from an experiment involving 180 subjects from young/elderly gait analysis. As a result, our method shows high detection rate.

The organization of the rest of the paper is as follows. In Section II, we discuss the advantage and problem of frontal view gait analysis. In Section III, we present our models for frontal view gait data based on the statistical registration and gait modeling. In Section IV, we present some performance results showing the effectiveness of our models, based on applying proposed models to 180 subjects gait data. We conclude with a summary in Section V.

## II. FRONTAL VIEW GAIT DATA

In this section, we describe an overview of frontal view gait data. Many of gait analysis using lateral view gait data, because lateral view gait is easy to detect the human gait features. However, in a corridor like structure, the subject is approaching a camera. Such case is difficult observe lateral view gait.

In a lateral view gait, at least two cycles or four steps are needed. For more robust estimation of the period of walking, about 8m is recommended. To capture this movement, the camera distance required is about 9m. Practically, having such a wide space is difficult. On the other hand, frontal view gait video is easy to observe 8m (or more) gait steps [11].

Figure 1 is an example of frontal view gait data recorded by Figure 2 situation. Figure 1 illustrates difficulty of frontal view gait analysis. Even if subject do the same motion with the same timing, frontal view gait data is included scale changing components. Figure 3 shows subject width time-series behavior of frontal view gait data. This figure illustrates frontal view gait data contains many time-series components.



Fig. 1. Frontal view gait data

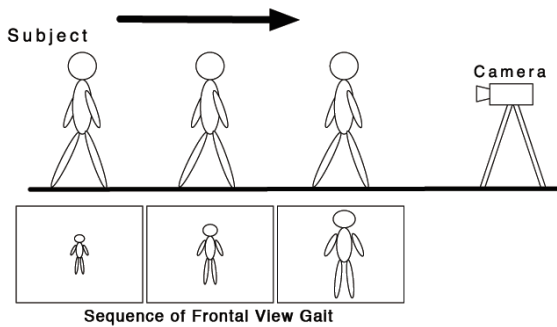


Fig. 2. Filming situation of frontal view gait data

## III. MODELING OF FRONTAL VIEW GAIT DATA

### A. Preprocessing

The raw video data is difficult to observe subject width and height time-series behavior because data contain background. We separate subject from background using inter-frame subtraction method (Eq. 1).

$$\Delta^{(T)} = |I^{(T+1)} - I^{(T)}|, T = 1, \dots, (n-1),$$

$$\Delta^{(T)}(p, q) = \begin{cases} 1 & (\Delta^{(T)}(p, q) > 0) \\ 0 & (\text{Otherwise}). \end{cases} \quad (1)$$

Here,  $\Delta^{(T)}$  is an inter-frame subtraction image,  $I^{(T)}$  is grey scaled video data image at frame  $T$ ,  $(p, q)$  is the pixel coordinate.

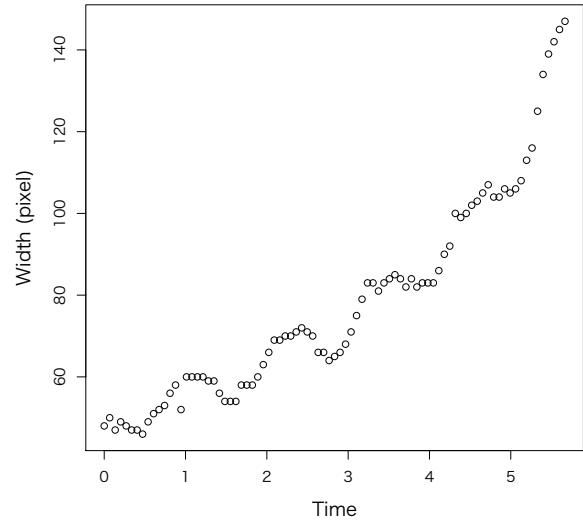


Fig. 3. Time-series behavior of frontal view subject width

a) *Subject Width/Height Calculation:* Inter-frame subtraction method can separate the subject and background. However, it is difficult to measure the time-series behavior of the subject width and height. In this section, we describe the subject width and height calculation method using inter-frame subtraction data.

Let us suppose that inter-frame subtraction image is binary matrix. We can measure the subject height and width by integration calculation of row and column at each frame. In this study, we focus on the human gait arm and leg swing of the frontal view gait. We assume that subject width and height time-series behavior consist of the arm and leg swing behavior.

### B. Relationship between camera and subject

Figure 4 shows a relationship between camera and subject. Width and height modeling has same structure. In this section, we describe the subject width modeling. We can assume simple camera structure. We consider the virtual screen exists between observation point and subject, and we define subject width on the virtual screen  $x_i$  at  $i$ -th frame ( $i = 1, \dots, n$ ).

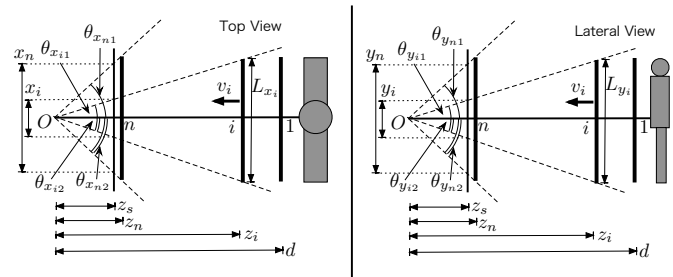


Fig. 4. Relationship between camera and subject

Here we define  $z_i, z_j$  as distance between observation point and subject at  $i$ -th,  $j$ -th frame,  $z_s$  as distance between observation point and virtual screen,  $\theta_{xi1}, \theta_{xi2}$  as subject angle of view from observation point at  $i$ -th frame,  $d$  as

distance between observation point and 1st frame,  $v_i$  as subject speed at  $i$ -th frame. Okusa *et al.* [12] defined the subject length  $L$  was constant. We assume that  $L$  has the time-series behavior and we define  $L_i$  is the subject length at  $i$ -th frame.

$x_i$  at  $i$ -th frame depends on  $\theta_{x_{i1}}, \theta_{x_{i2}}$  as shown in Figure 4.

$$x_i = z_s(\tan \theta_{x_{i1}} + \tan \theta_{x_{i2}}). \quad (2)$$

Similarly, the subject length at  $i$ -th frame is

$$L_{x_i} = z_i(\tan \theta_{x_{i1}} + \tan \theta_{x_{i2}}). \quad (3)$$

From Eq.(2), Eq.(3), ratio between  $x_n$  and  $x_i$  is

$$\frac{x_n}{x_i} = \frac{L_{x_n} z_i}{L_{x_i} z_n} \quad (4)$$

Frame interval is equally-spaced (15 fps). Okusa *et al.* [12] assumed the average speed is constant. We can assume that average speed from  $i$ -th frame is  $(n-i) = (z_i - z_n)/\bar{v}$ , therefore  $z_i$  is  $z_i = z_n - \bar{v}(n-i)$ . We substitute  $z_i$  to Eq.(4)

$$x_i = \frac{M_{x_i} \gamma}{\gamma + (n-i)} x_n + \epsilon_i, \quad (5)$$

where  $\gamma$  is  $z_n/\bar{v}$ ,  $M_{x_i}$  is  $L_{x_i}/L_{x_n}$ ,  $\epsilon_i$  is noise. From Eq.(5), predicted value  $\hat{x}_i^{(n)}$  is registration from  $i$ -th frame's scale to  $n$ -th frame's scale

$$\hat{x}_i^{(n)} = \frac{\gamma + (n-i)}{M_{x_i} \gamma} x_i. \quad (6)$$

Similarly, we can define subject height as

$$y_i = \frac{M_{y_i} \gamma}{\gamma + (n-i)} y_n + \epsilon_i, \quad (7)$$

where  $M_{y_i}$  is  $L_{y_i}/L_{y_n}$ .

Next, we discuss the scale changing, human movement, and speed changing parameter estimation model.

### C. Scale changing parameter estimation

From Eq.(5), scale parameter is  $\gamma$ . Solve Eq.(5) for  $\gamma$  shows

$$\gamma = \frac{x_i(n-i)}{x_i - M_{x_i} x_n}. \quad (8)$$

Here  $\gamma$  is the ungaugable parameter, and we estimate it using nonlinear least squares method

$$S(\gamma, M_{x_i}) = \sum_{i=1}^n \left\{ x_i - \frac{M_{x_i} \gamma}{\gamma + (n-i)} x_n \right\}^2. \quad (9)$$

### D. Human movement parameter estimation

$M_{x_i}$  and  $M_{y_i}$  are movement model of the subject. If the subject is the rigid body, movement model  $M_{x_i}$  and  $M_{y_i}$  are constant. Meanwhile, human gait is not a constant.  $M_{x_i}$  and  $M_{y_i}$  needs the movement model because the subject body is moving wildly.

b) *Human gait modeling: arm swing*: Collins *et al.* [15] has reported that arm swing is an very important role in the gait motion based on the simple gait model. We consider the human gait modeling based on Collins *et al.* [15] model (see Figure 5, Figure 6).

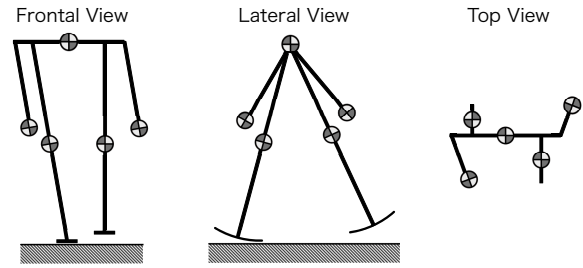


Fig. 5. Gait model

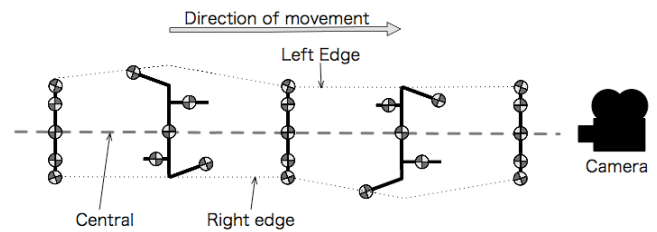


Fig. 6. Gait pattern of proposed model

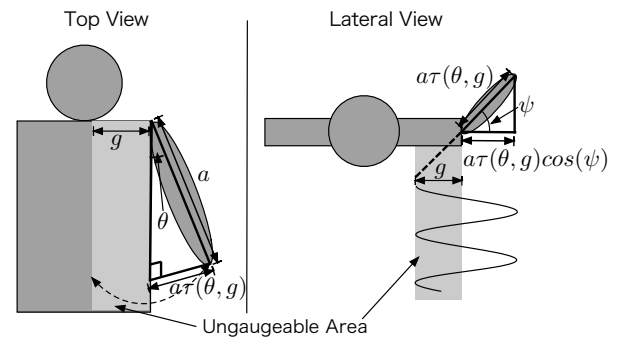


Fig. 7. Arm swing model

It seems reasonable to think that arm is single pendulum. Collins *et al.* [15] model assumed the arm swing is move to anteroposterior direction. Our model, on the other hand, can assume that arm swing move to an oblique direction (Figure 7).

Figure 7's model has an ungaugable area. Our method's width/height calculation is based on integration calculation of row and column at each frame. If the arm move to inside body area, arm length is ungaugable. Arm swing model is

$$x_i = \frac{\left( \frac{W(P_1, P_2, Q_1, Q_2, g_1, g_2, f, i)}{W(P_1, P_2, Q_1, Q_2, g_1, g_2, f, n)} + s \right) \gamma}{\gamma + (n-i)} x_n + \epsilon_i$$

$$W(P_1, P_2, Q_1, Q_2, g_1, g_2, f, i) = P_1 \tau(fi + Q_1, g_1) + P_2 \tau(fi + Q_2, g_2)$$

$$\tau(\theta, g) = \begin{cases} \sin(\theta) + g & (\sin(\theta) + g > 0) \\ 0 & (\text{Otherwise}) \end{cases} \quad (10)$$

where  $P_1 = a_1 \cos(\psi)$  and  $P_2 = a_2 \cos(\psi)$ .  $P_1 \tau(fi + Q_1, g_1)$  and  $P_2 \tau(fi + Q_2, g_2)$  are right and left arm model respectively. From Eq.(10), we estimate each gait parameter using nonlinear least squares method.

$$S(\gamma, P_1, P_2, Q_1, Q_2, g_1, g_2, f, s) = \sum_{i=1}^n \left\{ x_i - \frac{\left( \frac{W(P_1, P_2, Q_1, Q_2, g_1, g_2, f, i)}{W(P_1, P_2, Q_1, Q_2, g_1, g_2, f, n)} + s \right) \gamma}{\gamma + (n - i)} x_n \right\}^2 \quad (11)$$

Here,  $f$  is gait cycle frequency,  $s$  is adjustment parameter,  $P_1, P_2$  are arm swing amplitude parameters,  $Q_1, Q_2$  are arm phase parameters, and  $g_1, g_2$  are ungaugable area parameters.

c) *Human gait modeling: leg swing*: The leg swing modeling is simpler than arm swing model because the leg model does not have a ungaugable area. Okusa *et al.* [12] and Okusa & Kamakura [13] does not consider the leg swing. It seems reasonable to think like arm swing that leg swing is single pendulum (Figure 8).

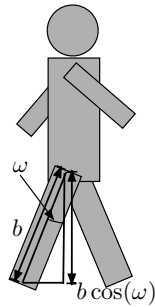


Fig. 8. Leg swing model

Leg swing model is

$$y_i = \frac{\left( \frac{H(b_1, Q_3, f, i)}{H(b_1, Q_3, f, n)} + s \right) \gamma}{\gamma + (n - i)} y_n + \epsilon_i$$

$$H(b_1, Q_3, f, i) = b_1 \cos(fi + Q_3). \quad (12)$$

Here  $b_1$  is leg swing amplitude parameter, and  $Q_3$  is leg phase parameter.

#### E. Speed changing parameter estimation

Frontal view video data is difficult to see the subject's speed. If our gait model is correct, observed value  $x_i$  and  $y_i$  is same as the fitted value of gait model at point  $\ell_i$ . Previous model's  $\ell_i$  assumes equally spaced ( $\ell_i = i = 1, \dots, n$ ). We estimate  $\ell_{x_i}$  and  $\ell_{y_i}$  value for minimize the observed value and model fitted value at  $\ell_i$ . We can define estimated value  $\ell_{x_i}$  and  $\ell_{y_i}$  as a virtual space coordinate at i-th frame (Figure 9).

Eq.5, Eq.7 with the coordinate estimation shows

$$x_i = \frac{M_{x_i} \gamma}{\gamma + (n - \ell_{x_i})} x_n + \epsilon_i$$

$$y_i = \frac{M_{y_i} \gamma}{\gamma + (n - \ell_{y_i})} y_n + \epsilon_i. \quad (13)$$

Here,  $\ell_{x_i}, \dots, \ell_{x_n}$  and  $\ell_{y_i}, \dots, \ell_{y_n}$  are virtual space coordinate parameters of width and height respectively. From

Eq.13, arm swing and leg swing model with the coordinate estimation shows Eq.14, Eq.15.

$$x_i = \frac{\left( \frac{W(P_1, P_2, Q_1, Q_2, g_1, g_2, f, \ell_{x_i})}{W(P_1, P_2, Q_1, Q_2, g_1, g_2, f, \ell_{x_n})} + s \right) \gamma}{\gamma + (n - \ell_{x_i})} x_n + \epsilon_i$$

$$W(P_1, P_2, Q_1, Q_2, g_1, g_2, f, \ell_{x_i}) = P_1 \tau(f \ell_{x_i} + Q_1, g_1) + P_2 \tau(f \ell_{x_i} + Q_2, g_2)$$

$$\tau(\theta, g) = \begin{cases} \sin(\theta) + g & (\sin(\theta) + g > 0) \\ 0 & (\text{Otherwise}). \end{cases} \quad (14)$$

$$y_i = \frac{\left( \frac{H(b_1, Q_3, f, \ell_{y_i})}{H(b_1, Q_3, f, \ell_{y_n})} + s \right) \gamma}{\gamma + (n - \ell_{y_i})} y_n + \epsilon_i$$

$$H(b_1, Q_3, f, \ell_{y_i}) = b_1 \cos(f \ell_{y_i} + Q_3). \quad (15)$$

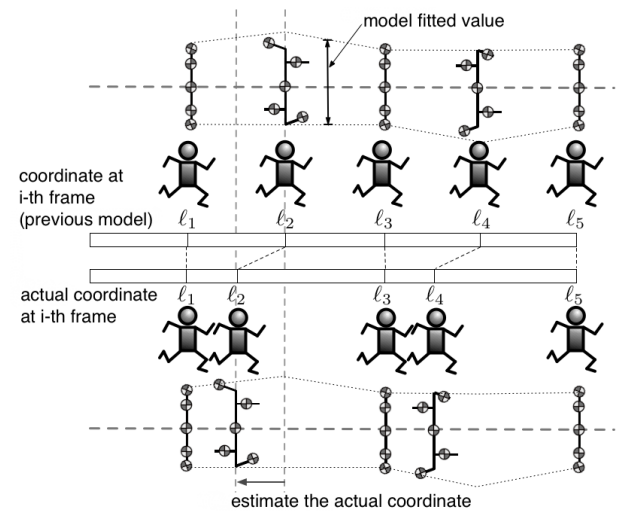


Fig. 9. Virtual space coordinate estimation

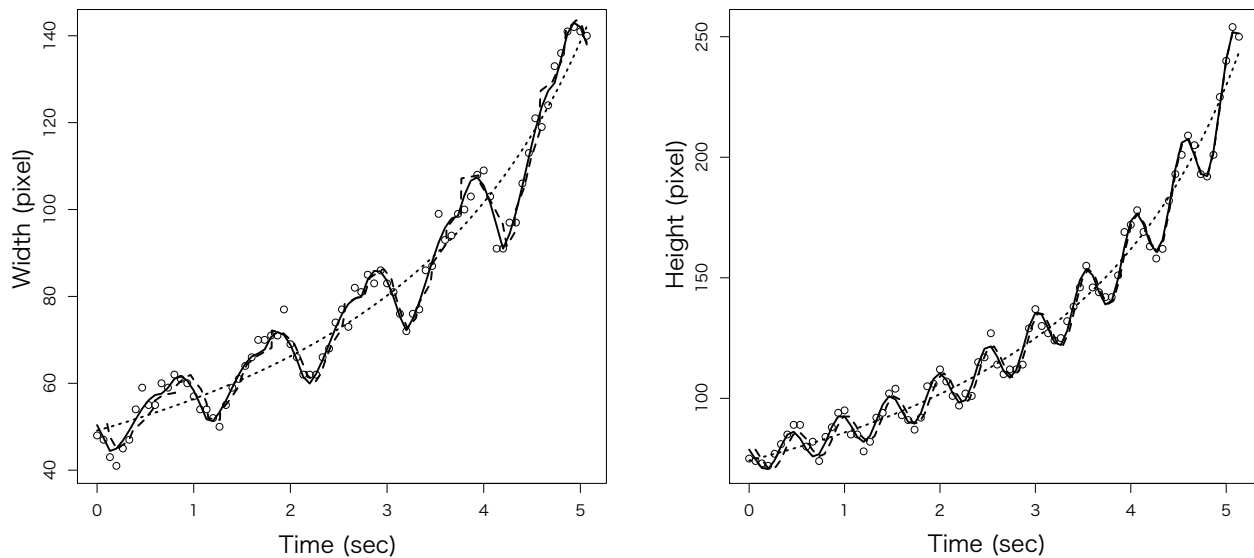
We suppose that virtual space coordinate of subject is  $\hat{\ell}_i = (\ell_{x_i} + \ell_{y_i})/2$ . Then, we can assume that subjects speed is 1st order difference of  $\hat{\ell}_i$ , and acceleration is 2nd order difference of  $\hat{\ell}_i$ .

We estimate these models parameters using Okusa & Kamakura [16] method. This method is very stable and very fast to estimate these parameters.

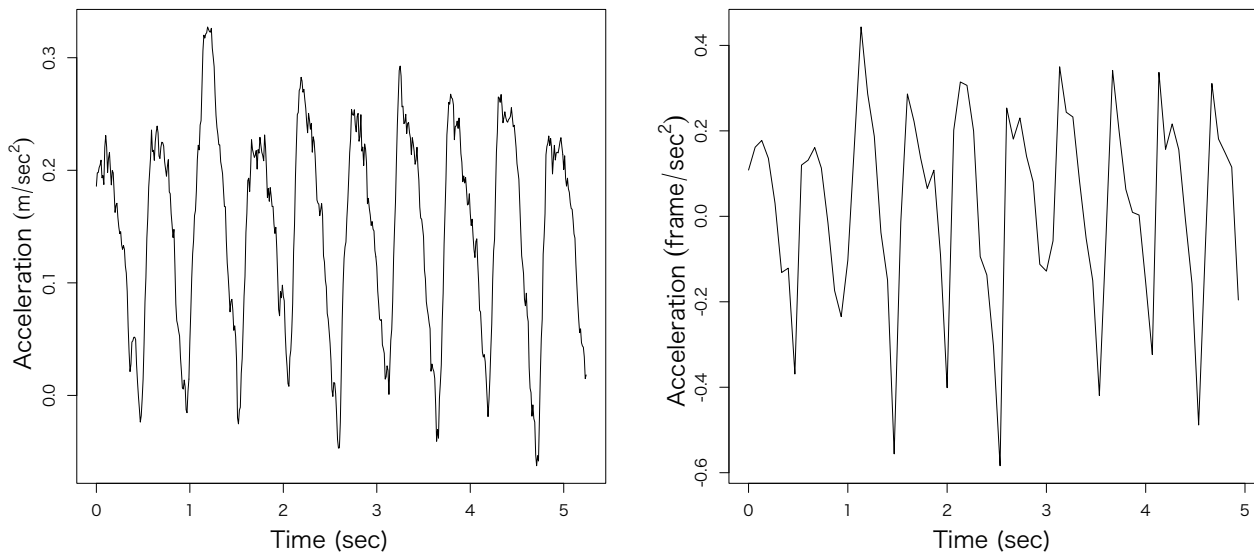
#### F. Gait parameter estimation

In this section, we discuss the gait parameter estimation. We took movie of 10 subjects walking video data from frontal view (10 steps, Male, average height: 176.4cm, sd: 3.07cm) and apply to our proposed method. To validate the effectiveness of Eq.14 & Eq.15 model, we observe the gait acceleration of hip at the same time. We use Wireless Technology WAA-006 acceleration/angular velocity sensor.

Figure 10(a) (left side) is plot of the subject width(pixel) time-series behavior. Here dotted line represent fitted value of Eq.5 (scale variant estimation model), continuous line represent fitted value of Eq.10 (scale variant + arm movements estimation model), dashed line represent fitted value of Eq.14 (scale variant + arm movements + speed variant estimation model). Similarly, Figure 10(a) (right side) is plot of the subject height(pixel) time-series behavior. Here dotted



(a) Model fitting: width (left side), height (right side)



(b) Observed acceleration (left side) and estimated acceleration (right side)

Fig. 10. Fitted value and estimated acceleration

line represent fitted value of Eq.7 (scale variant estimation model), continuous line represent fitted value of Eq.12 (scale variant + leg movements estimation model), dashed line represent fitted value of Eq.15 (scale variant + leg movements + speed variant estimation model).

Figure 10(b) (left side) is observed acceleration of hip and 10(b) (right side) is estimated acceleration from Eq.14 and Eq.15 model. Eq.14 and Eq.15 model can not estimate acceleration scale, because estimated acceleration is second order difference of  $\hat{\ell}_i$ . However, from Figure 1, we think our proposed model can estimate gait cycle and its timings.

Table I is Residual Sum of Squares (RSS), Akaike Information Criterion (AIC) [17] and Consistent Akaike's Information Criterion (cAIC) [18] value of first order regression, second order regression, Eq.5 and Eq.7, Eq.10 and Eq.12, and Eq.14 and Eq.15 models of width and height data.

In Table I, most minimal AIC model is Eq.10, Eq.12.

Meanwhile, most minimal RSS and cAIC model are Eq.14, Eq.15. Burnham & Anderson [19] strongly recommend using cAIC, rather than AIC, if number of data  $n$  is small or number of parameters  $k$  is large. Since cAIC converges to AIC as  $n$  gets large, cAIC generally should be employed regardless. Therefore, we select the Eq.14, Eq.15 model. Figure 10(a), 10(b) and Table I illustrates our method has a good performance.

In next section, we discuss the effectiveness of our method.

#### IV. EXPERIMENTAL DETAILS AND RESULTS

To demonstrate the effectiveness of our method, we conducted two sets of experiments, assessing the proposed method in gait analysis for young/elderly person and abnormal gait detection. We use SONY DCR-TRV70K camera. Frame rate of video data is 15 fps and resolution is  $640 \times 480$ .

TABLE I  
RSS, AIC, CAIC VALUE OF WIDTH AND HEIGHT DATA

Model	Method	Subject ID									
		A	B	C	D	E	F	G	H	I	J
1st order regression	RSS	9428.58	8051.10	5141.30	6834.98	8659.38	5882.43	3231.88	3867.81	7402.96	3695.14
	AIC	607.97	601.95	541.97	569.94	627.29	558.38	501.09	508.77	607.95	545.31
	cAIC	608.03	602.00	542.02	569.99	627.34	558.44	501.15	508.83	608.00	545.36
2nd order regression	RSS	5260.57	2175.70	1654.54	3808.77	3250.35	1190.80	912.90	2062.37	2395.75	2909.74
	AIC	563.88	499.28	457.80	526.91	547.96	437.39	408.28	464.24	517.43	527.96
	cAIC	564.04	499.43	457.96	527.08	548.11	437.55	408.44	464.41	517.59	528.11
Eq.5 & Eq.7 model	RSS	5271.18	1367.39	1888.35	3077.40	2707.40	891.99	706.91	2052.45	2062.45	2865.62
	AIC	562.04	460.12	465.85	508.50	530.79	413.14	387.10	461.88	503.15	524.72
	cAIC	564.19	462.28	468.01	510.66	532.94	415.30	389.26	464.05	505.30	526.88
Eq.10 & Eq.12 model	RSS	174.52	94.46	112.06	425.63	306.59	286.70	65.99	87.02	0.40	0.56
	AIC	308.81	262.32	267.19	372.17	366.00	341.74	225.25	244.00	-180.87	-150.70
	cAIC	311.42	264.90	269.91	374.86	368.46	344.43	228.02	246.81	-178.37	-148.17
Eq.14 & Eq.15 model	RSS	84.31	33.02	60.49	189.46	95.82	149.21	61.39	27.33	0.02	0.10
	AIC	409.33	338.23	372.33	463.84	435.47	445.45	369.83	306.29	-258.9562	-130.86
	cAIC	-1157.07	-1263.77	-1089.67	-1032.56	-1275.73	-1050.95	-1058.17	-1088.11	-1896.956	-1768.86
Number of frames:		79	80	76	77	83	77	75	74	81	79

In this paper, we focus on  $\hat{\gamma}$  (speed parameter),  $(\hat{P}_1 + \hat{P}_2)/2$  (width amplitude parameter), and  $\hat{b}_1$  (height amplitude parameter).

#### A. Gait analysis: young person

In this experiment we took movie of 120 subjects walking video data from frontal view (10 steps, Male: 96 (average height: 173.24cm, sd: 5.64cm), Female: 24 (average height: 156.25cm, sd: 3.96cm)) and apply to our proposed method for the gait analysis.

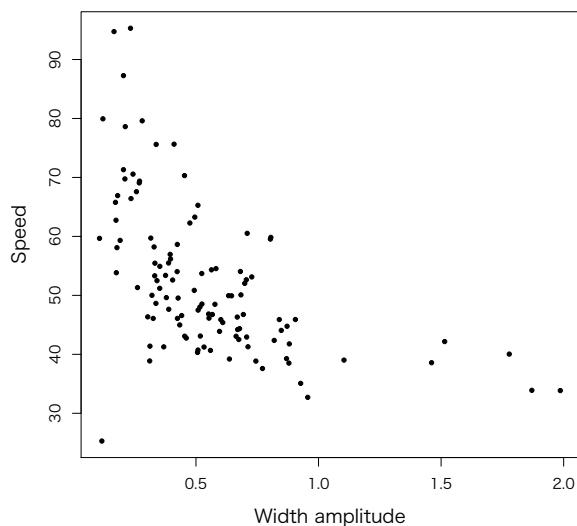


Fig. 11. Width amplitude vs speed (young)

Figure 11, 12 are width amplitude vs speed and height amplitude vs speed. The important point to note is that speed parameter  $\hat{\gamma}$  is  $z_n/\bar{v}$ . If the subject walking fast, speed parameter  $\hat{\gamma}$  is small. From Figure 11, 12, width amplitude vs speed and height amplitude vs speed have a nonlinear relationship. This results means, if the subject's arm swing and leg swing moving strongly, subject's walking speed is fast.

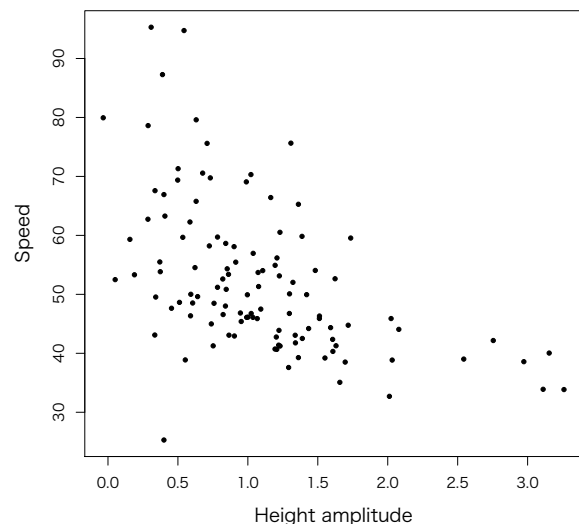


Fig. 12. Height amplitude vs speed (young)

#### B. Gait analysis: elderly person

In this experiment we took movie of 60 subjects walking video data from frontal view (10 steps / average age: 76.97 · sd: 4.16 / abnormal gait subjects; average age: 77.56 · sd: 4.35 / normal gait subjects; average age: 75.37 · sd: 3.18) and apply to our proposed method for the gait analysis.

Figure 13, 14 are width amplitude vs speed and height amplitude vs speed. Black and white circle means normal and abnormal gait subjects respectively. From Figure 13, 14, normal gait subject width amplitude vs speed and height amplitude vs speed have a nonlinear relationship like a young person. However, on the other hand, abnormal gait subject estimated parameters does not have nonlinear relationship. These abnormal gait parameters clustered in different place from normal gait subjects. The result leads to our presumption that the abnormal gait subject trying to moving fast, but this effort is not effective to moving speed.

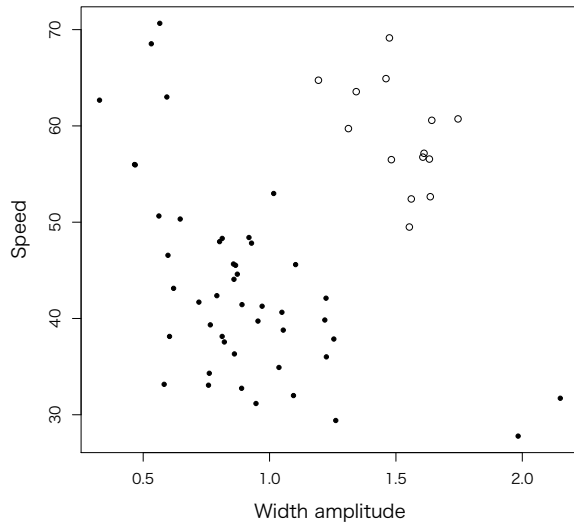


Fig. 13. Width amplitude vs speed (elderly)

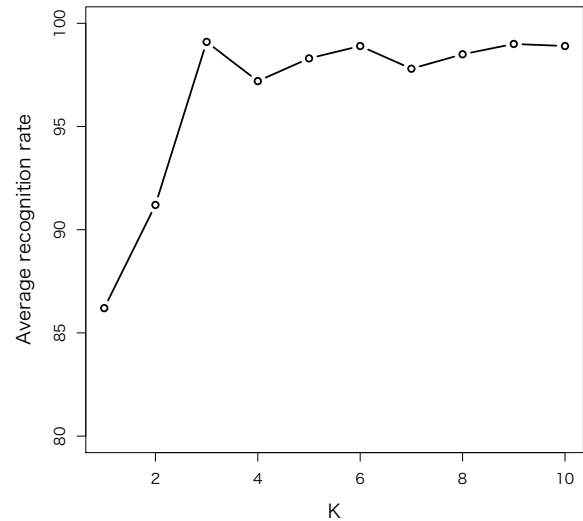
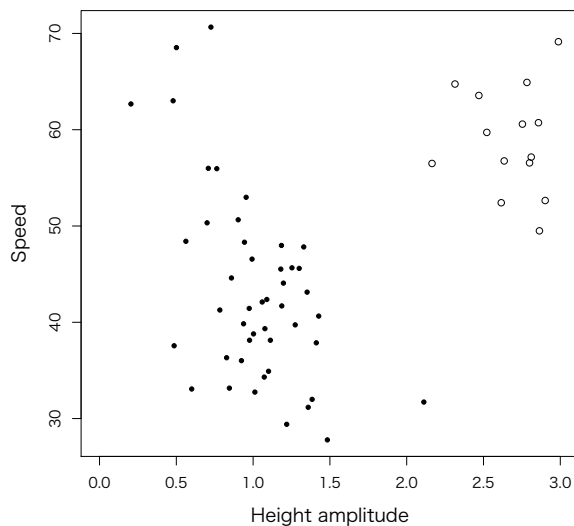

 Fig. 15. average recognition rate of  $K=1, \dots, 10$ 


Fig. 14. Height amplitude vs speed (elderly)

### C. Abnormal gait detection

In this section, we discuss the abnormal gait detection. Okusa & Kamakura [14] only focused on  $K=3$  case. In this paper, we apply K-NN classifier ( $K=1, \dots, 10$  cases), using the all estimated parameters, to perform normal/abnormal gait detect, and present results from an experiment involving 120 subjects (young person), and 60 subjects (elderly person). To evaluate our estimated parameters, we apply these parameters to leave-one-out cross-validation test.

Figure 15 is the average detection rate of K-NN classifier. x-axis and y-axis means K value and average detection rate respectively. Figure 15 shows estimated parameters are good feature values of the human gait. Most high performance case is  $K=3$ . However,  $K \geq 3$  cases are high performance too like  $K=3$  case. From the standpoint of calculation cost, we recommend to use  $K=3$ .

Table II is average detection rate of normal/abnormal gait

( $K=3$ ). Table II shows our estimated parameters may be used for the normal/abnormal gait detection.

TABLE II  
NORMAL/ABNORMAL GAIT AVERAGE DETECTION RATE(%)

	Normal Gait	Abnormal Gait
Normal Gait	98.2	1.8
Abnormal Gait	0	100

### V. CONCLUSIONS

In this article, focusing on the human gait cycles, we consider the human gait modeling based on simple gait structure. We estimate the parameters of the human gait cycles using the method of nonlinear least squares. We also show that estimated parameters may be used for the human gait analysis and abnormal gait detection. Experimental results verify that our model can estimate the various parameters and these parameters are good feature values of the human gait.

We plan to implement this scheme for the gait authentication. The primary concern in gait authentication is realtime processing and fineness. In next phase, we focus on these problems.

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