

Rotorcraft Trajectory Tracking by Supervised NLI Control

A. Drouin, O. Lengerke, A.B. Ramos and F. Mora-Camino

Abstract— The purpose of this communication is to present a new nonlinear control structure for trajectory tracking taking explicitly into account actuators saturation. Here trajectory tracking by a four rotor aircraft is considered. After introducing the flight dynamics equations for the four rotor aircraft, a trajectory tracking control structure based on a two layer non linear inverse approach is adopted and a supervision layer is introduced to take into account the possible actuators saturation.

Index Terms— Rotorcraft, nonlinear inverse control, saturation supervision, trajectory tracking.

I. INTRODUCTION

In the last years a large interest has risen for the four rotor concept since it appears to present simultaneously hovering, orientation and trajectory tracking capabilities of interest in many practical applications [1].

The flight mechanics of four rotor aircraft are highly non linear and different control approaches (integral LQR techniques, integral sliding mode control [2]) have been considered with little success to achieve not only autonomous hovering and orientation, but also trajectory tracking. In this paper, some simplifying assumptions are adopted and the flight dynamics equations for a four rotor aircraft with fixed pitch blades, or rotorcraft, are considered.

One important limitation to perform automatic guidance for a rotorcraft is related with the one way effect of rotors and its saturation levels. Then the purpose of this study is to introduce a supervision layer in a non linear inverse control structure to improve maneuverability and trajectory tracking effectiveness by this class of rotorcraft. This approach has been already considered in the case of aircraft trajectory tracking by different authors [3,4, 5].

It appears that the flight dynamics of the considered rotorcraft present a two level input affine structure which is made apparent when a new set of equivalent inputs is defined. This allows the development of a non linear inverse control approach with two time scales, one devoted to attitude control and one devoted to orientation and trajectory tracking. However this is done in general without

considering actuators saturations and when these occur, trajectory tracking capability can be largely affected.

II. ROTORCRAFT FLIGHT DYNAMICS

The considered system is shown in figure 1 where rotors one and three are clockwise while rotors two and four are counter clockwise. In appendix the dynamics of the rotors are briefly characterized.

The main simplifying assumptions adopted with respect to flight dynamics in this study are a rigid cross structure, no wind, negligible aerodynamic contributions resulting from translational speed, no ground effect as well as negligible air density effects and very small rotor response times. It is then possible to write simplified rotorcraft flight equations [6].

The moment equations can be written as:

$$\left. \begin{aligned} \dot{p} &= (a/I_{xx})(F_4 - F_2) + k_2 q r \\ \dot{q} &= (a/I_{yy})(F_1 - F_3) + k_4 p r \\ \dot{r} &= (k/I_{zz})(F_2 - F_1 + F_4 - F_3) \end{aligned} \right\} \quad (1)$$

where p, q, r are the components of the body angular

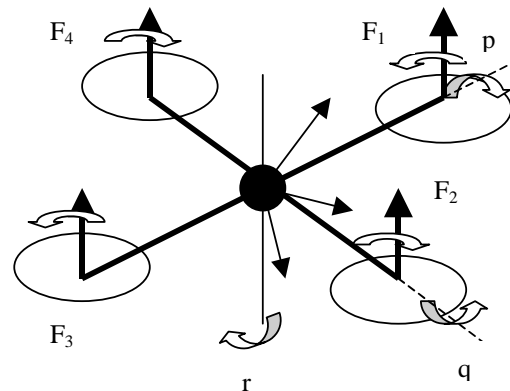


Fig 1. Four rotor aircraft

speed, with $k_2(I_{zz} - I_{yy})/I_{xx}$ and $k_4 = (I_{xx} - I_{zz})/I_{yy}$, I_{xx} , I_{yy} and I_{zz} being the moments of inertia in body-axis and m the total mass of the rotorcraft. The Euler equations are given by:

$$\left. \begin{aligned} \dot{\phi} &= p + \tan(\theta) \sin(\phi) q + \tan(\theta) \cos(\phi) r \\ \dot{\theta} &= \cos(\phi) q - \sin(\phi) r \\ \dot{\psi} &= ((\sin(\phi) / \cos(\theta)) q + (\cos(\phi) / \cos(\theta)) r) \end{aligned} \right\} \quad (2)$$

where θ, ϕ , and ψ are respectively the pitch, bank and heading angles.

A. Drouin is with MAIAA Laboratory, Automation Research Group at ENAC, Toulouse, France, antoine.drouin@enac.fr.

O. Lengerke is with Mechatronic and Robotic Laboratory, Universidad Autonoma de Bucaramanga-UNAB, Bucaramanga, Colombia, olengerke@unab.edu.co

A.B. Ramos is with Instituto de Ciências Exatas, UNIFEI, Itajubá, Brazil., ramos@unifei.edu.br

F. Mora-Camino is with MAIAA Laboratory, Automation Research Group at ENAC, Toulouse, France, Tel.+33562174358, fax. +33562174403, felix.mora@enac.fr

The acceleration equations written directly in the local Earth reference system are such as:

$$\left. \begin{aligned} \ddot{x} &= (1/m)(\cos(\psi) \sin(\theta) \cos(\phi) + \sin(\psi) \sin(\phi)) F \\ \ddot{y} &= (1/m)(\sin(\psi) \sin(\theta) \cos(\phi) - \cos(\psi) \sin(\phi)) F \\ \ddot{z} &= -g + (1/M) \cos(\theta) \cos(\phi) F \end{aligned} \right\} (3)$$

where x, y and z are the centre of gravity coordinates and where :

$$F = F_1 + F_2 + F_3 + F_4 \quad (4)$$

and with the constraints:

$$0 \leq F_i \leq F_{\max} \quad i \in \{1,2,3,4\} \quad (5)$$

III. NLI CONTROL APPROACH FOR TRAJECTORY TRACKING

Here we are interested in controlling the four rotor aircraft so that its centre of gravity follows a given path with a given heading ψ while attitude angles θ and ϕ remain small. Many potential applications require not only the centre of gravity of the device to follow a given trajectory but also the rotorcraft to present a given orientation.

A. Attitude Control

From equations (1) it appears that the effectiveness of the rotor actuators is much larger with respect to the roll and pitch axis than with respect to the yaw axis. Then it is considered here that attitude control is involved with controlling the θ and ϕ angles. In equations (1) the effect of rotor forces appears as differences so, we define new attitude inputs u_1 and u_2 as:

$$u_1 = F_1 - F_3 \quad u_2 = F_2 - F_4 \quad (6.1)$$

In the heading and position dynamics, the effects of rotor forces and moments appear as sums, so we define new guidance inputs v_1 and v_2 as:

$$v_1 = F_1 + F_3 \quad v_2 = F_2 + F_4 \quad (6.2)$$

It is supposed that u_1 and u_2 can be made to vary significantly while v_1 and v_2 can remain constant. Then the attitude dynamics can be rewritten under the affine input form:

$$\dot{\underline{X}} = f(\underline{X}, \underline{V}) + g(\underline{X}) \underline{U} \quad (7.1)$$

$$\underline{Y}' = (\theta, \phi) \quad (7.2)$$

with

$$\underline{X}' = (p, q, \theta, \phi), \quad \underline{U}' = (u_1, u_2) \quad \text{and} \quad \underline{V}' = (v_1, v_2) \quad (8)$$

Then, taking profit of non linear inverse control theory, it appears that all the attitude angles have relative degrees equal to one and that there is no internal dynamics while the output equations can be rewritten as:

$$\ddot{\underline{Y}} = M(\underline{Y}) \underline{U} + N(\underline{X}) \underline{V} + P(\underline{X}) \quad (9)$$

with

$$M(\underline{Y}) = \begin{bmatrix} a \cos \phi / I_{yy} & 0 \\ a \operatorname{tg} \theta \sin \phi / I_{yy} & -a / I_{xx} \end{bmatrix} \quad (10)$$

$$N(\underline{X}) = \begin{bmatrix} k \sin \phi / I_{zz} & -k \sin \phi / I \\ -k \operatorname{tg} \theta \cos \phi / I_{zz} & k \operatorname{tg} \theta \cos \phi / I_{zz} \end{bmatrix} \quad (11)$$

$$P(\underline{X}) = [P_1, P_2]'$$

where:

$$P_1 = k_4 \cos \phi p r - (q \sin \phi + r \cos \phi) (p + \operatorname{tg} \theta (q \sin \phi + r \operatorname{tg} \theta \cos \phi)) \quad (12.1)$$

$$P_2 = k_2 q r + k_4 p r \operatorname{tg} \theta \sin \phi + q d(\operatorname{tg} \theta \sin \phi) / dt + r d(\operatorname{tg} \theta \cos \phi) / dt \quad (2.2)$$

Then, while $\phi \neq \pm \pi / 2$, the attitude dynamics given by (9) are invertible. Then it appears opportune to adopt as a partial control objective to assign to the attitude angles second order linear dynamics towards their current reference values:

$$\begin{bmatrix} \ddot{\theta}_d \\ \ddot{\phi}_d \end{bmatrix} = \ddot{\underline{Y}}_d = \begin{bmatrix} -2\zeta_\theta \omega_\theta \dot{\theta} - \omega_\theta^2 (\theta - \theta_c) \\ -2\zeta_\phi \omega_\phi \dot{\phi} - \omega_\phi^2 (\phi - \phi_c) \end{bmatrix} \quad (13)$$

where $\zeta_\theta, \zeta_\phi, \omega_\theta, \omega_\phi$ are respectively damping and natural frequency parameters while θ_c and ϕ_c are reference values for the attitude angles. Then the resulting non linear inverse attitude control law is given by:

$$\underline{U} = -M(\underline{Y})^{-1} (N(\underline{X}) \underline{V} + P(\underline{X}) - \ddot{\underline{Y}}_d) \quad (14)$$

B. Guidance Control Law

Considering that the attitude dynamics are stable and much faster than the guidance dynamics, the guidance equations can be approximated by the control affine form:

$$\begin{bmatrix} \ddot{\psi} \\ \ddot{x} \\ \ddot{y} \\ \ddot{z} \end{bmatrix} = \begin{bmatrix} \frac{k \cos \phi_c}{I_{zz} \cos \theta_c} (v_2 - v_1) \\ (1/m)(\cos(\psi) \sin(\theta_c) \cos(\phi_c) + \sin(\psi) \sin(\phi_c)) (v_1 + v_2) \\ (1/m)(\sin(\psi) \sin(\theta_c) \cos(\phi_c) - \cos(\psi) \sin(\phi_c)) (v_1 + v_2) \\ -g + (1/m) \cos(\theta_c) \cos(\phi_c) (v_1 + v_2) \end{bmatrix} \quad (15)$$

Here also, the outputs of the guidance dynamics present relative degrees equal to 1 while the internal dynamics, which are concerned with the attitude angles are supposed already stabilized. Then, considering that second order linear dynamics are also of interest for the guidance variables, we can define desired accelerations by:

$$\begin{bmatrix} \ddot{\psi}_c \\ \ddot{x}_c \\ \ddot{y}_c \\ \ddot{z}_c \end{bmatrix} = \begin{bmatrix} -2\zeta_\psi \omega_\psi \dot{\psi} - \omega_\psi^2 (\psi - \psi_c) \\ -2\zeta_x \omega_x \dot{x} - \omega_x^2 (x - x_c) \\ -2\zeta_y \omega_y \dot{y} - \omega_y^2 (y - y_c) \\ -2\zeta_z \omega_z \dot{z} - \omega_z^2 (z - z_c) \end{bmatrix} \quad (16)$$

where $\zeta_\psi, \zeta_x, \zeta_y, \zeta_z, \omega_\psi, \omega_x, \omega_y, \omega_z$ are respectively damping and natural frequency parameters while ψ_c, x_c, y_c and z_c are reference values for the attitude angles. Of course, many other schemes can be proposed to define desired accelerations at the guidance level.

Once desired accelerations are made available, the inversion of the guidance dynamics brings nominal the solution:

$$v_1 = \frac{1}{2} (m\sqrt{\dot{x}_c^2 + \dot{y}_c^2 + (\ddot{z}_c + g)^2} - \frac{I_{zz} \cos \theta_c}{k \cos \phi_c} \ddot{\psi}_c) \quad (17.1)$$

$$v_2 = \frac{1}{2} (m\sqrt{\dot{x}_c^2 + \dot{y}_c^2 + (\ddot{z}_c + g)^2} + \frac{I_{zz} \cos \theta_c}{k \cos \phi_c} \ddot{\psi}_c) \quad (17.2)$$

with

$$\theta_c = \arctg((\ddot{x}_c \cos \psi + \ddot{y}_c \sin \psi) / (\ddot{z}_c + g)) \quad (18.1)$$

and

$$\phi_c = \arcsin\left(\frac{\ddot{x}_c \sin \psi - \ddot{y}_c \cos \psi}{\sqrt{\ddot{x}_c^2 + \ddot{y}_c^2 + (\ddot{z}_c + g)^2}}\right) \quad (18.2)$$

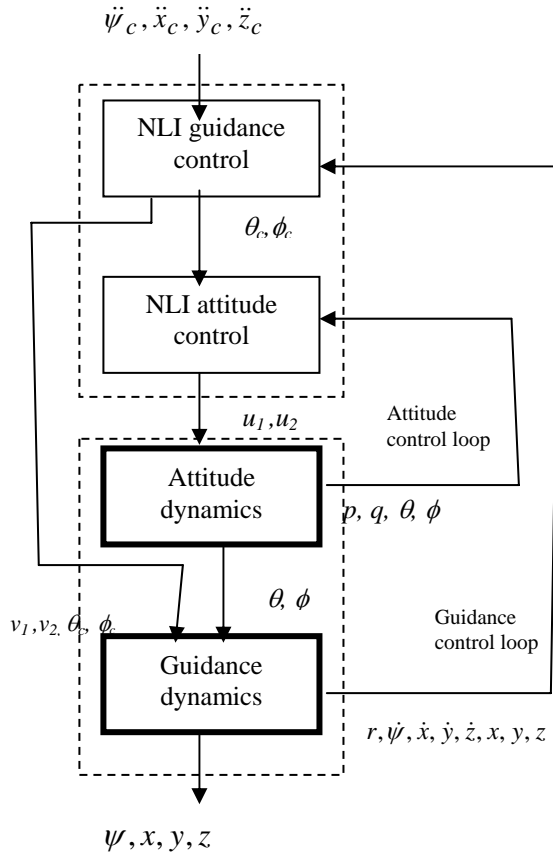


Fig 2. Proposed control structure

Then, returning to the expression of the attitude control law, it happens that the centre of gravity acceleration terms compensate each others and the law becomes simply:

$$\underline{U} = -M(\underline{Y})^{-1} (N(\underline{X}) + P(\underline{X}) - \ddot{\underline{Y}}_d) \quad (19)$$

with

$$N(\underline{X}) = \begin{bmatrix} N_1 \\ N_2 \end{bmatrix} = \begin{bmatrix} -\cos \theta_c & \sin \phi_c \\ \sin \theta_c & \cos \phi_c \end{bmatrix} \ddot{\psi}_c \quad (20)$$

The whole proposed control structure is given in the above figure 2.

IV. FLIGHT CONTROL SUPERVISION

Since the above control approach does not consider explicitly the input level constraints, we introduce here a supervision layer whose function is to avoid the generation

of unfeasible reference values for the inputs by modifying, as less as possible, the current control objectives. According to (5), (6) and (7), the control signals should be such as:

$$-F_{\max} \leq u_i \leq F_{\max} \quad i=1,2 \quad (21.1)$$

and

$$0 \leq v_i \leq 2 F_{\max} \quad i=1,2 \quad (21.2)$$

Conditions (21.1) implies for the desired attitude accelerations to satisfy the following conditions:

$$\ddot{\phi}_{\min} \leq \ddot{\phi}_c \leq \ddot{\phi}_{\max} \quad (22.1)$$

with

$$\ddot{\phi}_{\min} = N_2 + P_2 - \frac{a \cos \phi}{I_{yy}} F_{\max} \quad (22.2)$$

and

$$\ddot{\phi}_{\max} = N_2 + P_2 + \frac{a \cos \phi}{I_{yy}} F_{\max} \quad (22.3)$$

and condition:

$$\ddot{\theta}_{\min} \leq \ddot{\theta}_c - tg \theta \ddot{\phi}_c \leq \ddot{\theta}_{\max} \quad (23.1)$$

with

$$\ddot{\theta}_{\min} = -a F_{\max} / I_{xx} + (N_1 + P_1) - tg \theta (N_2 + P_2) \quad (23.2)$$

and

$$\ddot{\theta}_{\max} = a F_{\max} / I_{xx} + (N_1 + P_1) - tg \theta (N_2 + P_2) \quad (23.3)$$

Then, reference values for instant attitude angles accelerations can be obtained from the solution of the following linear-quadratic optimization problem:

$$\min_{\alpha, \beta} (\ddot{\theta}_c - \alpha)^2 + (\ddot{\phi}_c - \beta)^2 \quad (24.1)$$

with

$$\ddot{\phi}_{\min} \leq \beta \leq \ddot{\phi}_{\max} \quad (24.2)$$

$$\ddot{\theta}_{\min} \leq \alpha - tg \theta \beta \leq \ddot{\theta}_{\max} \quad (24.3)$$

Observe that the solution of this problem is equal to $(\ddot{\theta}_c, \ddot{\phi}_c)$ if it is feasible with respect to constraints (24.2) and (24.3), otherwise the solution will be on the border of the convex feasible set.

Then if α^* and β^* are solution of this problem, u_1 and u_2 are given by:

$$\begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = -M(\underline{Y})^{-1} (N(\underline{X}) \underline{V} + P(\underline{X}) - \begin{bmatrix} \alpha^* \\ \beta^* \end{bmatrix}) \quad (25)$$

In the case of v_1 and v_2 (relations (21.2)) and considering the expressions of θ_c and ϕ_c the above approach leads to the consideration of an intricate non convex optimization problem. A different approach is proposed here. Let λ be such as:

$$\ddot{x}_r = \lambda \ddot{x}_c, \ddot{y}_r = \lambda \ddot{y}_c, \ddot{z}_r + g = \lambda(\ddot{z}_c + g) \quad (26)$$

then according to (18.1) and (18.2):

$$\theta_r = \theta_c \quad \text{and} \quad \phi_r = \phi_c \quad (27)$$

Feasible reference values for $\ddot{x}_r, \ddot{y}_r, \ddot{z}_r$ and $\ddot{\psi}_r$ can be obtained from the solution of the following linear-quadratic optimization problem:

$$\min_{\lambda, \mu} (\lambda - 1)^2 + \eta^2 (\mu - \ddot{\psi}_c)^2 \quad (28.1)$$

with

$$0 \leq (m\sqrt{\ddot{x}_c^2 + \ddot{y}_c^2 + (\ddot{z}_c + g)^2}) \lambda - \left(\frac{I_{zz} \cos \theta_c}{k \cos \phi_c}\right) \mu \leq 4 F_{\max} \quad (28.2)$$

$$0 \leq (m\sqrt{\ddot{x}_c^2 + \ddot{y}_c^2 + (\ddot{z}_c + g)^2}) \lambda + \left(\frac{I_{zz} \cos \theta_c}{k \cos \phi_c}\right) \mu \leq 4 F_{\max} \quad (28.3)$$

where η is here a time constant. Let λ^* and μ^* be the solution of the above problem, then the control inputs can be taken as:

$$v_1 = \frac{1}{2} (m \lambda^* \sqrt{\ddot{x}_c^2 + \ddot{y}_c^2 + (\ddot{z}_c + g)^2} - \frac{I_{zz} \cos \theta_c}{k \cos \phi_c} \mu^*) \quad (29.1)$$

$$v_2 = \frac{1}{2} (m \lambda^* \sqrt{\ddot{x}_c^2 + \ddot{y}_c^2 + (\ddot{z}_c + g)^2} + \frac{I_{zz} \cos \theta_c}{k \cos \phi_c} \mu^*) \quad (29.2)$$

Then, F_1, F_2, F_3, F_4 given by:

$$F_1 = (u_1 + v_1)/2 \quad F_2 = (u_2 + v_2)/2 \quad (30.1)$$

$$F_3 = (v_1 - u_1)/2 \quad F_4 = (v_2 - u_2)/2 \quad (30.1)$$

satisfy condition (5).

V. CASE STUDIES

Here we considered two cases: one where the objective is to hover at an initial position of coordinates x_0, y_0, z_0 while acquiring a new orientation ψ_1 , and one where the rotorcraft is tracking the helicoidal trajectory of equations:

$$\left. \begin{aligned} x_c(t) &= \rho \cos vt \\ y_c(t) &= \rho \sin vt \\ z_c &= \delta + \gamma t \\ \psi_c(t) &= vt + \pi/2 \end{aligned} \right\} \quad (31)$$

where ρ is a constant radius and γ is a constant path angle.

A. Heading control at hover

In this case we get the guidance control laws:

$$v_1 = \frac{1}{2} (m g - \frac{I_{zz}}{k} \ddot{\psi}_c) \quad v_2 = \frac{1}{2} (m g + \frac{I_{zz}}{k} \ddot{\psi}_c) \quad (32)$$

with the following reference values for the attitude angles:

$$\theta_c = 0 \quad \text{and} \quad \phi_c = 0 \quad (33)$$

Here the heading acceleration is given by:

$$\ddot{\psi}_c = -2 \zeta_{\psi} \omega_{\psi} r - \omega_{\psi}^2 (\psi - \psi_1) \quad (34)$$

Starting from an horizontal attitude ($\theta(0)=0, \phi(0)=0$), attitude inputs u_1 and u_2 given by relation (14) remain equal to zero. Then, figures 3 and 4 display some simulation results:

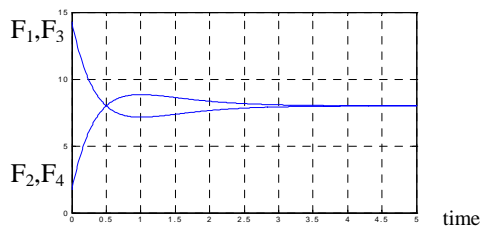


Fig 3. Hover control inputs

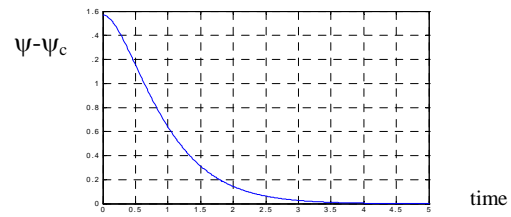


Fig 4. Heading response during hover

B. Trajectory tracking case

In this case we get the guidance control laws:

$$v_1 = v_2 = \frac{1}{2} (m \sqrt{\rho^2 v^2 + g^2}) \quad (38)$$

Here the permanent reference values for the attitude angles are such as:

$$\theta_c = 0 \quad (39.1)$$

and

$$\sin \phi_c = -\frac{\rho v^2}{\sqrt{\rho^2 v^4 + g^2}} \quad (39.2)$$

and the desired guidance and orientation accelerations are given by:

$$\left. \begin{aligned} \ddot{x}_c &= -\rho v^2 \cos(vt) \\ \ddot{y}_c &= -\rho v^2 \sin(vt) \\ \ddot{z}_c &= 0, \quad \ddot{\psi}_c = 0 \end{aligned} \right\} \quad (40)$$

Attitude inputs are given by relation (14) where now:

$$M^{-1} = \begin{bmatrix} I_{yy}/(a \cos \phi) & 0 \\ tg \theta \, tg \phi \, I_{xx}/a & -I_{xx}/a \end{bmatrix} \quad (41)$$

and

$$\underline{N}(\underline{X})' = [0 \quad 0] \quad (41)$$

In figures 5 to 7 simulation results are displayed where at initial time the rotorcraft is hovering:

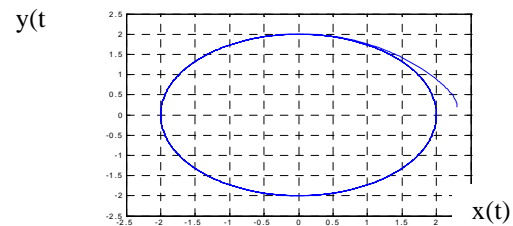


Fig 4. Evolution of rotorcraft horizontal track

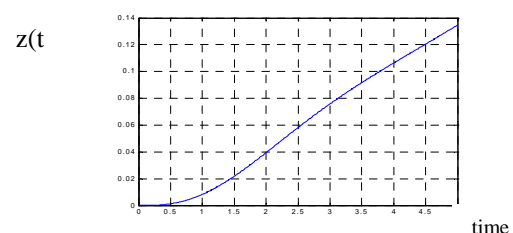


Fig 5. Evolution of rotorcraft altitude

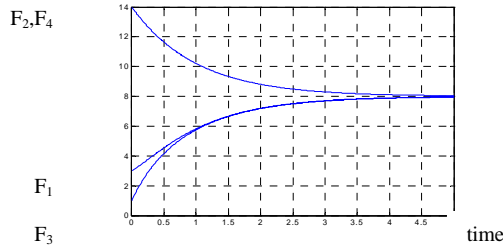


Fig 7. Rotorcraft trajectory tracking inputs

VI. CONCLUSION

In this communication a nonlinear inverse control technique applied to rotorcraft trajectory tracking has been considered. This approach leads to the design of a two level control structure based on analytical laws. However the possibility of actuators saturation has led to the design of a supervision layer whose objective is to modify references values for the nonlinear inverse control laws so that the tracking performance is maintained as much as possible. The applicability of the proposed approach appear acceptable since the complexity of the resulting optimization problems to be solved online appear to be rather low. Then the proposed approach should enlarge the field of applications for rotorcraft. This approach could be adapted to the supervision of actuators saturation with other autonomous aircraft.

APPENDIX

The rotor engine dynamics are characterized by the relation between the input voltage V_a and the angular rate ω . A possible model of rotor dynamics is given by:

$$\dot{\omega}(t) = -\frac{1}{\tau}\omega(t) - K_Q\omega(t)^2 + (K_{V_a}/\tau)V_a(t) \quad (\text{A.1})$$

with $\omega(0) = \omega_0$, where τ , K_Q and K_{V_a} are given positive parameters and where the voltage input is such as:

$$0 \leq V_a \leq V_{\max} \quad (\text{A.2})$$

with a negligible time response for the voltage generator.

The step response ($V_a = \text{constant}$) of the rotor is solution of the scalar *Riccati* equation:

$$\dot{\omega}(t) = -\frac{1}{\tau}\omega(t) - K_Q\omega(t)^2 + (K_{V_a}/\tau)V_a \quad (\text{A.3})$$

with $\omega(0) = \omega_0$.

A particular solution ω_l of the associated differential equation is such as:

$$\omega_l = \frac{1}{2\tau K_Q}(\sqrt{1 + 4K_{V_a}K_Q\tau V_a} - 1) \quad (\text{A.4})$$

In the general case, the solution of (A.3) can be written as

$$\omega(t) = \omega_l + \frac{1}{\frac{1}{\omega(0) - \omega_l} + K_Q\tau'(1 - e^{-t/\tau'})}} e^{-t/\tau'} \quad (\text{A.5})$$

$$\tau' = \tau / \sqrt{1 + 4K_{V_a}K_Q\tau V_a} \quad (\text{A.6})$$

$$\text{and} \quad \lim_{t \rightarrow +\infty} \omega(t) = \omega_l \quad (\text{A.7})$$

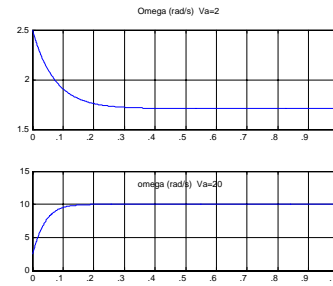


Fig 8. Two examples of rotor step response

It appears from figure 8 that the dynamics of the rotor may be close to those of a first order linear system with time constant τ' , but as can be seen in (A.6), this value is a function of V_a . If the desired dynamics for the output are such as:

$$\dot{\omega} = -\frac{1}{T}(\omega - \omega_c) \quad (\text{A.8})$$

where T is a very small time constant V_a can be chosen such as:

$$V_a(t) = \frac{1}{K_{V_a}}((1 - \frac{\tau}{T})\omega(t) + \frac{\tau}{T}\omega_c + \tau K_Q\omega(t)^2) \quad (\text{A.9})$$

The rotor forces are then given by:

$$F_i = f \omega_i^2 \quad i = 1 \text{ to } 4 \quad (\text{A.10})$$

while the rotor moments are given by:

$$M_i = k F_i \quad i = 1 \text{ to } 4 \quad (\text{A.11})$$

where f and k are positive constant parameters.

REFERENCES

- [1] G. Hoffmann, D.G. Rajnarayan, S.L. Waslander, D. Dostal, J.S. Jang, and C.J. Tomlin, "The Stanford Testbed of Autonomous Rotorcraft for Multi-Agent Control", *23rd Digital Avionics Systems Conference*, Salt Lake City, UT, November 2004.
- [2] H. K. Khalil, "Nonlinear Systems", Prentice Hall, 3rd Ed., 2002.
- [3] S.N. Singh and A.A. Schy, "Nonlinear decoupled control synthesis for maneuvering aircraft", Proceedings of the 1978 IEEE conference on Decision and Control, Piscataway, NJ, 1978.
- [4] R. Ghosh and C.J. Tomlin, "Nonlinear Inverse Dynamic Control for Model-based Flight", Proceeding of AIAA-GNC, 2000.
- [5] R. Asep, T.J. Shen, and F. Mora-Camino, "An application of the nonlinear inverse technique to flight-path supervision and control", Proceedings of the 9th International Conference of Systems Engineering, Las Vegas, NV, 1993.
- [6] B. Etkin, and L. R. Reid, "Dynamics of Flight-Stability and Control". John Wiley & Sons. New York, NY, 1996.
- [7] W.C. Lu, and F. Mora-Camino, "Flight Mechanics and Differential Flatness". Dincon 04, Proceedings of Dynamics and Control Conference, Ilha Solteira, Brazil, pp. 830-839, 2004.
- [8] A. Drouin, A.B. Ramos and F. Mora-Camino, "Rotorcraft Trajectory Tracking by Nonlinear Inverse Control", Dincon, São Paulo, 2007.
- [9] S.A. Beltran Mendoza, O. Lengerke, H. Gonzalez Acuña and F. Mora-Camino, "Control PID de altura de un quadrirotor", 3rd International Mechatronic Conference, Bucaramanga, Colombia, October 2011.