Empty Containers Inventory System with Fuzzy Demand

Chien-Min Su, Sheng-Long Kao, Ming-Fung Yang, Cheng-Hao Lin

ABSTRACT – In this research, with the trend of globalization; trade inequality leads to differences in the throughput of ports. Ports with large number of export goods will face the problem of the lacking of containers. In the model, the cost of dispatching containers is divided into three parts: container holding cost, container ordering cost and container leasing cost. According to the status of inventory level, cost can be effectively reduced according to which method is used to dispatch the container. Due to the reason of demand for each period cannot be accurately predicted, therefore fuzzy theory is added in the research in order to obtain a more realistic and accurate result. Finally, this research cooperates Matlab R2014b in calculating the result for the hypothesis model.

Index Terms—Trade inequality, empty containers scheduling, fuzzy theory

I. INTRODUCTION

As a low-cost, high-capacity transport vehicle, shipping is definitely an important and indispensable means of trade in international trade. For shipping, cost is the primary consideration. The import and export volume of each port is different. If there are more ports than imported ports, there will be problems with excessive containers; if ports with less imports than exports, there will be a shortage of containers. For ports that are out of the containers, the cost of container dispatching is a challenge. If there is a set of well-considered models, the cost can be effectively controlled.

Yang M.F. (2006) uses fuzzy theory to create fuzzy assumptions about the integration of inventory model demand and productivity, also uses the reduced distance method to estimate the total cost. During the process of fuzzification and defuzzification, each procedure is described in detail.

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Rafael Diaz et al. (2011) compared the number of empty containers in the port to a more cost-effective plan for container redistribution, comparing three prediction methods for numerical analysis. Won Young Yun et al. (2011) established a complete cost estimation model, taking into account the differences in the off-season season, and decided to order or lease containers according to the inventory status. The numerical analysis is a complete discussion of the variables.

Ata Allah Taleizadeh et al. (2012) assumes that the time between replenishment is an independent random variable. Although the demand is treated as a fuzzy number, for the shortage, the combination of reverse order and loss sales is considered and proposed. The hybrid algorithm compares the differences in performance of each algorithm. Seved Mohsen Mousavi and Seyed Taghi Akhavan Niaki (2012) considered the capacity location allocation problem, where the customer demand and location are uncertain, the location follows the normal probability distribution, and the distance between the location and the customer uses Euclidean and Euclidean Reed square, also uses the hybrid intelligent algorithm to calculate the simplex algorithm, fuzzy simulation and improved genetic algorithm. Yuanji Xu and Jinsong Hu (2012) develop a newsboy model with stochastic fuzzy demand that maximizes profits for more accurately describe the uncertain demand. Through the credibility measure of fuzzy events, the expected profit model is given and the concavity of the profit function is revealed. A hybrid algorithm combining random fuzzy simulation and simultaneous perturbation stochastic approximation is designed to obtain the optimal order quantity.

Min Huang et al. (2013) studied the distributed capacity allocation of a single facility between different organizations with fuzzy requirements, established a fuzzy optimization model related to each organization and facility, and transformed the fuzzy optimization model into parameters based on fuzzy theory. The fuzzy optimization model is transformed into a parametric programming model, and an interactive algorithm is proposed to solve these parametric programming models. Feyzan Arikan (2013) argues that multi-sourcing supplier selection issues are multi-objective linear programming problems with fuzzy demand levels. Minimizing total currency costs, maximizing total quality, and maximizing the level of service for purchasing items are three goals. Through a two-stage addition method to solve the problem, in the first stage, the ideal solution is used to find the desired level of each target. In the second stage, the fuzzy additive model is solved by Chen&Tsai's fuzzy model. S. Sarkar and T. Chakrabarti (2013) studied the EPQ calculation model in the fuzzy sense, in which the shortage is allowed and the delivery is fully extended. After defuzzification, the total cost in the fuzzy model is lower than the clear model. Shengju Sang (2014) studies market demand as a positive trapezoidal fuzzy number in a three-stage supply chain consisting of one manufacturer, one manufacturer and one retailer. In the fuzzy demand environment, the method of fuzzy set theory is used to concentrate. The decision system and the cross-revenue sharing (SRS) contract model are proposed, and the optimal solution of the fuzzy model is proposed.

I. Burhan Turksen et al. (2015) explored the fuzzy inventory model considering the (s, S) type in the Nakagami demand distribution. The membership function of the fuzzy update function can be obtained through the demand distribution with fuzzy extended parameters. The membership function obtains the result of numerical analysis. Vineet Mittal et al. (2015) consider a joint two-tier inventory system in which a single supplier provides a single type of product to a single buyer, demonstrating the optimality of inventory decisions under non-fuzzy and fuzzy requirements through models. Wasim and Sahidul (2016) analyzed the allowable out-of-stock fuzzy inventory system with degraded products. In the fuzzy environment, all necessary parameters are treated as triangular fuzzy numbers, with the aim of minimizing the cost function.

Jianhua Yang et al. (2015) developed a support plan for emergency parts in the face of large-scale emergencies in the large equipment spare parts supply network. Taking into account the occurrence of emergencies, information theory is used to prioritize the weights of emergency repair stations. The paper proposes emergency response time and demand satisfaction functions, aiming at time, demand satisfaction and cost constraints, and establishing under fuzzy requirements. Support the model. M.F. Yang (2015) studies a three-level integrated inventory model for the development of defective products, reprocessing and credit periods. Assuming fuzzy requirements, numerical analysis is used to observe the impact of fuzzy demand on inventory strategy and total profit.

During previous researches, fuzzy is often used in the calculation of demand in order to generate results that fit better to the reality. For example, M.F. Yang et al. (2010) built a two-echelon inventory model for fuzzy demand in a supply chain, while at the same time took approach with mutual beneficial pricing.

This research took reference of the traditional model of container dispatching cost, and construct a model with the addition of fuzzy theory. Demand for each period during offpeak season cannot be accurately predicted in reality. With the application of fuzzy theory, the demand is assumed to be a triangular fuzzy number; which able to provide a result that is in line with the reality environment. At the end, numerical analysis is performed with the use of software; also by changing the upper and lower limits of the fuzzy number, sensitive analysis is done.

II. MODEL FORMULATION

When building the model, demand will change according to peak or off-season. Holding cost can be calculated by taking the remaining inventory of the previous period as the beginning inventory of the current period; then by adding the previous order quantity and deduct the lease amount, the inventory level of the current period will be obtained. Decision of ordering will be considered by the inventory limits and reorder point of the current season, then ordering cost may be calculated. If there are situations of lacking containers, the insufficient amount is fulfilled by leasing;

rental cost is then calculated. Finally, total cost can be estimated by adding the above costs.

A. Ordering and Leasing Policy

When the container's inventory level is below the low bound (reorder point), the container can be dispatched by ordering; but there will be a lead time for the goods from order to delivery. This research assumes that four periods of lead time are required for ordering containers in the ith period; the goods will be delivered in the i+4 period.

There are situations while containers are urgently needed, but ordering containers are not efficient enough to satisfy immediately needs. Therefore, container leasing took place. The lacking containers can be fully compensated with container leasing, but the cost will be higher than regular containers ordering. Since it is a leasing container, there will be problem due to the containers have to be returned at certain point. This research also assumed that in the *i*th period lease of containers, although the required quantity can be fulfilled immediately, but the goods need to be returned in the (i+4) period.

B. Assumption

- (1) Only one type of container will be considered.
- (2) Demand will increase during high demand season.
- (3) Demand will decrease during low demand season.
- (4) Leasing container will have 0 lead time.
- (5) Leasing containers should be returned after (i+4) periods.
- (6) Ordering containers will have a lead time that is stable for 4 periods.

(7) Demand and supply of empty containers per week are independent variables.

C. Notation

- S_1 Highest inventory level in low demand season.
- Reorder point in low demand season. s_1
- S_2 Highest inventory level in high demand season.
- Reorder point in high demand season. S_2
- Customer demand in the ith period. D_i
- Vi The amount of containers returned from customers in the ith period.
- Net inventory at the beginning of the ith period. Ni
- Inventory level in the ith period. Hi
- Inventory level in the lead time of ith period. I_i
- Order quantity in the *i*th period. 0_i
- Lease in the i^{th} period. Li
- C_n Inventory holding cost per unit.
- C_f C_o Fixed-ordering cost.
- Ordering cost per unit.
- C_l Leasing cost per unit.
- TC_i Total cost of the *i*th period

 \tilde{D}_{i-1} is a low demand triangular fuzzy number, $\widetilde{\mathbf{D}}_{i-1} = (\mathbf{D}_1 - \Delta_1, \mathbf{D}_1, \mathbf{D}_1 + \Delta_2), 0 < \Delta_1 < \mathbf{D}, 0 < \Delta_2,$ while Δ_1, Δ_2 is determined by the decision maker.

 \widetilde{D}_i is a high demand triangular fuzzy number, $\widetilde{D}_{i} = (D_{2} - \Delta_{3}, D_{2}, D_{2} + \Delta_{4}), 0 < \Delta_{3} < D, 0 < \Delta_{4},$ while Δ_3, Δ_4 is determined by the decision maker. Proceedings of the International MultiConference of Engineers and Computer Scientists 2019 IMECS 2019, March 13-15, 2019, Hong Kong

D. Model building

The choice of (S_1, s_1) or (S_2, s_2) depends on the differences between low and high demand season, using the previous remaining stock as the net stock at the beginning of the present period:

$$N_i = H_{i-1} + V_{i-1} - \widetilde{D}_{i-1} + L_{i-1}$$
(1)

Holding cost will be calculated by the use of the net stock at the beginning of the present period:

$$NC_i = N_i * C_n \tag{2}$$

The current inventory level can be obtained by subtracting the lease amount in period (i - 4)(lead time); followed by adding the order amount in period (i - 4)(lead time):

$$H_i = N_i + O_{i-4} - L_{i-4} \tag{3}$$

Then,

$$I_i = H_i + \sum_{t=-3}^{0} O_{i+1} + \sum_{i=0}^{3} E[V_i] - \sum_{i=0}^{3} E[\tilde{D}_i]$$
(4)

Determine $(l_i \ge s)$, if $(l_i \ge s)$, ordering is not in need; order $[S - MX(0, I_i)]$ will be placed while $(l_i < s)$:

$$\begin{cases} O_i = 0 & while(I_i \ge s) \\ O_i = S - MX(0, I_i) & while(I_i < s) \end{cases}$$
(5)

Then,

$$OC_i = O_i * C_o \tag{6}$$

Determine $(H_i + V_i \ge \tilde{D}_i)$, if $(H_i + V_i \ge \tilde{D}_i)$, leasing is not in need; lease $[(\tilde{D}_i - (H_i + V_i)]$ will be place while $(H_i + V_i < \tilde{D}_i)$:

$$\begin{cases} L_{i} = 0 & while(H_{i} + V_{i} \ge \widetilde{D}_{i}) \\ L_{i} = \widetilde{D}_{i} - (H_{i} + V_{i}) & while(H_{i} + V_{i} < \widetilde{D}_{i}) \end{cases}$$
(7)

Then,

$$LC_i = L_i * C_l \tag{8}$$

Finally, take NC_i , OC_i , and LC_i and add them together to obtain the total cost of the dispatching container.

$$TC_i = NC_i + OC_i + LC_i \tag{9}$$

Definition 1. From kaufmann and Gupta (1991), Zimmermann (1996), Yao and Wu (2000), for a fuzzy set $\tilde{D} \in \Omega$ and ore [0,1], the α -cut of the fuzzy set \tilde{D} is $D(\alpha) = \{x \in \Omega | \mu_D(x) \ge \alpha\} = [D_L(\alpha), D_U(\alpha)],$

$$\begin{cases} D_L(\alpha) = a + \alpha(b - d) \\ D_U(\alpha) = c - \alpha(c - b) \end{cases}$$
(10)

We can obtain the following equation. The signed distance of \tilde{D} to $\tilde{0}_1$ is defined as:

$$d(\tilde{D}, \tilde{0}_{1}) = \int_{0}^{t} d\{[D_{L}(\alpha), D_{U}(\alpha)], \tilde{0}_{1}\} d\alpha$$
$$= \frac{1}{2} \int_{0}^{1} [D_{L}(\alpha), D_{U}(\alpha)] d\alpha \qquad (11)$$

So the equation will become:

$$d(\tilde{D}, \tilde{0}_1) = \frac{1}{2} \int_0^1 [D_L(\alpha), D_U(\alpha)] d\alpha = \frac{1}{4} (2b + a + c)$$
(12)

Streamlined distance method is used to the defuzzication of TC_i

$$\widetilde{D} = d(\widetilde{D}, \widetilde{0}_1) = \frac{1}{4} [(D - \Delta_1) + 2D + (D + \Delta_2)] = D + \frac{1}{4} (\Delta_2 - \Delta_1)$$
(13)

Then,

$$\begin{cases} \widetilde{D}_{i-1} = D_1 + \frac{1}{4}(\Delta_2 - \Delta_1) \\ \widetilde{D}_i = D_2 + \frac{1}{4}(\Delta_4 - \Delta_3) \end{cases}$$
(14)

Replace the original with the above formula :

$$N_i = H_{i-1} + V_{i-1} - [D_1 + \frac{1}{4}(\Delta_2 - \Delta_1)] + L_{i-1} \quad (15)$$

Then,

$$H_{i} = H_{i-1} + V_{i-1} - D_{1} - \frac{1}{4}(\Delta_{4} - \Delta_{3}) + L_{i-1} + O_{i-4} - L_{i-4}$$
(16)

Then,

$$I_{i} = H_{i-1} + V_{i-1} - D_{1} - \frac{1}{4}(\Delta_{2} - \Delta_{1}) + L_{i-1} + O_{i-4} - L_{i-4} + \sum_{t=-3}^{0} O_{i+1} + \sum_{i=0}^{3} E[V_{i}] - \sum_{i=0}^{3} E\left[D_{2} + \frac{1}{4}(\Delta_{4} - \Delta_{3})\right]$$
(17)

Then,

$$\begin{cases} while \ \{H_i + V_i \ge [D_2 + \frac{1}{4}(\Delta_4 - \Delta_3)]\}, \\ L_i = 0 \end{cases}$$

$$while \ \{H_i + V_i < [D_2 + \frac{1}{4}(\Delta_4 - \Delta_3)]\}, \\ L_i = \left[D_2 + \frac{1}{4}(\Delta_4 - \Delta_3)\right] - (H_i + V_i) \end{cases}$$

$$(18)$$

By substituting fuzzy demand into the original equation, the initial inventory quantity, the order quantity, and the lease quantity with fuzzy demand quantity can be obtained; and the dispatching cost can be recalculated.

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III. NUMERICAL ANALYSIS

The calculation for the numerical analysis uses Matlab R2014b; the 500th period is used as a reference for analyzing. Data assumptions for D_i , V_i , S_i , s_i and various costs factors (holding costs per unit, ordering cost per unit, fixed-ordering costs and leasing costs) in the off-peak season are made in TABLE I and TABLE II; while TABLE III does sensitivity analysis for changes in Δ .

TABLE I

D_i AND V_i IN MOLIOR LOW DEMAND							
D_i in high	D_i in low	V_i in high	V_i in high				
demand season	demand season	demand season	demand season				
300	200	220	150				

TABLE II							
	S	i, Si	AND	VARIOU	JS COSTS	FACTOR	S
<i>S</i> ₁	S_1	S_2	<i>s</i> ₂	Holding	Ordering	Fixed-	Leasing
				costs	costs	ordering	costs
				per unit	per unit	costs	per unit

2000

60

130

40

TABLE III NUMERICAL EXAMPLE RESULTS

4000

12000

50000

٨	1101			νη με κι δ	<u>50LI5</u>	TC
Δ ₁	Δ ₂	Δ ₃	Δ_4	D_{i-1}	D_i	
20	40	30	10	295	205	410000
			20	297.5	205	195000
			30	300	205	220000
			40	302.5	205	335000
			50	305	205	270000
		50	10	290	205	180000
			30	295	205	410000
			50	300	205	220000
			70	305	205	270000
			90	310	205	500000
		100	40	285	205	170000
			70	292.5	205	185000
			100	300	205	220000
			130	307.5	205	445000
			160	315	205	1140000
40	40	30	10	295	200	210000
			20	297.5	200	215000
			30	300	200	580000
			40	302.5	200	575000
			50	305	200	870000
		50	10	290	200	200000
			30	295	200	210000
			50	300	200	580000
			70	305	200	870000
			90	310	200	560000
		100	40	285	200	130000
			70	292.5	200	205000
			100	300	200	580000
			130	307.5	200	415000
			160	315	200	670000
40	20	30	10	295	195	230000
			20	297.5	195	235000
			30	300	195	240000
			40	302.5	195	245000
			50	305	195	570000
		50	10	290	195	220000
			30	295	195	230000
			50	300	195	240000
			70	305	195	570000
			90	310	195	860000
		100	40	285	195	210000
		100	70	292.5	195	225000
			100	300	195	240000
			130	307.5	195	565000
			160	315	195	1500000
			100	515	195	1300000



Fig.1. The effect on TC while $\Delta_1 > \Delta_2$ and $\Delta_4 - \Delta_3$ changed

(1) During the situation when $\Delta_1 > \Delta_2$ and Δ_3 are unchangeable, the larger Δ_4 gets, TC will increase as well. (2) TC normally increases obviously while the difference between Δ_3 and Δ_4 increase.

(3) According to the numerical result, the minimum of TC can be obtained while $\Delta_1 = \Delta_2$ and $\Delta_4 - \Delta_3 = -60$.

IV. CONCLUSION

Cost control is one of the problems that cannot be ignored in the maritime industry. With the development of the maritime market, the mastery of demand has become the key to controlling costs. By assuming the demand quantity as a triangular fuzzy number, the decision makers can consider the actual situation and set the upper and lower limits of the demand during different periods; which allow to predict the inventory quantity and the total cost more accurately in the estimation model.

By using Matlab in calculating numerical analysis results, while the larger Δ_4 gets, the total cost will increase substantially, which means that the enterprise should guard against a sudden large amount of demand; otherwise, it will cause huge losses. In order to make the model more suitable to the realistic environment, hopefully this model is able to add more conditions in consideration in the future.

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