Cluster Analysis Based on Indicator System on the Development of Digital Economy in Guangdong

Xue Deng, Keyao Zheng, Ye Xiong

Abstract-The digital economy is regarded as a new economic form that achieves high-quality economic development, which is a new engine for social and economic development. Research on the social and economic development in the context of the digital economy plays a significant part in optimizing the social economic system in the digital age. We divide the digital economy into four major types, "basic type, technology type, integration type and service type". In this essay, we will select 5 indicators to evaluate these types and set up a digital economy index evaluation system with 5 indicators. Under the indicator system, systematic clustering and K-means clustering were performed on 31 provinces and cities across the country. Compared with each province or cities, the advantages and disadvantages of the overall digital economy and the four digital economy types in different provinces or cities are analyzed based on the comprehensive factor scores, which provides a strong basis for the future development of the digital economy in Guangdong Province. Thus, this essay will give some suggestions for the growth of Guangdong Province in digital economy.

Index Terms—Digital economy, Indicator evaluation system, Systematic clustering, K-means clustering, Factor scores

I. INTRODUCTION

Asian economic development. Rita et al. [2] combined

Manuscript received January 22, 2021; revised July 2, 2021. This research was supported by the "Humanities and Social Sciences Research and Planning Fund of the Ministry of Education of China, No. 18YJAZH014-x2lxY9180090", "Natural Science Foundation of Guangdong Province, No. 2019A1515011038", "Guangdong Province Characteristic Innovation Project of Colleges and Universities, No. 2019GKTSCX023", "Soft Science of Guangdong Province, No. 2018A070712006, 2019A101002118".

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comprehensive indices into a new framework to study a country's social economic system over time. According to the data of Eurostat from 2001 to 2016, Monica et al. [3] carried out research into digital economic growth and the progress of digital in the EU by analyzing and selecting a certain amount of specific indices, and finally determined the policies and measures which can foster the digital economic growth in EU states. The rapid increase was explained by Schweighofer et al. [4] in the importance of technology intensive learning. He pointed out the known relationship between technology intensive learning and digital economy, but the relationship between digital economy and technology promoted learning was rarely studied. Talar [5] assessed the consistency of the concept and new challenges of the European digital economy in 2020. The model of the evolution of digital control was built by Landini [6].

Based on the above research, this paper believes that digital economy is worth studying as a new area in the 20th century. Del et al. [7] explained the understanding of today's digital economy and determined its scale and impact on enterprises, thus demonstrating the need to develop its theoretical basis. In addition, an empirical study was conducted in the context of Spain. Berdykulova et al. [8] revealed the essence of digital economy and studied the shortcomings of Kazakhstan's digital economy through examples. Protopopova et al. [9] studied the rationalization of the relevance of digital economy development in Russia, the comparative analysis between Russia and other major countries in digital economy development, and the reasons and solutions of Russia's inability to establish digital economy in recent ten years. Modern Russia was taken by Skiter et al. [10] as an example to study the development trend and Prospect of national food security under the condition of digital economy. Dong et al. [11] summarized the characteristics and measurement methods of digital economy. And the measuring method of digital economy was studied. Nudurupati et al. [12] discussed the improvement and practice of PMM model to make it more flexible and reflect the progress of digital economy.

However, it is known that the research on digital economy is almost qualitative. The development path of digital economy is lack of data support through qualitative research. Therefore, we can carry out quantitative research on the use of cluster analysis, factor analysis and other statistical methods of digital economy in Guangdong. Economic development path should be optimized. Wei et al. [13] used cluster analysis to make development strategy. Kim et al. [14] showed division of related fields so that we can divide the digital economy into 4 types. An memetic algorithm for clustering tasks was proposed by Jiang et al. [15]. The data processing was used for reference in this paper. For the sake of understanding the status of the 4 digital economic types in China and the overall development level of digital economy in Guangdong. This paper conducts cluster analysis on the data of 31 provinces and cities. A comprehensive factor score model is established through factor analysis to cross verifies the results of cluster analysis, so as to explore the shortcomings of digital economy development in Guangdong compared with other provinces (cities).

In Section II, the basic knowledge of cluster analysis is described. Building a new indicator system is in Section III. In Section IV, cluster analysis is carried out with examples. The Section V summarizes comparative analysis between cluster analysis and factor analysis, and put forward advice.

II. BASIC PRINCIPLES OF CLUSTER ANALYSIS

A. System Clustering Algorithm

A.1 Basic content

According to Gao [16], six clustering algorithms are as follows:

(1) The shortest distance method

The shortest distance between all sample pairs in two categories is as follow: $D_{KL} = \min_{i \in G_k, j \in G_L} d_{ij}$. This is the shortest distance method. The distance between sample *i* and sample *j* is represented by d_{ij} , G_1, G_2, L is a class, and the distance between G_K and G_L is represented by D_{KL} . The recurrence formula is

$$D_{MJ} = \min_{i \in G_M, j \in G_J} d_{ij}$$

= min { min_{i \in G_K, j \in G_J} d_{ij}, min_{i \in G_L, j \in G_J} d_{ij} }
= min \{ D_{KL}, D_{LJ} \}. (1)

(2) Longest distance method

The distance between the two categories is the farthest distance among the samples in the two categories is as follow: $D_{KL} = \max_{i \in G_k, j \in G_L} d_{ij}$. When class G_K and class G_L synthesize a new class G_M , then the distance between G_M

and other classes G_J is $D_{MJ} = \max\{D_{KL}, D_{LJ}\}$.

(3) Intermediate distance method

Taking the middle distance for the shortest distance method and the longest distance method mentioned above. When G_{K} and G_{L} are combined into a new class G_{M} , for a certain class G_{J} , D_{KL} , D_{LJ} , D_{KJ} are taken as the side lengths to form a triangle, and the center line D_{MJ} of D_{KL} side is made. At this time, we can know from geometric knowledge that:

$$D_{_{MJ}}^2 = \frac{1}{2}D_{_{KJ}}^2 + \frac{1}{2}D_{_{LJ}}^2 - \frac{1}{4}D_{_{KL}}^2.$$
 (2)

(4) Class average method

The average value of the square distance between every two samples in the two categories is the class average method, and the formula is

$$D_{KL}^{2} = \frac{1}{n_{K}n_{L}} \sum_{i \in G_{K}, j \in G_{L}} d_{ij}^{2}.$$
 (3)

The recurrence formula is as follows:

$$D_{MJ}^{2} = \frac{n_{K}}{n_{M}} D_{KJ}^{2} + \frac{n_{L}}{n_{M}} D_{LJ}^{2}.$$
 (4)

(5) Barycenter method

The distance between the two categories is defined as the Euclidean distance of the center of gravity. Suppose \bar{x}_{k} and \bar{x}_{L} are the centers of gravity of G_{k} and G_{L} , then the distance between G_{k} and G_{L} is

$$D_{KL} = d_{\overline{x}_K \overline{x}_L}^2 = (\overline{x}_K - \overline{x}_L)^T (\overline{x}_K - \overline{x}_L).$$
⁽⁵⁾

The recurrence formula is as follows:

$$D_{MJ}^{2} = \frac{n_{K}}{n_{M}} D_{KJ}^{2} + \frac{n_{L}}{n_{M}} D_{LJ}^{2} - \frac{n_{K} n_{L}}{n_{M}^{2}} D_{KL}^{2}.$$
 (6)

(6) Method of sum of squares of deviation

Let G_M be the combined category of G_K and G_L , then the sums of deviation squares for G_K , G_L and G_M are

$$W_{K} = \sum_{i \in G_{K}} (x_{(i)} - \overline{x}_{K})^{T} (x_{(i)} - \overline{x}_{K}),$$
(7)

$$W_{L} = \sum_{i \in G_{L}} (x_{(i)} - \overline{x}_{L})^{T} (x_{(i)} - \overline{x}_{L}),$$
(8)

$$W_{M} = \sum_{i \in G_{M}} (x_{(i)} - \overline{x}_{M})^{T} (x_{(i)} - \overline{x}_{M}).$$
(9)

Where \overline{x}_{K} , \overline{x}_{L} and \overline{x}_{M} are the focus of G_{K} , G_{L} and G_{M} respectively, and the dispersion degree of samples in each class is represented by W_{K} , W_{L} and W_{M} . If G_{K} and G_{L} are two classes which are close to each other, then the value of the sum of squares of deviations $W_{M} - W_{K} - W_{L}$ will be smaller after merging into a new class. Therefore, the square distance between G_{K} and G_{L} can be defined as: $D_{KL}^{2} = W_{M} - W_{K} - W_{L}$. This is the method of sum of squares of deviation in system clustering. The recurrence formula is as follows:

$$D_{MJ}^{2} = \frac{n_{J} + n_{K}}{n_{J} + n_{M}} D_{KJ}^{2} + \frac{n_{J} + n_{L}}{n_{J} + n_{M}} D_{LJ}^{2} - \frac{n_{J}}{n_{J} + n_{M}} D_{KL}^{2}.$$
 (10)

To sum up, the basic steps of systematic clustering can be summarized. Suppose there are n samples.

A.2 Basic steps

The basic steps of using hierarchical clustering in R software are as follows:

Step 1:Calculate the distance between every two samples;

- **Step 2:**Construct *n* classes and each sample is a class;
- Step 3: Merge the two nearest classes into a new class;
- **Step 4:**Calculate the distance between the new class and the existing class;
- **Step 5:**Repeat Step 3 and Step 4 until there is only one category left;
- **Step 6:**Draw a genealogy, and determine the number of classes and the samples in the class according to the genealogy.
- B. K-means clustering
- B.1 Basic content

Let
$$x_i = (x_{i1}, x_{i2}, L, x_{in})^T$$
, $y_i = (y_{i1}, y_{i2}, L, y_{in})^T$ be the data

of two samples. The Euclidean distance is defined as

$$d(x_i, y_i) = \sqrt{\sum_{m=1}^{n} (x_{im} - y_{im})^2}.$$
 (11)

If C_i is the *i*-th category and T_i is the number of samples in Category C_i , then the centroid of data in the same category is

$$\mu_i = \frac{1}{|T_i|} \sum_{x_i \in C_i} x_i.$$
(12)

B.2 Basic steps

The basic steps of K-means algorithm are as follows:

Step 1:Determine the number of clusters *k* ;

Step 2:Determine *k* initial clustering centers;

- **Step 3:**Calculate the distance from each sample to each cluster center according to Formula (11), and allocate the samples to the nearest cluster;
- **Step 4:**Recalculate the centroids of the existing classes as *k* new cluster centers by Formula (12);
- **Step 5:**Repeat Step 3 and Step 4. When the centroid remains unchanged, the class and the sample in the category are obtained.

III.BUILDING THE INDICATOR SYSTEM

According to the white paper of the release of Chinese digital economy indicator in 2017 issued by CCID consultants, digital economy can be divided into five types: basic, resource-based, technological, integrated and service-oriented. According to the availability and effectiveness of the indicator data, the digital economy indicator system in line with Guangdong Province is established by combined with the index system in Ning [17], as shown in Table I:

In Table I, the basic digital economy indicators start with the two respects of basic telecommunications and network. The evaluation system select indicators such as optical cable line length, telephone penetration rate, Internet broadband access users and so on to measure the popularization and growth in telecommunications and Internet.

Technological digital economy indicators should start with the view of digital technology, including block-chain, big data, AI and other emerging industries into the indicator system. However, due to the difficulty of data acquisition, its industry is primarily used to measure the development of digital technology. Thus, some representative data are used as the evaluation indicators of technological digital economy, as follows: the information technology service income, the total amount of telecommunication business, the income of software business and so on.

The indicator of integrated digital economy is analyzed from the perspective of industry, agriculture and digital economy. These selected indicator are to measure the application of enterprises, industry and agriculture informatization. Hence the 5 indicators are selected as above.

From the integration of digital economy and service industry, service-oriented digital economy indicator shows the significant element of digital technology in life, study and entertainment. Five indicators are adopted, including amount of public information on government websites, e-commerce transaction volume, amount of electronic reading room terminals in public libraries, amount of digital TV users, scientific research, technical services and social fixed asset investment in geological exploration industry.

		EVALUATION INDICATOR SYSTEM OF DIGITAL ECONOMY IN GUANGDONG PROVINCE	
Indicator category	Indicator expression	Indicator name	Unit
	<i>X</i> ₁	Length of optical cable line	km
Basic	X_{2}	Telephone penetration rate	Department / person
digital	X_{3}	Internet broadband access users	Ten thousand households
economy	X_4	Number of websites	Ten thousand
	X_5	Number of domain names	Ten thousand
	X_6	IT service revenue	Ten thousand yuan
Technolog	X_7	Software revenue of embedded system	Ten thousand yuan
ical digital	X_8	Total telecom services	100 million yuan
economy	X_9	Software business income	Ten thousand yuan
	X_{10}	Information transmission, computer service and fixed asset investment in software industry	100 million yuan
	X ₁₁	Increase of rural e-commerce comprehensive demonstration counties	Unit / year
Integrated	X_{12}	Number of P & D projects of Industrial Enterprises above Designated Size	term
digital	X ₁₃	Proportion of enterprises with e-commerce transaction activities	%
economy	X_{14}	Quantity of enterprise informatization	unit
	X_{15}	Number of enterprises integrated with industrialization and industrialization	unit
	X_{16}	E-commerce transaction volume	100 million yuan
Service	X_{17}	Amount of public information on government websites	strip
oriented	X_{18}	Amount of terminals in electronic reading room of Public Library	Number
digital economy	X_{19}	Amount of digital TV users	Ten thousand households
y	X_{20}	Scientific research, technical services and social fixed asset investment in geological exploration industry	100 million yuan

TABLE I EVALUATION INDICATOR SYSTEM OF DIGITAL ECONOMY IN GUANGDONG PROVINCE

Volume 51, Issue 3: September 2021

IV. EMPIRICAL RESEARCH

A. Experimental Data

TABLE II-(a) Standardized Data										
Provinces (cities)	X_1	X_2	<i>X</i> ₃	X_4	X_5	X_6	X ₇	X_8	X_9	X_{10}
Beijing	-1.06	3.51	-0.64	2.80	2.74	2.68	-0.35	-0.03	2.25	0.29
Tianjin	-1.24	0.04	-0.90	-0.48	-0.53	-0.04	-0.22	-0.86	-0.15	-0.24
Hebei	0.57	-0.36	0.85	-0.07	-0.27	-0.55	-0.38	0.35	-0.58	0.27
Shanxi Inner Mongolia	-0.16 -0.51	-0.45 -0.03	-0.28 -0.72	-0.47 -0.68	-0.44 -0.67	-0.68 -0.68	-0.38 -0.38	-0.46 -0.58	-0.65 -0.66	-0.95 -0.52
Liaoning	-0.02	0.26	-0.72	-0.03	-0.37	0.12	-0.38	-0.38	-0.00	-0.32
Jilin	-0.79	0.10	-0.70	-0.60	-0.58	-0.47	-0.24	-0.64	-0.45	0.52
Heilongjiang	-0.37	-0.41	-0.51	-0.54	-0.50	-0.63	-0.36	-0.54	-0.61	0.10
Shanghai	-0.75	1.87	-0.49	1.00	0.67	1.30	-0.16	-0.26	0.96	-0.56
Jiangsu	2.69	0.44	2.24	0.69	0.34	2.20	3.57	1.75	2.61	3.29
Zhejiang	1.98	1.53	1.53	1.21	0.75	1.24	0.09	1.36	0.94	0.82
Anhui	0.65	-1.19	0.23	-0.36	-0.27	-0.58	-0.32	0.01	-0.54	0.56
Fujian	0.10	0.52	0.30	0.79	3.10	0.26	-0.01	0.04	0.26	0.83
Jiangxi	0.07 1.09	-1.22 -0.34	-0.12 1.73	-0.54 0.81	-0.43 0.32	-0.64 0.69	-0.38 1.02	-0.33 0.94	-0.62 1.04	-0.27 0.75
Shandong Henan	0.72	-0.34 -0.81	1.73	0.81	0.32	-0.54	-0.36	0.94 0.96	-0.54	0.75
Hubei	0.72	-0.81	0.20	-0.17	-0.04	-0.34	-0.30	0.90	-0.34	-0.43
Hunan	0.64	-1.06	0.20	-0.33	-0.04	-0.54	-0.27	0.16	-0.50	0.86
Guangdong	1.50	1.56	2.50	3.29	2.39	2.63	3.65	3.81	2.87	2.32
Guangxi	-0.14	-0.90	-0.16	-0.51	-0.41	-0.63	-0.38	-0.15	-0.63	0.03
Hainan	-1.22	0.27	-1.05	-0.65	-0.56	-0.62	-0.38	-0.97	-0.62	-0.84
Chongqing	-0.32	0.13	-0.31	-0.48	-0.45	-0.16	-0.15	-0.39	-0.22	-0.83
Sichuan	1.52	-0.20	1.19	0.39	0.10	0.44	-0.26	0.67	0.38	0.60
Guizhou	-0.35	-0.59	-0.65	-0.67	-0.58	-0.61	-0.38	-0.13	-0.61	-0.90
Yunnan	-0.03	-0.91	-0.37	-0.63	-0.55	-0.65	-0.38	0.19	-0.64	-0.45
Tibet	-1.30	-0.65	-1.24	-0.76	-0.73	-0.69	-0.38	-1.25	-0.67	-1.46
Shanxi	-0.17	0.24	-0.24	-0.42	-0.46	0.03	-0.20	-0.01	-0.07	0.08
Gansu	-0.61	-0.52	-0.69	-0.70	-0.63	-0.66	-0.38	-0.63	-0.65	-0.95
Qinghai Ningxia	-1.23 -1.27	-0.02 0.15	-1.17 -1.13	-0.75 -0.73	-0.72 -0.71	-0.69 -0.68	-0.38 -0.38	-1.09 -1.05	-0.66 -0.66	-0.92 -1.05
Xinjiang	-0.25	-0.16	-0.66	-0.73	-0.71	-0.65	-0.38	-0.75	-0.64	-0.48
			STA	TABLE II-(ANDARDIZED						
Provinces (cities)	<i>X</i> ₁₁	<i>X</i> ₁₂	X ₁₃	X_{14}	X ₁₅	X_{16}	X ₁₇	X_{18}	X_{19}	X_{20}
Beijing	-1.45	-0.30	2.89	0.03	0.50	2.30	-0.48	-1.13	-0.22	-0.48
Tianjin	-1.45	-0.04	-0.62	-0.46	-0.49	-0.16	-0.88	-0.95	-0.66	0.55
Hebei	0.66	-0.17	-0.78	-0.04	0.67	-0.27	-0.64	0.38	0.16	0.71
Shanxi	0.40	-0.55	-0.91	-0.59	-0.62	-0.52	-0.52	0.09	-0.62	-0.50
Inner Mongolia	0.57 -0.07	-0.59 -0.30	-1.01 -1.43	-0.72 -0.15	-0.46 -0.03	-0.42 -0.24	0.54 -0.37	0.08 0.41	-0.81 0.19	-0.37 -0.33
Liaoning Jilin	-0.07	-0.59	-1.43	-0.13	-0.03	-0.24	-0.37	-0.77	-0.34	-0.33
Heilongjiang	-0.41	-0.53	-1.56	-0.70	-0.33	-0.65	-0.23	-0.23	-0.10	0.06
Shanghai	-1.45	-0.06	0.69	0.07	0.05	2.14	-0.71	-0.78	-0.25	-0.61
Jiangsu	-1.45	2.75	-0.07	2.52	2.46	0.67	1.18	0.92	2.14	2.37
Zhejiang	-1.45	2.85	1.14	1.88	1.56	0.39	0.93	1.43	1.75	-0.24
Anhui	-0.33	0.21	0.79	0.29	0.21	-0.09	0.63	0.60	-0.18	0.58
Fujian	-0.24	0.10	0.45	0.44	0.13	-0.30	-0.86	0.04	0.15	-0.34
Jiangxi	0.10	-0.27	-0.46	-0.25	-0.53	-0.35	1.78	0.19	-0.13	-0.22
Shandong	-0.50	1.46	0.04	1.82	1.99	1.52	0.77	1.55	2.23	4.04
Henan	-0.03	0.08	-1.04	0.89	0.01	0.00	0.12	0.99	0.22	0.33
Hubei	-0.20	-0.08	-0.02	0.27	0.54	-0.14	0.26	0.22	0.83	0.00
Hunan	0.66	-0.15	0.00	0.14	-0.53	-0.26	-0.95	0.15	0.78	0.92
Guangdong Guangxi	-0.76 0.57	2.58 -0.56	0.33 -0.10	2.71 -0.52	2.91 -0.58	3.42 -0.54	0.78 0.84	2.69 -0.03	2.22 -0.23	0.30 -0.18
Hainan	-1.05	-0.56 -0.68	-0.10	-0.52 -0.98	-0.58 -1.06	-0.54 -0.64	-0.83	-0.03	-0.23	-0.18 -0.71
Chongqing	0.01	-0.19	0.31	-0.28	-0.22	-0.18	-0.58	-0.57	-0.51	-0.71
Sichuan	2.12	-0.16	0.71	0.23	-0.05	-0.17	3.67	1.53	0.89	-0.30
Guizhou	1.56	-0.58	0.23	-0.56	-0.68	-0.50	-0.03	-0.46	-0.22	-0.68
Yunnan	2.03	-0.50	0.45	-0.54	-0.73	-0.46	-0.09	0.40	-0.51	-0.73
Tibet	-0.29	-0.71	1.22	-1.06	-1.06	-0.74	-1.00	-1.61	-1.33	-0.81
Shanxi	1.60	-0.46	0.32	-0.38	-0.15	-0.51	-0.06	-0.14	0.00	0.14
Gansu	1.13	-0.62	-0.45	-0.79	-0.50	-0.62	-0.40	-0.49	-1.02	-0.56
Qinghai	-0.20	-0.69	-0.11	-1.01	-0.89	-0.68	-0.85	-1.43	-1.24	-0.74
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Ningxia Xinjiang	-0.24 0.53	-0.63 -0.65	-0.04 -1.27	-0.96 -0.73	-0.29 -0.89	-0.71 -0.62	-0.84 -0.68	-1.31 -0.15	-1.19 -0.90	-0.75 -0.59

	CLUSTERING RESUL	TABLE III ts of The Overall Develo	OPMENT OF DIGITAL ECO	ONOMY	
Methods	Cluster1	Cluster2	Cluster3	Cluster4	Cluster5
Longest distance	Guangdong	Jiangsu, Zhejiang Shandong	Beijing, Shanghai	Sichuan	others
Class average	Guangdong	Jiangsu, Zhejiang, Shandong	Beijing, Shanghai	Sichuan	others
Barycenter	Beijing	others	Guangdong	Zhejiang	Jiangsu, Shandong
Sum of deviation squares	Zhejiang, Shandong, Guangdong	Hainan, Tibet, Qinghai, Ningxia	others	Beijing, Shanghai	Hebei, Anhui, Fujian, Henan Hubei, Hunan, Sichuan
K-means	Tianjin, Hainan, Tibet, Qinghai, Ningxia	Jiangsu, Zhejiang, Shandong, <mark>Guangdong</mark>	Beijing, Shanghai	Hebei, Anhui, Fujian, Henan, Hubei, Hunan, Sichuan	others
			1	1 7 1 1	[10] 1.1 ·

Above the indicator system established in Section II, combined with the data published on the websites of the National Bureau of Statistics, the Ministry of Commerce and the provincial people's governments, the existing data of 31 provinces and cities from 2015 to 2018 are averaged. On this basis, all the data are standardized, and the final data are as shown in Tables II-A and II-B.

B. Clustering results

According to the standardized data, under the indicator system of digital economy established in Table I, the data of 31 provinces and cities are clustered by four clustering methods (the longest distance method, the class average method, the center of gravity method, the sums of deviation squares) and K-means clustering method, and are divided into five categories. On this basis, this paper studies the categories of the holistic digital economic development in Guangdong. The pedigree map can be obtained by cluster analysis in R software.

According to the pedigree map, the distribution of 31 provinces and cities under each category is summarized, as shown in Table III.

Similarly, the clustering results about the 4 kinds of digital economy are shown in Appendix respectively.

V.RESULT ANALYSIS

A. Analysis

It is impossible to judge the advantages and disadvantages of the clustering results of the digital economic population and the 4 types of digital economy. Hence, the factor analysis is carried out on the digital economic population and the four digital economic types respectively. In the result of factor analysis, *k* public factor with cumulative contribution rate is greater than 80%. Based on each digital economy type which are as indicators, the corresponding score coefficient matrix $Q = (q_{ij})_{m \times k}$ are selected. If *m* indicators are X_1, X_2, L, X_m , according to the score coefficient matrix and variance contribution rate, the score of each common factor can be calculated as well as the

comprehensive factor score by Lei et al. [18], and their expressions are shown in Formulae (13) and (14).

$$F_j = \sum_{i=1}^m q_{ij} X_i \tag{13}$$

$$F = F_j \times a_j \tag{14}$$

Where a_j is the proportion of the variance contribution rate of the *j*-th common factor in total variance contribution rate.

 TABLE IV

 Score Table of Digital Economy of Provinces and Cities

Provinces (cities)	Overall	Basic	Tech	Integrated	Service oriented
Beijing	-0.19	2.01	-1.10	0.45	-0.57
Tianjin	-0.47	-0.43	-0.53	-0.07	-0.74
Hebei	0.20	-0.03	0.39	-0.04	-0.16
Shanxi	-0.37	-0.37	-0.50	-0.54	-0.25
Inner Mongolia	-0.37	-0.46	-0.35	-0.57	0.15
Liaoning	-0.07	-0.07	-0.54	-0.20	0.01
Jilin	-0.38	-0.40	0.09	-0.45	-0.33
Heilongjiang	-0.31	-0.43	-0.04	-0.54	-0.27
Shanghai	-0.25	0.73	-0.95	0.29	-0.56
Jiangsu	1.94	0.80	2.58	2.05	0.93
Zhejiang	1.10	1.15	0.52	1.79	1.03
Anhui	0.20	-0.35	0.41	0.27	0.37
Fujian	0.10	1.10	0.30	0.22	-0.30
Jiangxi	-0.05	-0.53	-0.13	-0.30	0.78
Shandong	1.37	0.48	0.77	1.33	0.85
Henan	0.41	0.14	0.65	0.17	0.34
Hubei	0.13	-0.20	-0.24	0.20	0.29
Hunan	0.15	-0.26	0.62	-0.22	-0.27
Guangdong	2.09	2.14	2.87	2.09	1.28
Guangxi	-0.17	-0.46	0.09	-0.48	0.33
Hainan	-0.90	-0.44	-0.69	-0.37	-0.90
Chongqing	-0.37	-0.25	-0.54	-0.15	-0.43
Sichuan	0.69	0.32	0.31	-0.25	2.07
Guizhou	-0.40	-0.54	-0.36	-0.64	-0.12
Yunnan	-0.26	-0.54	0.01	-0.68	0.04
Tibet	-0.98	-0.75	-1.09	-0.55	-0.99
Shanxi	-0.13	-0.20	-0.03	-0.44	-0.06
Gansu	-0.54	-0.57	-0.58	-0.65	-0.41
Qinghai	-0.86	-0.58	-0.76	-0.60	-0.87
Ningxia	-0.82	-0.54	-0.81	-0.42	-0.83
Xinjiang	-0.49	-0.47	-0.41	-0.70	-0.41



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Fig. 1. Score of digital economy of provinces and cities

According to Formulas (13) and (14), we can calculate the comprehensive factor scores of 31 provinces and cities under the overall digital economy and the four major types of digital economy. The results are shown in Table IV.

With comparing the data in Table IV, the clustering results match the comprehensive factor scores obtained by factor analysis based on the works of MacCallum et al. [19]. Provinces (cities) with higher scores can often form a category. In addition, those with lower scores or close scores can also be divided into one category.

Thus, the results of clustering and factor score well confirm the growth of digital economy in various regions.

- B. Results and Advice
- From the view of the overall digital economic development, Guangdong's digital economy is divided into a group with Jiangsu, Zhejiang and Shandong under the method of sum of squares of deviation and K-means clustering, but it is divided into a separate category under the method of longest distance, class average and gravity center. Then, the comprehensive factor score is also the highest. It illustrates that although other digital economy provinces are developing better, the fact still be not able to shake the leading position of Guangdong as the largest digital economy province.
- 2) From the analysis of the results of basic digital economic clustering, although Guangdong is in the first place in most clustering methods, Beijing can also become a separate category under the longest distance method, class average method and barycenter method. The difference of comprehensive factor score between

Beijing and Guangdong is only 0.13, indicating that the gap between Beijing and Guangdong in the development of basic digital economy has not been widened.

- 3) From the aspect of technology-based digital economy, Jiangsu and Guangdong are in the same category under K-means clustering and two kinds of systematic clustering, and the scores of comprehensive factors are also very close, indicating that the scale of technological digital economy is not the unique one in Guangdong, and Jiangsu is likely to catch up with or even surpass Guangdong in the future.
- 4) According to the clustering results of the integrated digital economy, except for the gravity method, Guangdong and other provinces can be grouped into the same category, and the factor comprehensive score difference is not big, especially in Jiangsu, the score difference is only 0.04. It is thus clear that the integration of digital economy, primary industry and secondary industry in Guangdong Province should be strengthened.
- 5) Based on the clustering results about the service-oriented digital economy, Guangdong is a separate category under the three clustering methods, but the results of comprehensive factor score show that there is a big difference of 0.79 between Guangdong and Sichuan. In addition, the clustering results obtained by K-means and sum of squares of deviation show that Guangdong and Sichuan do not form a category, showing that the application degree of digital economy in service industry in Guangdong is quite different from that in Sichuan.

APPENDIX

The as seen in Fig. 1, we easily draw a clear conclusion that Guangdong is the industry leader of digital economy, and has great potential in service-oriented.

Therefore, it is necessary to strengthen the construction of service-oriented digital economy. Making use of the achievements of digital economy rapid development to benefit the public should become the next goal of Guangdong. technology should not only play a role in some important fields, but also be close to life and bring convenience to people's lives. When the digital products are universal and popular, people can enjoy the benefits brought by the development of information technology.

Consequently, the development of service-oriented digital economy can go up to a higher level.

The	results	obtained	from	the	development	of	digital
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		Appen	NDIX		
	C	LUSTERING RESULTS OF E	BASIC DIGITAL ECONOMY		
Methods	Cluster1	Cluster2	Cluster3	Cluster4	Cluster5
Longest distance method	Guangdong	Beijing	Shanghai, Fujian	others	Hebei, Jiangsu Zhejiang, Shandong Henan, Sichuan
Class average method	others	Hebei, Jiangsu Zhejiang, Shandong Henan, Sichuan	Guangdong	Beijing	Shanghai, Fujian
Barycenter method	Fujian	Jiangsu, Zhejiang	Beijing	others	Guangdong
Method of sum of deviation squares	Beijing, Shanghai Fujian	Jiangsu, Zhejiang Guangdong	others	Hebei, Shandong Henan, Sichuan	Anhui, Jiangxi Hubei, Hunan Guangxi, Yunnan
K-means clustering	others	Hebei, Shanxi Liaoning, Anhui Jiangxi, Henan Hunan, Guangxi Hubei, Shanxi	Jiangsu, Zhejiang Shandong, Sichuan	Guangdong	Beijing, Shanghai Fujian
	CLUST	ERING RESULTS OF TECHN	OLOGICAL DIGITAL ECONO	MY	
Methods	Cluster1	Cluster2	Cluster3	Cluster4	Cluster5
Longest distance method	Jiangsu, Guangdong	Zhejiang, Shandong	Beijing, Shanghai	Hebei, Jilin Anhui, Fujian Henan, Hunan Sichuan	others
Class average method	Jiangsu	Guangdong	Beijing	others	Shanghai, Zhejiang Fujian, Shandong Sichuan
Barycenter method	Jiangsu	Guangdong	Beijing	Shanghai	
Method of sum of deviation squares	Shanxi, Hainan Guizhou, Tibet Gansu, Qinghai Ningxia, Xinjiang Inner Mongolia	others	Jiangsu, Guangdong	Beijing, Shanghai	Zhejiang, Fujian Shandong, Sichuan
K-means clustering	others	Beijing, Shanghai	Jiangsu, Guangdong	Hebei, Jilin Anhui, Henan Jiangxi, Hubei Hunan, Guangxi Yunnan, Shanxi Heilongjiang	Sichuan, Fujian Shandong
	CLUS	TERING RESULTS OF INTE	GRATED DIGITAL ECONOM	Y	
Methods	Cluster1	Cluster2	Cluster3	Cluster4	Cluster5
Longest distance method	Jiangsu, Zhejiang Shandong, Guangdong	Beijing, Hainan Tibet	Sichuan, Guizhou Yunnan, Shanxi	Shanghai, Anhui Fujian, Hubei	others
Class average method	Jiangsu, Zhejiang Shandong, Guangdong	Sichuan, Guizhou Yunnan, Shanxi	others	Beijing	Hainan, Tibet
Barycenter method	Zhejiang	Jiangsu, Shandong Guangdong	Beijing	Hainan, Tibet	others
Method of sum of deviation squares	Jiangsu, Zhejiang Shandong, <mark>Guangdong</mark>	Tianjin, Shanghai Anhui, Fujian Hubei	Beijing, Hainan Tibet	Sichuan, Guizhou Yunnan, Shanxi	others
K-means clustering	Beijing, Shanghai Hainan, Tibet	Sichuan, Yunnan Shanxi, Gansu Guizhou	Zhejiang, Shandong Guangdong, Jiangsu	others	Hebei, Anhui Fujian, Henan Hunan, Hubei Chongqing

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Methods	Cluster1	Cluster2	Cluster3	Cluster4	Cluster5
Longest distance method	Hebei, Liaoning Zhejiang, Anhui Fujian, Jiangxi Henan, Hubei Hunan, Guangxi Inner Mongolia	others	Sichuan	Guangdong	Jiangsu, Shandong
Class average method	Zhejiang, Sichuan	Beijing, Shanghai	others	Guangdong	Jiangsu, Shandong
Barycenter method	Guangdong	Sichuan	Jiangsu, Shandong	Zhejiang	others
Method of sum of deviation squares	others	Hainan, Tibet Qinghai, Ningxia	Beijing, Shanghai	Hainan, Tibet Qinghai, Ningxia	Jiangsu, Shandong Guangdong
K-means clustering	Tianjin, Jilin Chongqing, Tibet Gansu, Ningxia Hainan, Qinghai Ningxia, Xinjiang	Zhejiang, Sichuan Jiangxi	others	Jiangsu, Shandong Guangdong	Beijing, Shanghai

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