

A Framework for UML Class Diagrams and Software Patterns Integration

Wararat Rungworawut

Abstract— In software engineering, a software pattern is a reusable solution to solve recurring software design problems. Traditionally, suitable patterns are identified by software designers to satisfy a set of requirements. A part of appropriate patterns is then applied to a recurring software design problem. However, the existing software patterns part has to be properly integrated to specific design problems. Therefore, the introduction of formalization is required to describe this integration accurately. In this paper, we propose a framework of UML class diagrams and software patterns integration prepared for formal specification to solve different software designer's experiences. The integration rules in this formal framework is intended to complement existing textual and graphical descriptions in order to eliminate the ambiguity of class diagrams with software patterns integration. A case study of our approach is illustrated in a purchase order system.

Index Terms— software patterns, UML class diagrams, software design, formal specification.

I. INTRODUCTION

The conventional software development starts with application domains modeling with software models such as UML models [1]. UML class diagrams are a widely used technique for modeling the static structure of a software model which is created by software designers. Therefore, software designers need to fully understand the problem domain in order to design such software models. Whereas, a part of solving design problem in software application is collected as software patterns those can be applied during software modeling. There are several kinds of patterns that can be applied to software models. In this paper, the focus is on archetype patterns which are used to describe possible software models. The archetype patterns are always at a higher level of abstraction than normal analysis class that can be adapted to specific business domains [2]. Many researches show reused patterns have been promoted. For example, [3] focused on the use of patterns for business processes and also the derivation of UML classes from the process patterns manually. [4], [5] tried to select patterns in different patterns to software models by expert systems such as ontology. As an aspect of formal specification of class diagrams and state diagrams in simple notation are based on

basic mathematics and predication logic has been proposed in [6]. Similarity to the approach in [7], a class diagram representation and software patterns have been defined with a suggestion of using a rule-based method to match design patterns into a UML model. However, these researches have not discussed how to apply software patterns to UML class diagrams in a formal specification accurately. The difference of our approach is trying to fabricate precise integration rules between UML class diagrams and software patterns in a form of a formal specification.

In this paper, we present an overview of a framework for the integration of software patterns applying to specific design problem as UML class diagrams. The main objective is to create the integration rules based on the basic mathematics and the predicate logic in order to eliminate ambiguity and allow rigorous reasoning about the integration of class diagrams with software patterns. These rules are easily used as criterion to apply in the information such as attributes, methods and associations, which are extracted between UML class diagrams and software patterns. Our framework will help software designers to construct a software model as UML class diagrams by adding these details to classes using software patterns.

The overview of framework for UML class diagrams and software patterns integration is proposed in Section II. The definition of UML class diagrams and software pattern is given in Section III. And Section IV is the description of integration rules. Section V shows the case study followed by integration rules used in this case and also the discussion about the case study. Last but not least, our future works are concluded in Section VI.

II. OVERVIEW OF FRAMEWORK

The overview of framework, software designers have knowledge in design software to create classes in a class diagram (D) for a particular design problem. These classes in a class diagram may be satisfied with a set of requirement but they may be not sufficient to derive the possible class diagram. However, software designers need to query existing solution of experts during a design decision such as looking for software patterns. A software pattern has a name corresponding to the document solution as problem domain name that is unique within a pattern catalog. Therefore, those software patterns are selected by searching problem domain names. The problem domain name is a meaningful name that will be a part of the shared design vocabulary [8]. Mostly software pattern description formats also contain an implicit or explicit related software patterns section [9], [10]. For

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W. Rungworawut is with the Information Systems Engineering Laboratory, Department of Computer Engineering, Chulalongkorn University, Bangkok 10330 Thailand (phone: +66 2 2186991; fax: +66 2 2186955; e-mail: wararatku@yahoo.com).

example, prototyping a class diagram (D) has labeled a problem domain name. The problem domain name is queried in software pattern catalogs that collected various software patterns. Software patterns are related to class diagram (D), which exactas software pattern P1 and P2. The class diagram (D) and those software patterns P1 and P2 are appropriate integrated by criteria selection from integration rules. These integration rules apply to a single new class diagram (D_{new}) in Fig. 1.

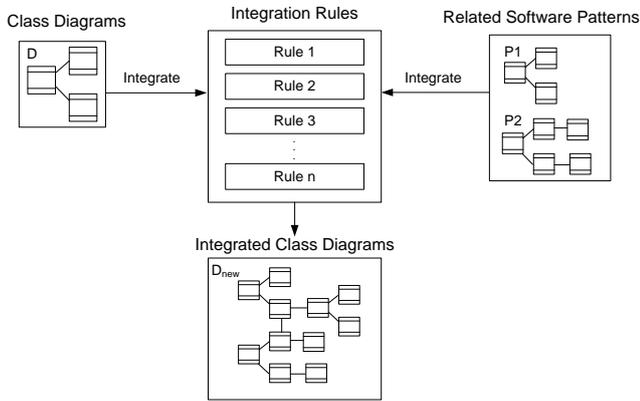


Fig. 1 Overview of UML class diagram and software pattern integration framework.

III. FORMAL SPECIFICATION OF INTEGRATION RULES

A. Class Diagram

A Class diagram relations are modeled by mean of labeled relationship between classes. Hence, D represents the set of a class diagram.

$$D = (C, R)$$

Class (C) is a set of classes and CN represents the infinite set of class names.

$$C = \{c_i (cn, A, M) \mid i \in \mathbb{N}, cn \in CN\}$$

Thus, a class c_i is a tuple $c_i = (cn, A, M)$ where, cn name of c_i .

A a finite set of attribute of c_i .

M a finite set of operations of c_i .

Each of the item x in the tuple c_i is denoted $c_i.x$. For example, $c_i.cn$ denotes the name of c_i or $c_i.A$ denotes the set of attributes A of c_i , etc.

Let us consider two infinite sets of AN and MN, which respectively represent the set of attribute name and method name. Given a set of basic types B includes integer, string, float, double, etc.

A is a set of attributes. An attribute a_i consists of a method name an , where $an \in AN$ and a attribute type is a basic type bi .

$$A = \{a_i(an, bi) \mid i \in \mathbb{N}, an \in AN, bi \in B \cup CN\}$$

Each of the item x in the tuple a_i is denoted $a_i.x$. For example, $a_i.an$ denotes the name of a_i .

M is a set of methods. We denote a method signature by notation $ms_1, \dots, ms_n \rightarrow ms$, where $ms_1, \dots, ms_n, ms \in B \cup CN$. A method $mi: ms_1, \dots, ms_n \rightarrow ms$ consists of a method name m , where $m \in MN$ and a method signature $ms_1, \dots, ms_n \rightarrow ms$.

$$M = \{m_i: ms_1, \dots, ms_n \rightarrow ms \mid i \in \mathbb{N}, m_i \in MN, ms \in B \cup CN\}$$

Relations (R) Let R is a set of relationship between classes.

$$R = \{r_i (c_i, c_j, S) \mid i, j \in \mathbb{N}\}$$

Thus, a relation r_i is a tuple $r_i = (c_i, c_j, S)$, where c_i, c_j are two classes, and $S = \{s\}$ is a set of description of the relationship between c_i and c_j . The description of an association $s = (t, L, g)$ where t is enumeration of types includes association, inheritance, aggregation, composition etc. L is a set of labels and g is a directional flag which is either unidirectional, represent by $c_i \rightarrow c_j$, or bidirectional represented by $c_i \leftrightarrow c_j$ as follows,

String information users

Role a pair (r_1, r_2) also information users

Multiplicity a pair (v_1, v_2) by v_i is of the form $l_i..u_i$ where $l_i, u_i \geq 0$ such as $0..2, 1..*, 0..*$ etc.

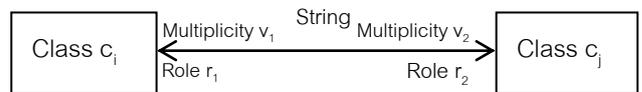


Fig. 2 A pair of relations of class diagram.

The definition of all classes and relationships can be illustrated by an example with consideration the UML class diagram shown in Fig. 3.

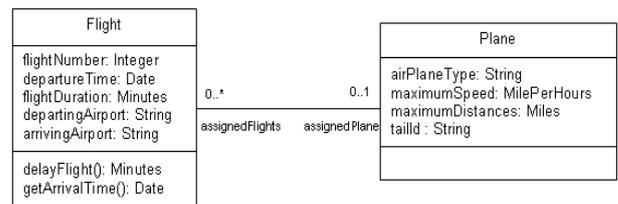


Fig. 3 Example of a part of class diagram (D).

As Fig. 3, set of flight class diagram is represented by

$$D_{\text{Flight}} = (C, R), \text{ by set of classes } C \text{ is}$$

$$C = \{c_1(\text{Flight}, A_{\text{Flight}}, M_{\text{Flight}}), c_2(\text{Plane}, A_{\text{Plane}}, M_{\text{plane}})\}$$

$$A_{\text{Flight}} = \{ a_1(\text{flightNumber}, \text{Integer}), a_2(\text{departureTime}, \text{Date}), a_3(\text{flightDuration}, \text{Minutes}), a_4(\text{departingAirport}, \text{String}), a_5(\text{arrivingAirport}, \text{String}) \}$$

$M_{Flight} = \{ m_1:delayFlight() \rightarrow Minutes,$
 $m_2:getArrivalTime() \rightarrow Date \}$

$A_{Plane} = \{ a_1(airPlaneType, String),$
 $a_2(maximumSpeed, MilePerHours),$
 $a_3(maximumDistance, Miles),$
 $a_4(tailId, String) \}$

$M_{plane} = \emptyset$

$R = \{ r_1(c_1, c_2, S) \}$
 $S = (association, L, c_1 \leftrightarrow c_2)$
 $L = (null, (assignedFlights, assignedPlane), (0..*, 0..1))$

B. Software Patterns

Software patterns are class diagram patterns which consist of classes and relations between classes in a class diagram pattern. Hence, P represents the set of class diagram patterns.

$P = (CP, RP)$

Class Patterns (CP) is a set of classes in a class diagram pattern and CPN represents the infinite set of class pattern names.

$CP = \{ cp_i (cpn, AP, MP) \mid i \in \mathbb{N}, cpn \in CPN \}$

Thus, a class cp_i is a tuple $cp_i = (cpn, AP, MP)$

where,

cpn name of cp_i .

AP a finite set of attribute of cp_i .

MP a finite set of operations of cp_i .

Therefore, let us consider two infinite sets of ANP and MNP, which respectively represent the set of attribute name and method name. To similar, given a set of basic types B in class diagram (including integer, string, float, double, etc).

AP is a set of attributes in a class pattern cp_i . An attribute ap_i consists of a method name anp , where $anp \in ANP$ and a attribute type is a basic type bi .

$AP = \{ ap_i(anp, bi) \mid i \in \mathbb{N}, anp \in ANP, bi \in B \cup CNP \}$

MP is a set of methods in a class pattern cp_i . We denote a method signature in a class pattern by notation $msp_1, \dots, msp_n \rightarrow msp$, where $msp_1, \dots, msp_n, msp \in B \cup CNP$ where $mp \in MN$ and a method signature $ms_1, \dots, ms_n \rightarrow ms$.

$MP = \{ mp_i: msp_1, \dots, msp_n \rightarrow msp \mid i \in \mathbb{N}, mp_i \in MNP,$
 $msp \in B \cup CNP \}$

Relations (RP) Let RP is a set of relationship between classes in a class diagram pattern.

$RP = \{ rp_i (cp_i, cp_j, SP) \mid i, j \in \mathbb{N} \}$

Thus, a relation rp_i is a tuple $rp_i = (cp_i, cp_j, SP)$, where cp_i, cp_j are two classes in a class diagram pattern, and $SP = \{ sp \}$ is a set of description of the relations hip between cp_i and cp_j . The description of an association $sp = (t, L, g)$ where t, L and g is similar to set s of class diagram (D).

IV. INTEGRATION RULES

The definitions of class diagram and software patterns are used for integration rules. This paper presents an example three of integration rules as follows,

A. Integration rule 1

Let c_i is a class in class diagram (D) and P1 is a software pattern that is related to domain in class diagram of c_i . Thus, c_i will be integrated to P1 and moved details (i.e. attributes, methods) in cp_i of P1 to original c_i followed definition of set in Rule 1.

Rule 1 If $c_i.c_n = cp_i.c_{pn}$ by $i \in \mathbb{N}, c_i \in D, cp_i \in P1$.

Then $c_i.A = c_i.A \cup cp_i.A$ and $c_i.M = c_i.M \cup cp_i.M$ by $i \in \mathbb{N}$.

Example of Rule 1

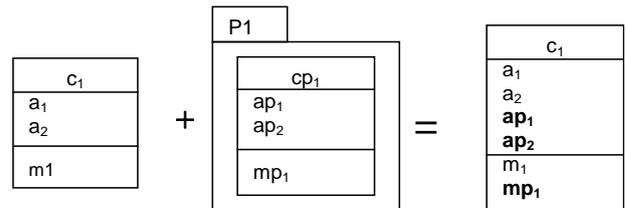


Fig. 4 Example of integration rule 1.

For example, a class c_i is relevant to cp_i in software pattern P1. Thus, the result in Fig. 4 shows new c_i that is added details in attributes and methods such as ap_1, ap_2 and mp_1 from cp_i respectively.

B. Integration rule 2

Let c_i is a class in class diagram (D) and P1 is a software pattern that is related to domain in class diagram of c_i . But multiple classes is related to a class cp_i in software pattern. Thus, c_i will be integrated all related to cp_i in P1 and moved details (i.e. attributes, methods) in all cp_i of P1 to original c_i followed definition of set in Rule 2.

Rule 2 If $c_i.c_n = cp_i.c_{pn}$ and $r_i.c_{pj} = (cp_i, cp_j, S)$ by $i, j \in \mathbb{N}, c_i \in D, cp_i \in P1$.

Then $c_i.A = c_i.A \cup cp_i.A$ and $c_i.M = c_i.M \cup cp_i.M$ and $r_i.c_i = r_i.c_i \cup rp_i.c_{pj}$, and $C = C \cup cp_j$

Example of Rule 2

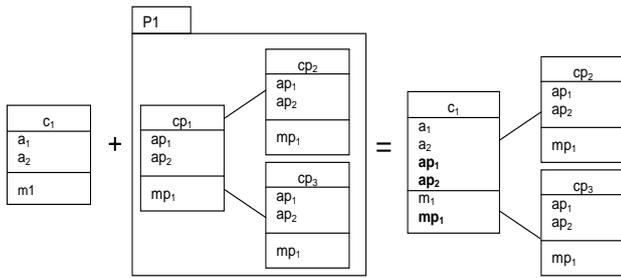


Fig. 5 Example of integration rule 2.

For example, a class c_i is relevant to cp_1 in software pattern P1 and cp_1 is related to cp_2 and cp_3 . Thus, the result in Fig. 5 shows new c_i that is added details in attributes and methods such as ap_1 , ap_2 and mp_1 from cp_1 . And new c_i has relation to cp_2 and cp_3 and their detailed of cp_2 and cp_3 .

C. Integration rule 3

Let c_i is a class in class diagram (D) and P1 is a software pattern that is related to domain in class diagram of c_i . But P1 needs required software pattern P2. In addition, multiple classes is related to a class cp_i in software pattern P1 and P2. Thus, c_i will be integrated all related to cp_i in P1 and P2, and moved details (i.e. attributes, methods) in all cp_i of P1 and cp_i of P2 to original c_i followed definition of set in Rule 3.

Rule 3 If $c_i.cn = cp_i.cpn$, $P1.cp_i.cpn = P2.cp_i.cpn$ by $P1.r_i.cp_i = (cp_i, cp_j, S)$ and $P2.r_i.cp_i = (cp_i, cp_j, S)$ by $i, j \in \mathbb{N}$.

Then $c_i.A = c_i.A \cup cp_i.A$ and $c_i.M = c_i.M \cup cp_i.M$ and $r_i.c_i = r_i.c_i \cup P1.rp_i.cp_i \cup P2.rp_i.cp_i$, and $C = C \cup P1.cp_j \cup P2.cp_j$.

Example of Rule 3

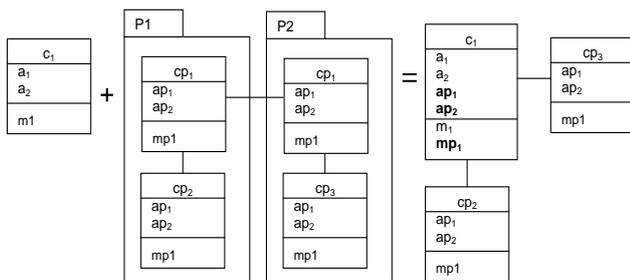


Fig. 6 Example of integration rule 3.

For example, a class c_i is relevant to cp_1 in software pattern P1 and P2. Class cp_1 of P1 is related to cp_2 and cp_1 of P2 is related to cp_3 . Thus, the result in Fig. 6 shows new c_i that is added details in attributes and methods such as ap_1 , ap_2 and mp_1 from cp_1 . And new c_i in P1 and P2 has relation to cp_2 and cp_3 respectively, so their detailed of cp_2 and cp_3 is also related to cp_1 .

V. CASE STUDY

An example of this case study is a vendor processing purchase orders of goods from its customers. Receiving a

purchase order, it will be checked that is enough goods in stock to complete the purchase order. If a sale order is opened, the tax is also calculated. But if not, the restock process is performed to reorder goods from a supplier before the purchase order is responded as an outstanding order. Thus, software designer may use their experience to create a UML class diagram as Fig. 7. and also look up software patterns related to purchase order problem domain. In this case, the software patterns that can be extracted from problem domain name is purchase order such as order archetype pattern [2] in Fig. 8 and restock policy pattern that is solved by domain expert based on the Economic Quantity Order model [11] which consider the quantity to order that minimizes the total variable costs required to order and hold inventory in Fig. 9.

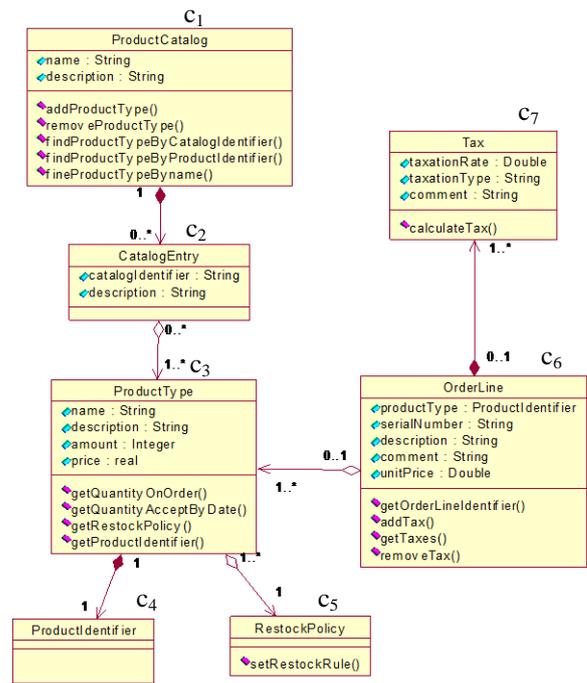


Fig. 7 An example of UML purchase order class diagram.

As Fig. 7, Purchase Order Class Diagram is presented as follows,

$$D_{PurchaseOrder} = (C, R), \text{ by set of classes } C \text{ is}$$

$$C = \{ c_1(\text{ProductCatalog}, A_{\text{ProductCatalog}}, M_{\text{ProductCatalog}}), c_2(\text{CatalogEntry}, A_{\text{CatalogEntry}}, M_{\text{CatalogEntry}}), c_3(\text{ProductType}, A_{\text{ProductType}}, M_{\text{ProductType}}), c_4(\text{ProductIdentifier}, \emptyset, \emptyset), c_5(\text{RestockPolicy}, A_{\text{RestockPolicy}}, M_{\text{RestockPolicy}}), c_6(\text{OrderLine}, A_{\text{OrderLine}}, M_{\text{OrderLine}}) \}$$

The set of Attributes in the class diagram can be represented by A of a class. For example, the class c_6 is *OrderLine* that has the set of attribute as follows,

$$A_{\text{OrderLine}} = \{ a_1(\text{productType}, \text{ProductIdentifier}), a_2(\text{serialNumber}, \text{String}), a_3(\text{description}, \text{String}), a_4(\text{comment}, \text{String}), a_5(\text{unitPrice}, \text{Double}). \}$$

$M_{OrderLine} = \{ m_1: getOrderLineIdentifier () \rightarrow null, \}$
 $m_2: addTax () \rightarrow null,$
 $m_3: getTax () \rightarrow null,$
 $m_4: removeTax () \rightarrow null. \}$

$mp_4: decreaseNumberOrdered () \rightarrow null,$
 $mp_5: addTax () \rightarrow null,$
 $mp_6: getTax () \rightarrow null,$
 $mp_7: removeTax () \rightarrow null. \}$

The relationship between classes in PurchaseOrder Class diagram is presented in R by,

The relationship between OrderLine class pattern and others class is presented by RP. For example,

$R = \{ r_1 (ProductCatalog, CatalogEntry, S1), \dots, r_5 (OrderLine, ProductType, S1), r_6 (OrderLine, Tax, S2) \}$

$RP_{OrderLine} = \{ rp_1 (OrderLine, Order, SP1), rp_2 (Order, PurchaseOrder, SP2), rp_3 (Order, SaleOrder, SP3) \}$

$S1 = (aggregation, L1, ProductCatalog \rightarrow CatalogEntry)$

$SP1 = (aggregation, LP1, OrderLine \leftarrow Order)$

$SP2 = (Inheritance, LP2, Order \leftarrow PurchaseOrder)$

$SP3 = (Inheritance, LP3, Order \leftarrow SalsOrder)$

...

$S5 = (aggregation, L5, OrderLine \rightarrow ProductType)$

$S6 = (composition, L6, OrderLine \rightarrow Tax)$

$LP1 = (null, (null, null), (0..*, 1))$

$LP2 = (null, (null, null), (null, null))$

$LP3 = (null, (null, null), (null, null))$

$L1 = (null, (null, null), (1, 0..*))$

...

$L5 = (null, (null, null), (0..1, 1..*))$

$L6 = (null, (null, null), (0..1, 1..*))$

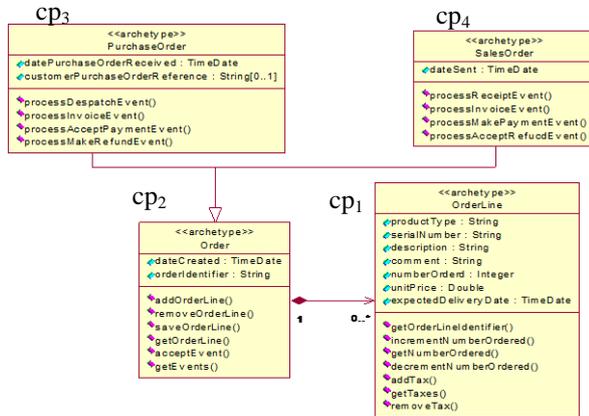


Fig. 8 Order archetype pattern.

As Fig. 8, Order Class Diagram pattern also is presented as follows,

$P_{Order} = (CP, RP)$, by set of classes CP is

$CP = \{ cp_1 (OrderLine, AP_{OrderLine}, MP_{OrderLine}), cp_2 (Order, AP_{Order}, MP_{Order}), cp_3 (PurchaseOrder, AP_{PurchaseOrder}, MP_{PurchaseOrder}), cp_4 (SaleOrder, AP_{SaleOrder}, MP_{SaleOrder}) \}$

Thus, the set of Attributes in the class diagram pattern can be represented by AP of a class pattern.

$AP_{OrderLine} = \{ ap_1 (productType, ProductIdentifier), \}$
 $ap_2 (serialNumber, String),$
 $ap_3 (description, String),$
 $ap_4 (comment, String),$
 $ap_5 (unitPrice, Double),$
 $ap_6 (expectedDeliveryDate, TimeDate) \}$

$MP_{OrderLine} = \{ mp_1: getOrderLineIdentifier () \rightarrow null, \}$
 $mp_2: increaseNumberOrdered () \rightarrow null,$
 $mp_3: getNumberOrdered () \rightarrow null,$

$A_{OrderLine} = \{ a_1 (productType, ProductIdentifier), \}$
 $a_2 (serialNumber, String),$
 $a_3 (description, String),$
 $a_4 (comment, String),$
 $a_5 (unitPrice, Double)$
 $ap_6 (expectedDeliveryDate, TimeDate). \}$

$M_{OrderLine} = \{ m_1: getOrderLineIdentifier () \rightarrow null, \}$
 $mp_2: increaseNumberOrdered () \rightarrow null,$
 $mp_3: getNumberOrdered () \rightarrow null,$
 $mp_4: decreaseNumberOrdered () \rightarrow null,$
 $m_5: addTax () \rightarrow null,$
 $m_6: getTax () \rightarrow null,$
 $m_7: removeTax () \rightarrow null. \}$

$D_{New_PurchaseOrder} = (C, R)$

$R = \{ r_1 (ProductCatalog, CatalogEntry, S1), \dots, r_5 (OrderLine, ProductType, S1), r_6 (OrderLine, Tax, S2), \mathbf{rp_1 (OrderLine, Order, SP1), rp_2 (Order, PurchaseOrder, SP2), rp_3 (Order, SaleOrder, SP3)} \}$

$C = \{ c_1 (ProductCatalog, A_{ProductCatalog}, M_{ProductCatalog}), \}$
 $c_2 (CatalogEntry, A_{CatalogEntry}, M_{CatalogEntry}), c_3 (ProductType, A_{ProductType}, M_{ProductType}), c_4 (ProductIdentifier, \emptyset, \emptyset), \}$
 $c_5 (RestockPolicy, A_{RestockPolicy}, M_{RestockPolicy}), c_6 (OrderLine, A_{OrderLine}, M_{OrderLine}), \mathbf{cp_2 (Order, AP_{Order}, MP_{Order}),}$

$cp_3(\text{PurchaseOrder}, AP_{\text{PurchaseOrder}}, MP_{\text{PurchaseOrder}}),$
 $cp_4(\text{SaleOrder}, AP_{\text{SaleOrder}}, MP_{\text{SaleOrder}})$

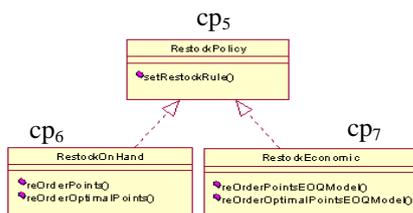


Fig. 9 Restock policy pattern.

In addition, restock policy pattern is integrated to purchase order class diagram, which also is based on Rule 2. The c_i of purchase order class diagram is *RestockPolicy* class that found in cp_1 of restock policy pattern. Therefore, the details (i.e. attributes, methods) of *RestockPolicy* classes, *RestockOnHand*, *RestockEconomic* classes which are moved to purchase order class diagram. The new purchase order class diagram is applied completely.

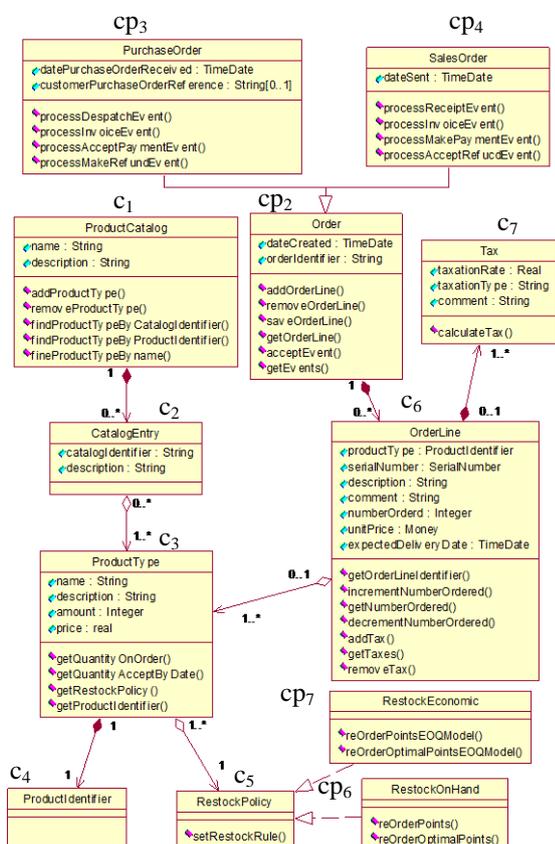


Fig. 10 Applied integration rules.

VI. CONCLUSION

We have presented a framework to enhance a class diagram with software patterns by integration rules. This framework helps software designer to identify classes for the class diagrams. Although, the traditional approach is done by their experience, the integration rules in formal specification are intended to complement existing textual and graphical descriptions in order to eliminate ambiguity and allow rigorous reasoning about integration fabrication between

UML class diagrams and software patterns. In addition, the integration rules can be mapped based on a formal specification language meant to specify them to achieve simplicity for a better understanding and accuracy for a precise semantics.

The case study shows results that are completed more details of class diagrams to fully satisfy with the requirements. We have tried to apply them to other case studies but more rules need to be added to achieve class diagram details. However, the detail of UML is a wide scope; we have not included other complex aspects of UML in this paper. It will be addressed in our future work.

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